

Stand Up Indulgent Gathering

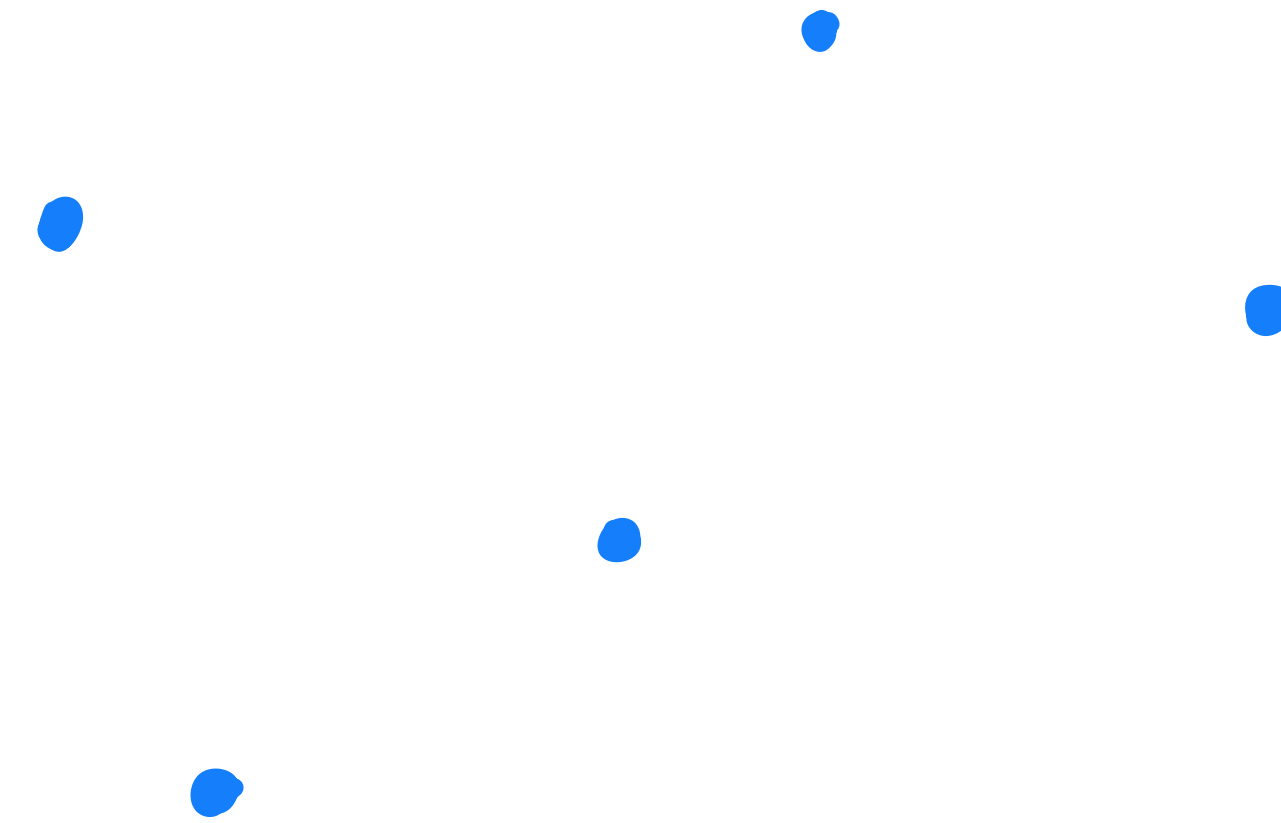
Quentin Bramas, Anissa Lamani, and Sébastien Tixeuil

Strasbourg University, Strasbourg University, and Sorbonne University

Quentin Bramas < bramas@unistra.fr >
ANR ESTATE Workshop, March 16th 2022

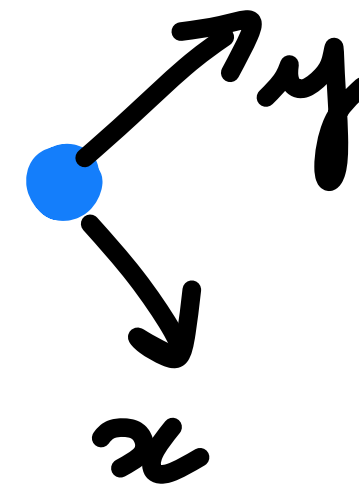
Mobile Autonomous Robots

- Anonymous
- Uniform
- Disoriented
- Silent
- Oblivious



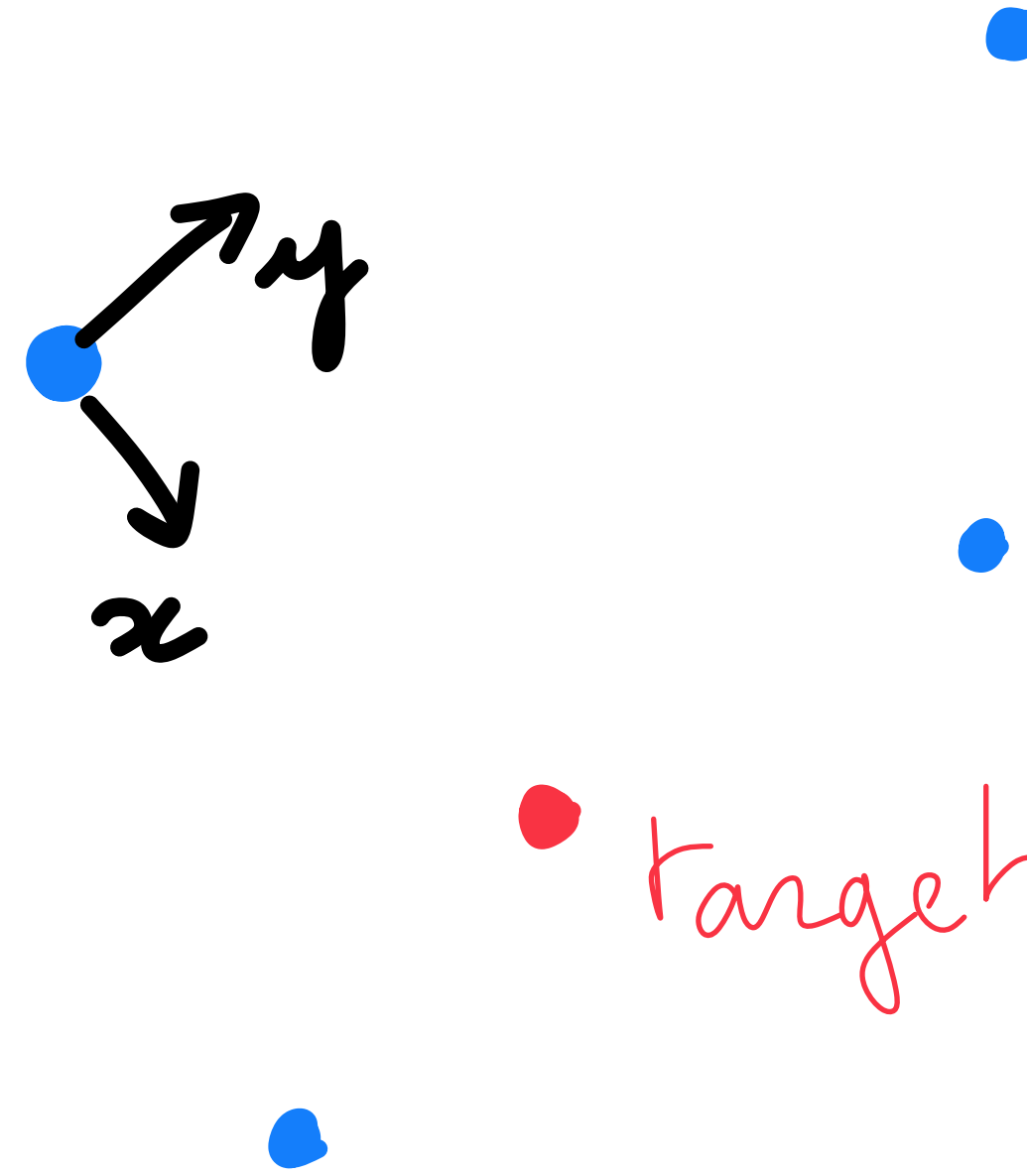
Execution Cycle

- Look
 - Compute
 - Move
-
- Fully-Synchronous
 - Semi-Synchronous



Execution Cycle

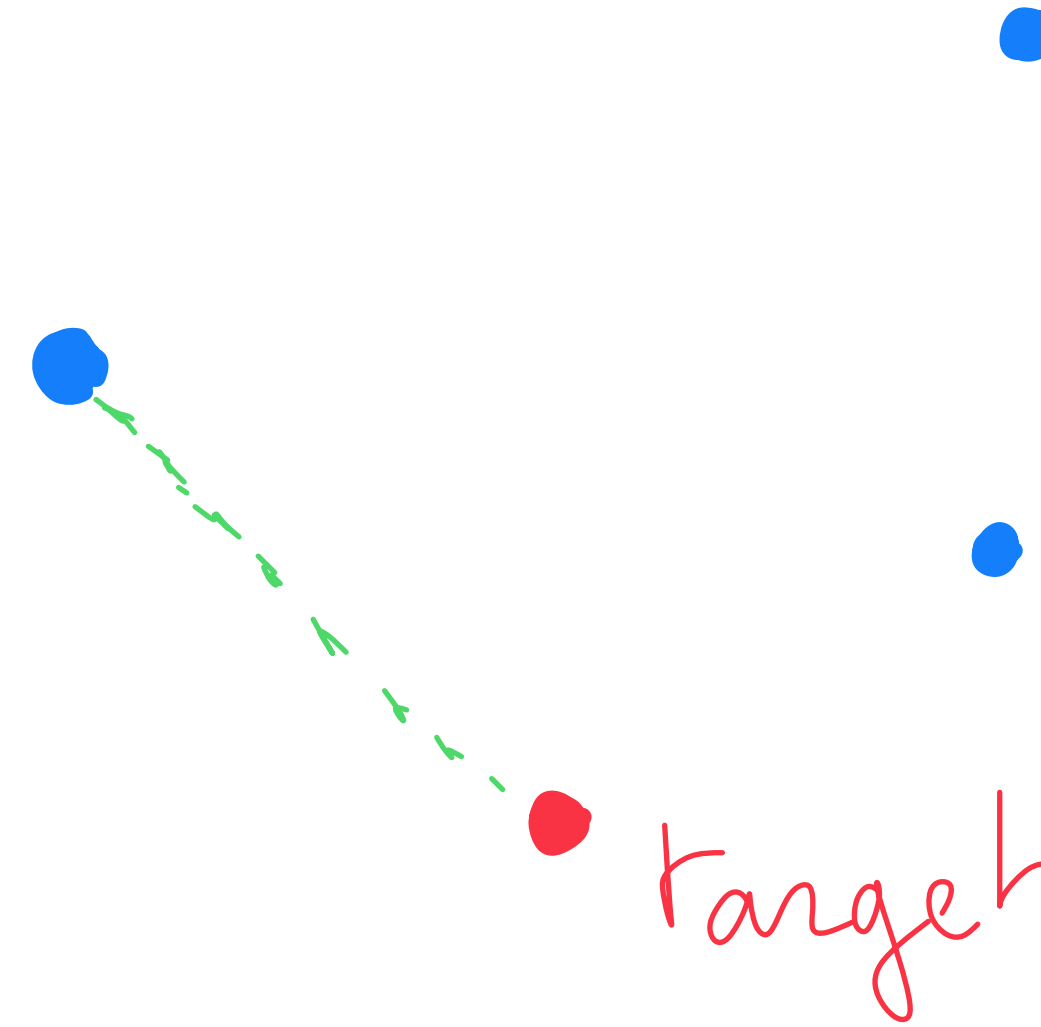
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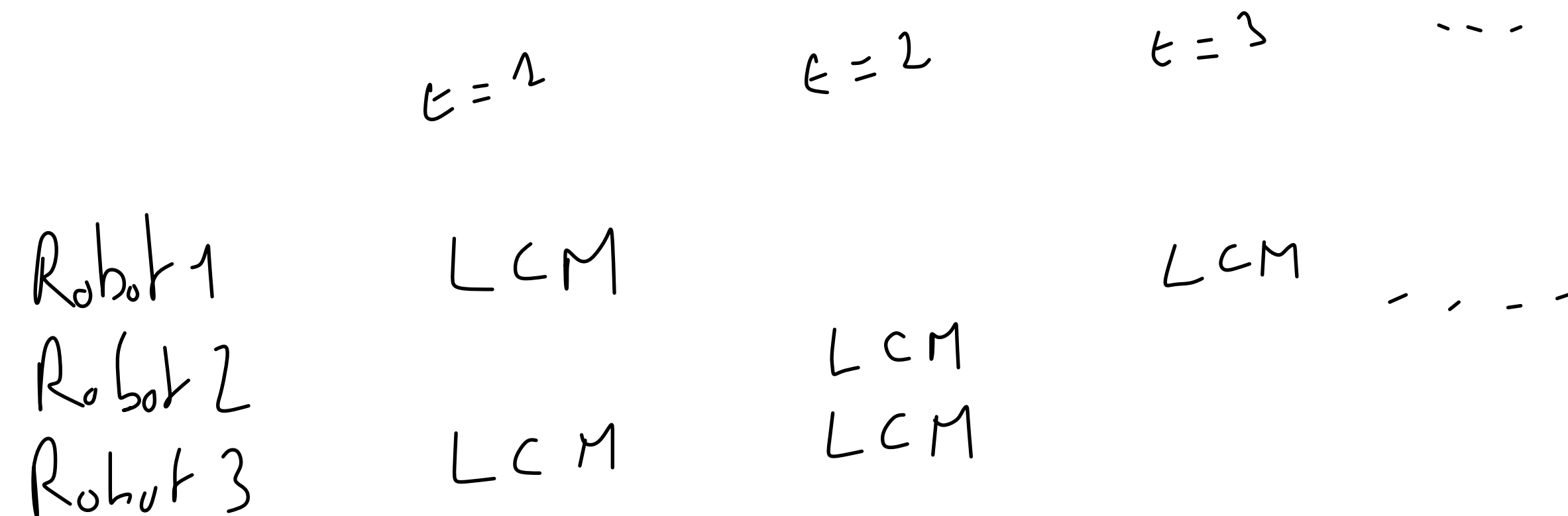
- Fully-Synchronous
- Semi-Synchronous

| | $t=1$ | $t=2$ | $t=3$ | ... |
|---------|-------|-------|-------|-----|
| Robot 1 | LCM | LCM | LCM | ... |
| Robot 2 | LCM | LCM | LCM | ... |
| Robot 3 | LCM | LCM | LCM | ... |

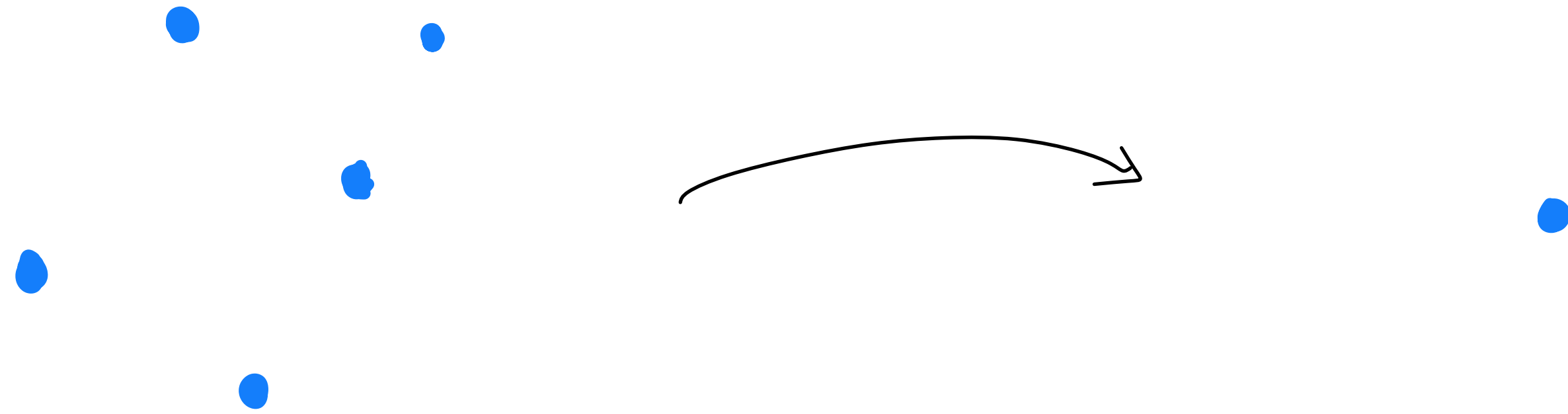
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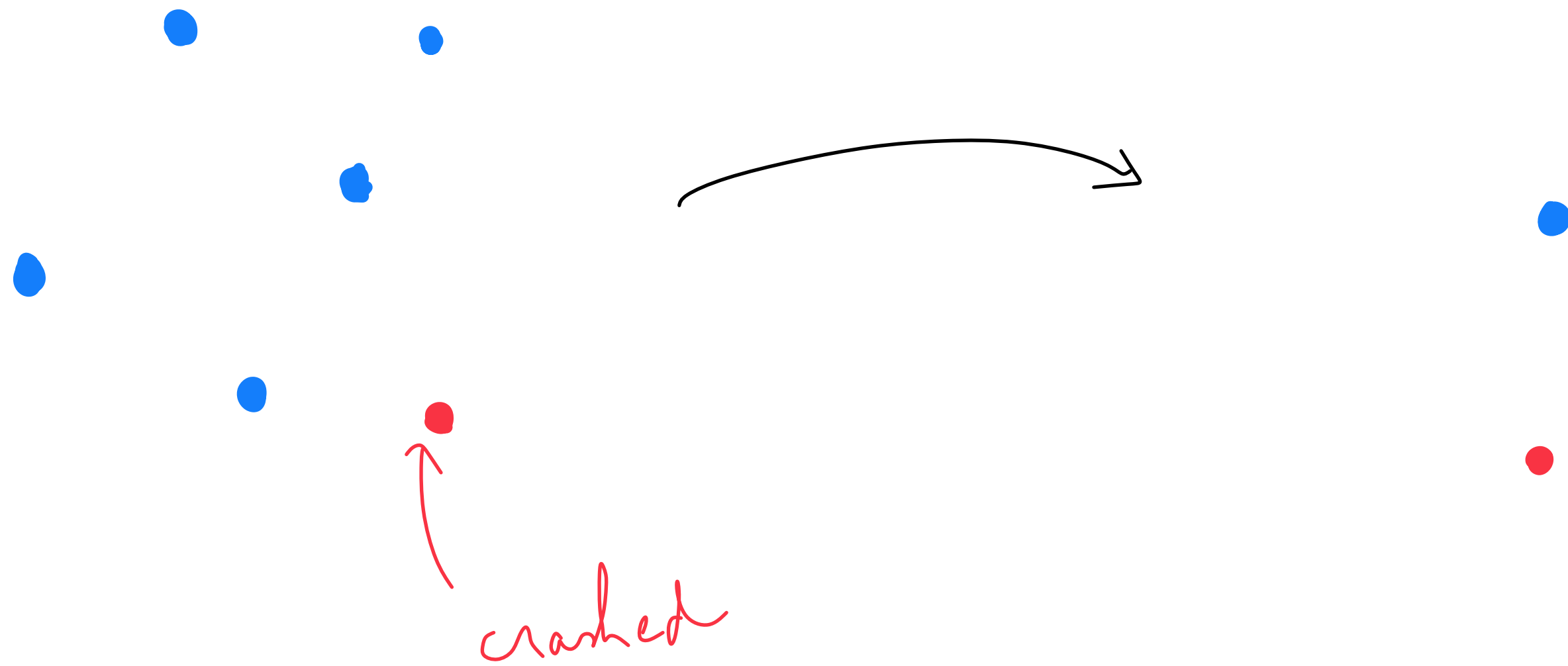


The Fundamental Problem of Gathering



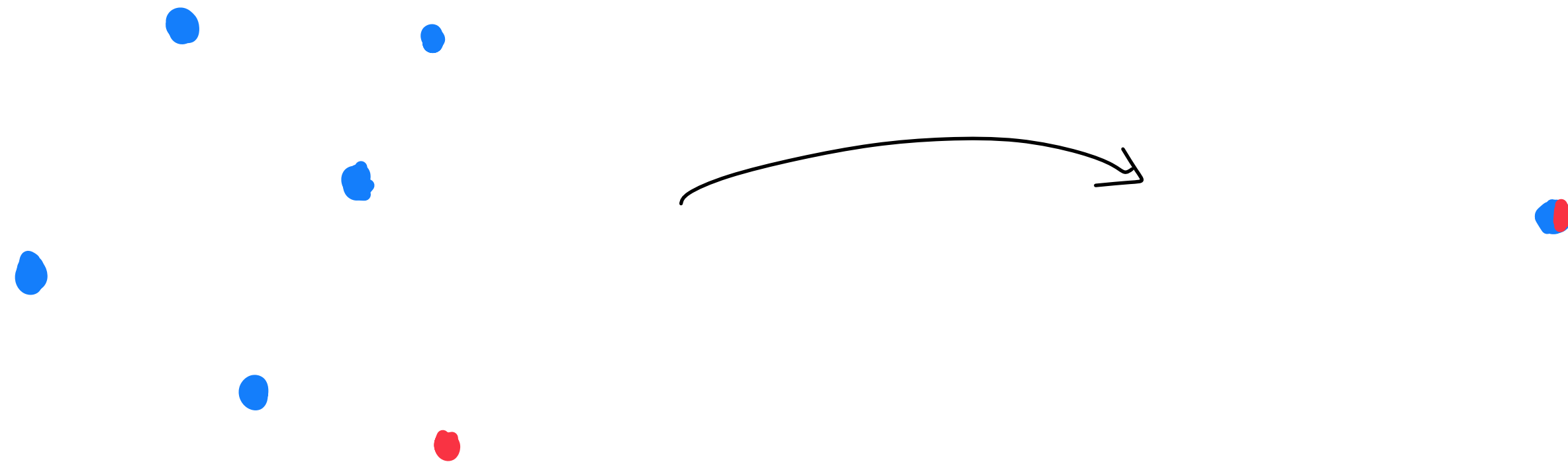
Fault-Tolerant Gathering

Weak Gathering



Stand Up Tolerant Gathering

Strong Gathering



Related Work

Related Work

Gathering:

Related Work

Gathering:

Solvable in FSYNC [SY1999]

Related Work

Gathering:

Solvable in FSYNC [SY1999]

Solvable in SSYNC with common coordinate system. [SY1999]

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Solvable in FSYNC [SY1999]

Solvable in SSYNC with common coordinate system. [SY1999]

Not solvable in SSYNC without common coordinate system. [SY1999]

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Weak Gathering:

Related Work

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Weak Gathering:

Solvable in SSYNC with up to $n-1$ crashes with multiplicity detection and non-bivalent initial configuration [Bramas&Tixeuil2015]

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Stand Up Indulgent Gathering (Strong Gathering):

Related Work

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Stand Up Indulgent Gathering (Strong Gathering):

Unsolvable in SSYNC, even with common coordinate systems and lights with infinite # of colors [SSS2020]

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Solvable in FSYNC with two robots [SSS2020]

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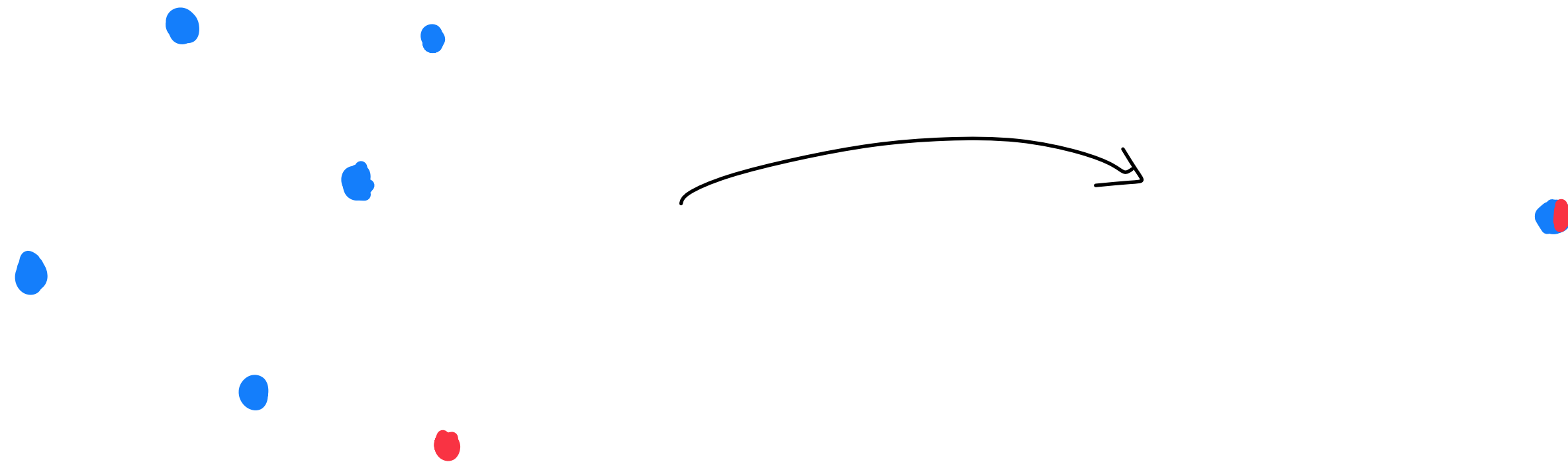
Unsolvable in SSYNC, even with common coordinate systems and lights with infinite # of colors [SSS2020]

Solvable in FSYNC with two robots [SSS2020]

Solvable in FSYNC with n robots [ALGOSENSOR2021]

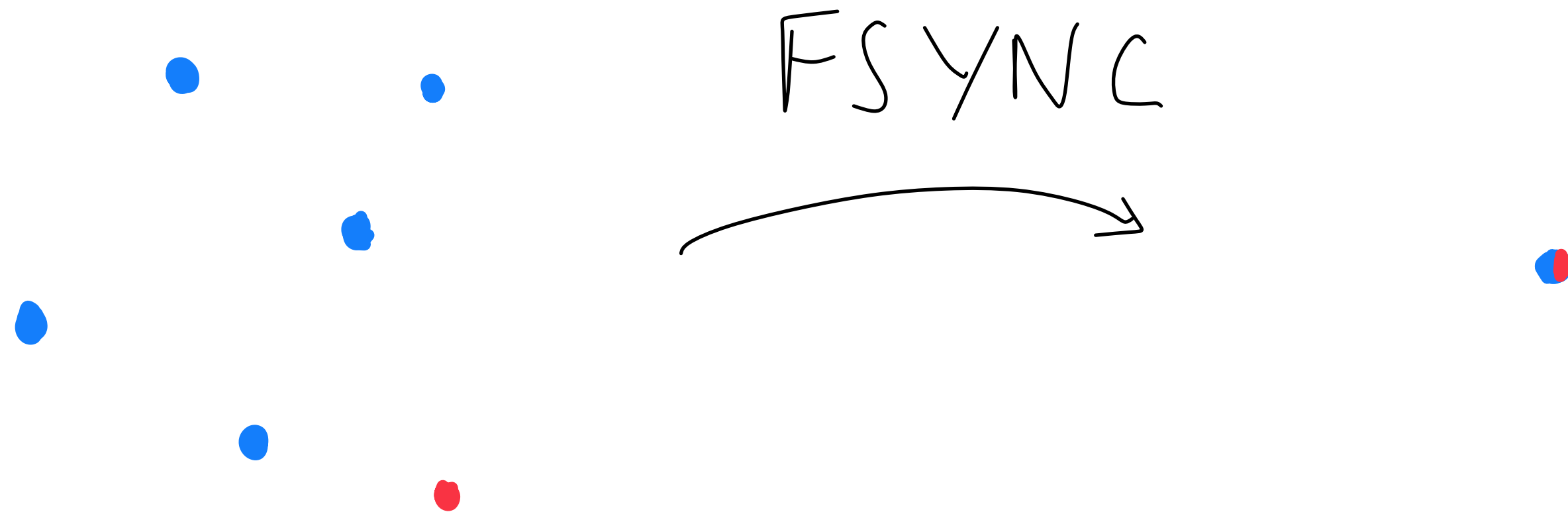
Stand Up Tolerant Gathering

Strong Gathering



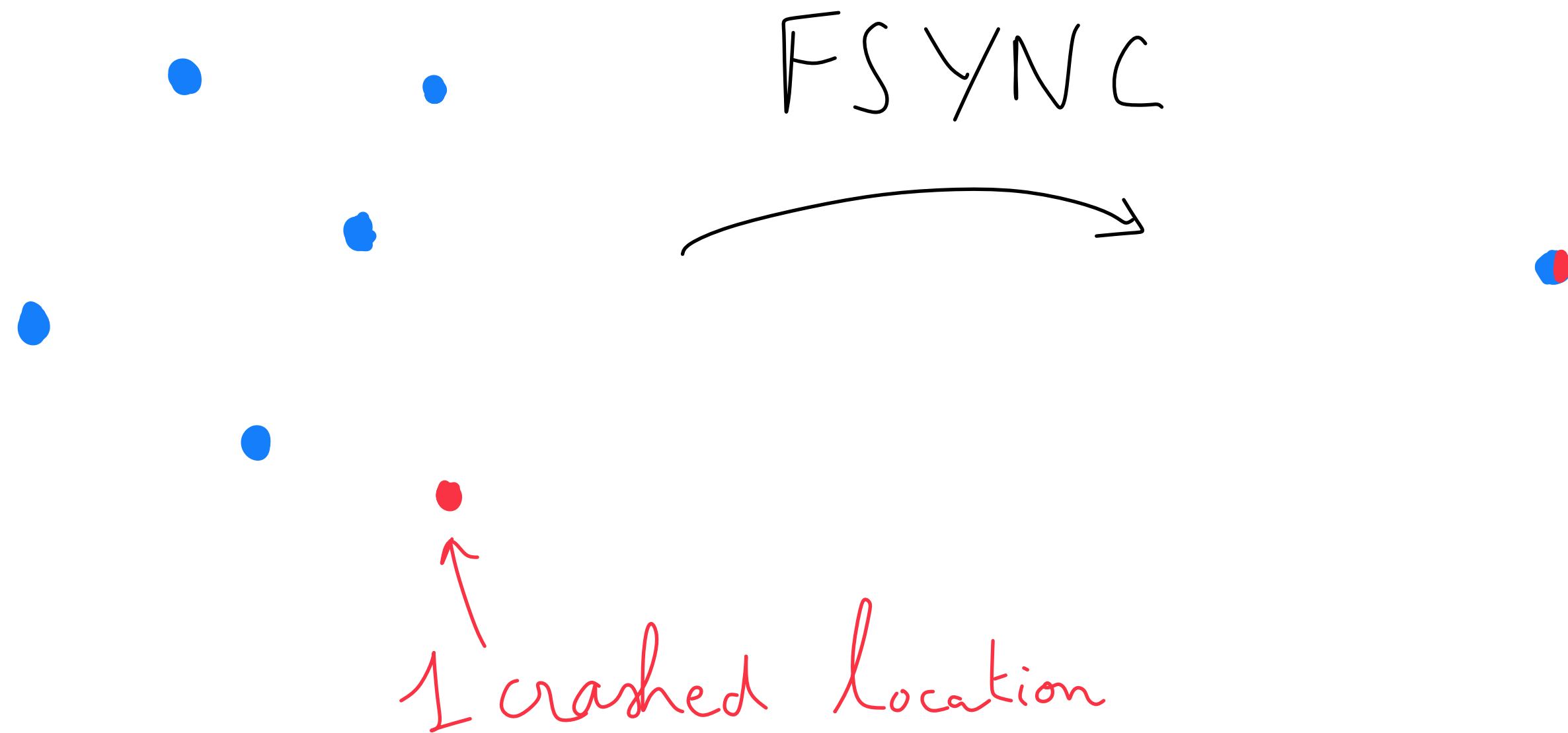
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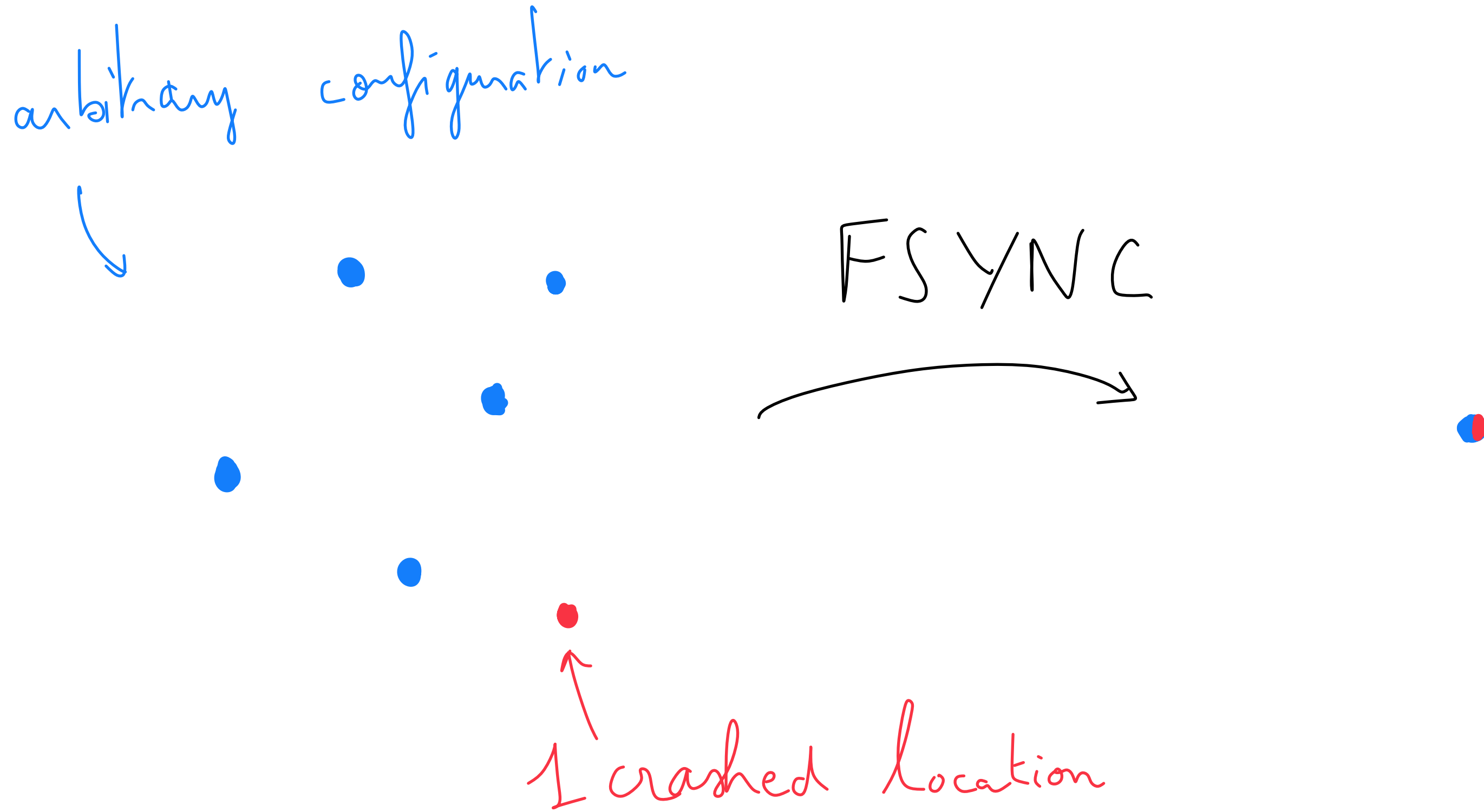
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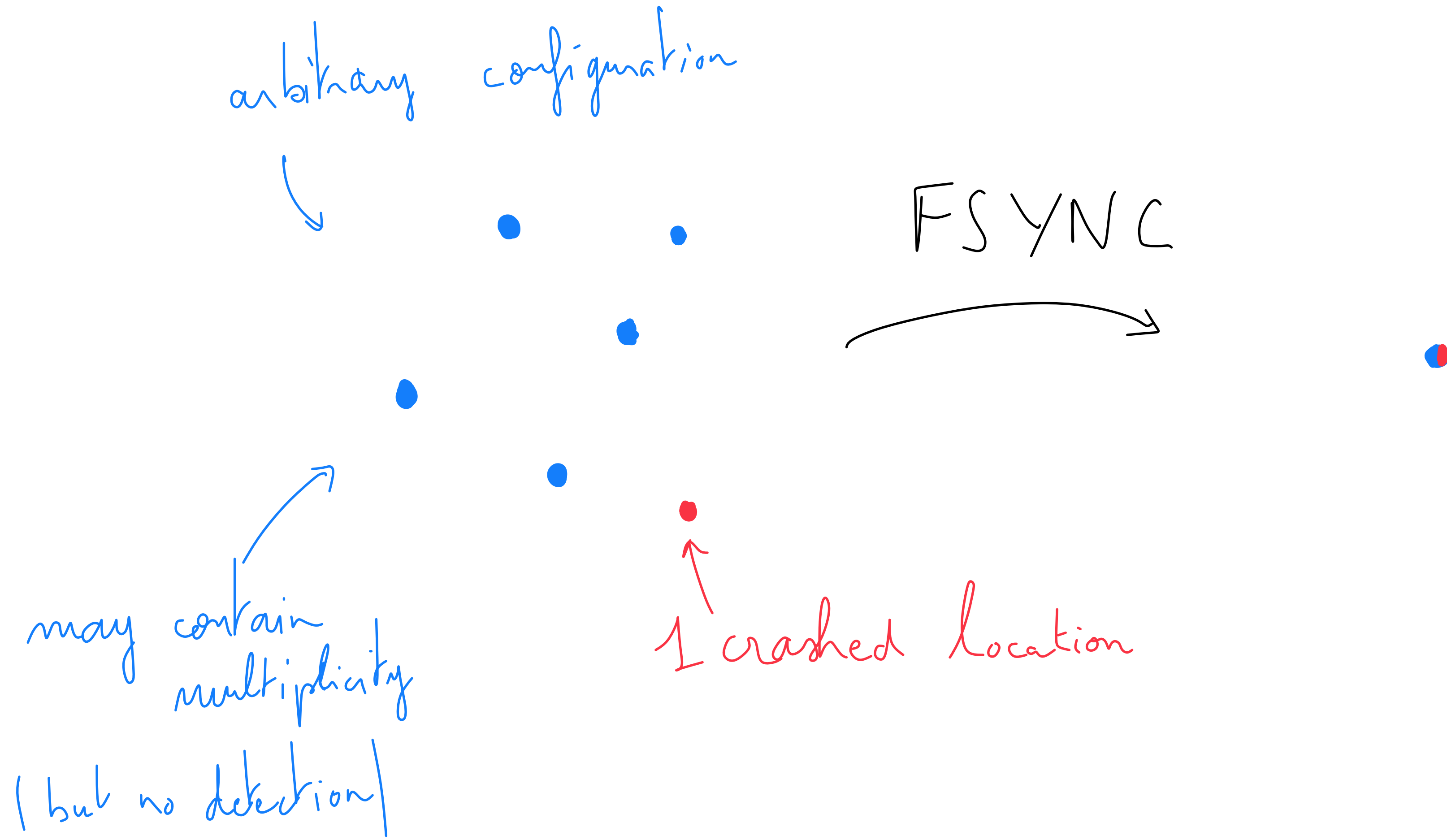
Stand Up Tolerant Gathering

Strong Gathering



Stand Up Tolerant Gathering

Strong Gathering



Impossibility Result

With 2 robots in SSYNC [SSS2020]

Impossibility result

[SSS2020]

Let A be an algorithm that solves the SUIR problem with lights
(infinite memory and communication capabilities)

Impossibility result

[SSS2020]

Let A be an algorithm that solves the SUIR problem with lights
(infinite memory and communication capabilities)

Lemma: *in an execution, if only one robot r is activated, then there is a round when r is dictated to move to the other robot.*

Impossibility result

[SSS2020]

Let A be an algorithm that solves the SUIR problem with lights
(infinite memory and communication capabilities)

Lemma: *in an execution, if only one robot r is activated, then there is a round when r is dictated to move to the other robot.*

Proof: Indeed, if the other robot is crashed, we know that in finite number of rounds r moves to the other robot.

Impossibility result

[SSS2020]

Theorem: *SUIR is not Solvable in SSYNC (even with lights and common coordinate system)*

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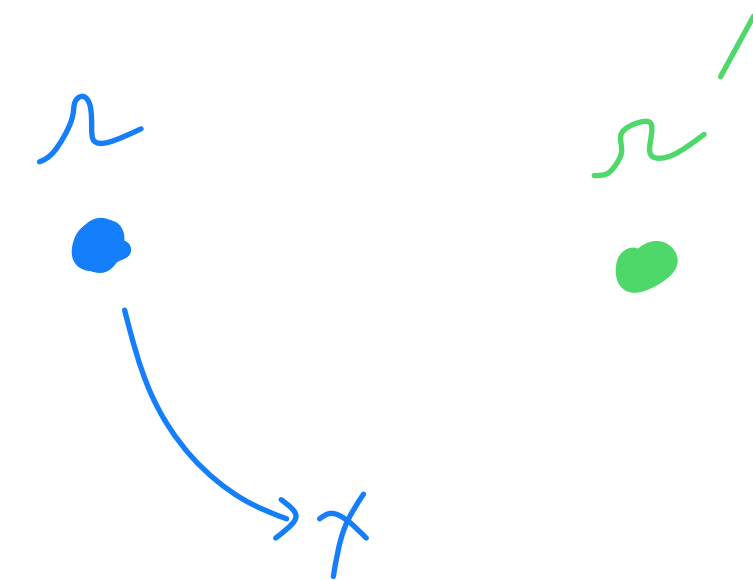
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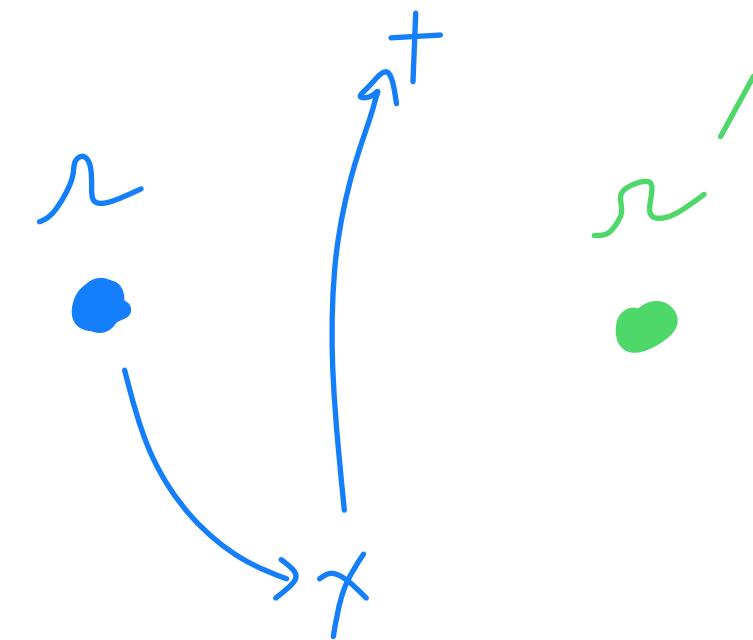
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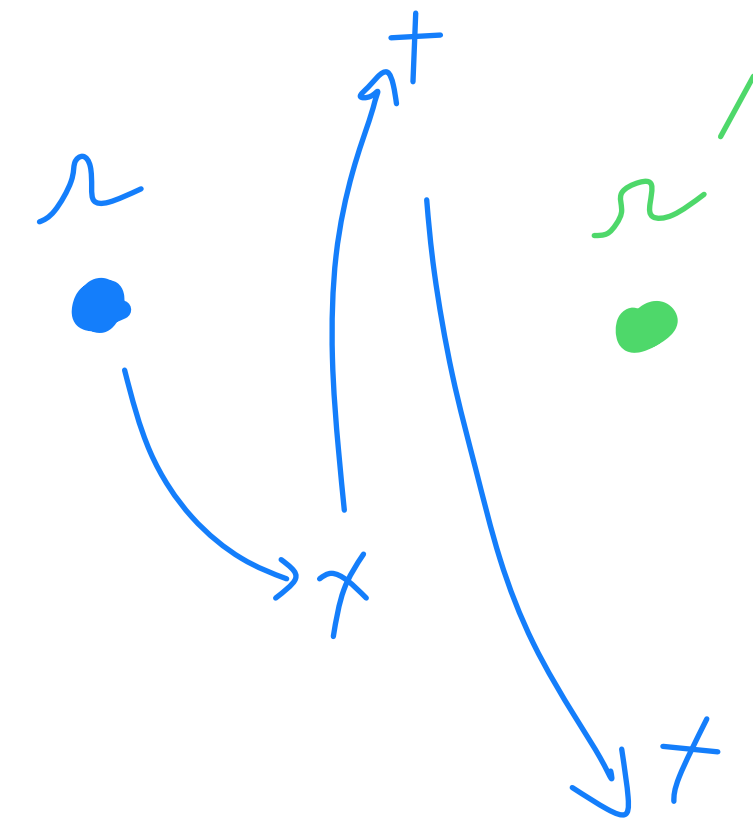
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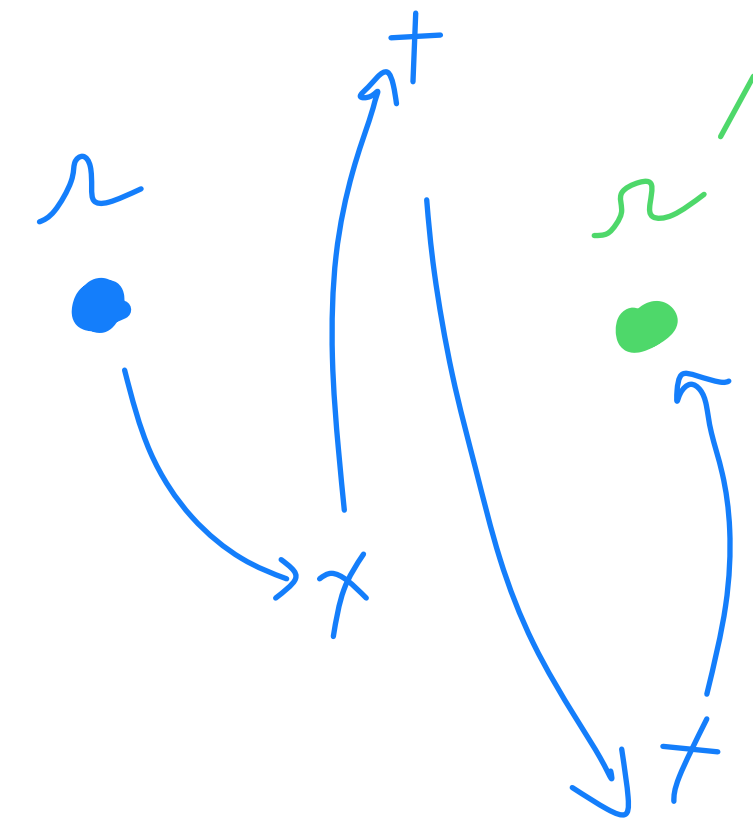
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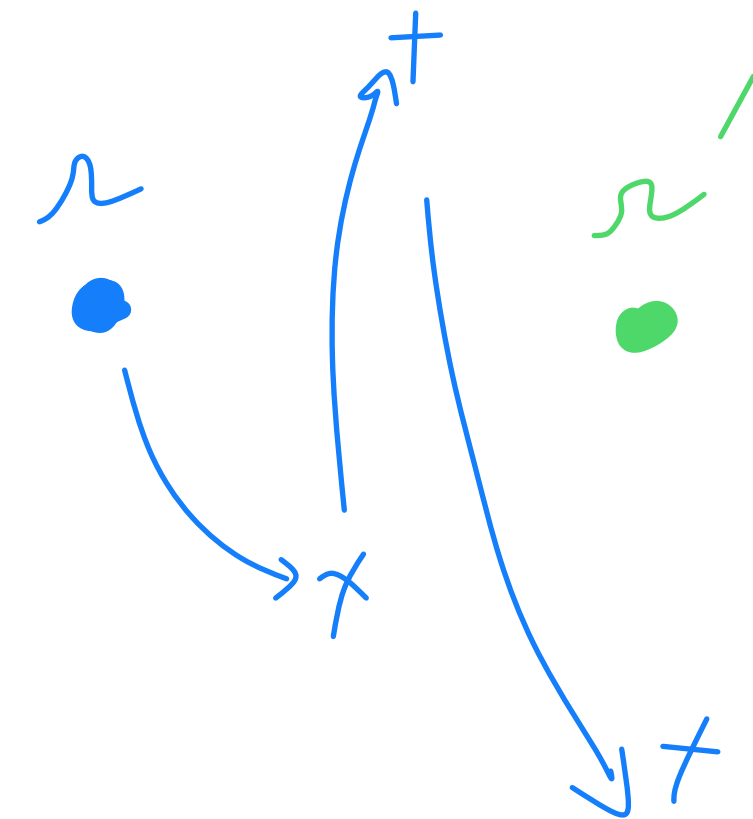
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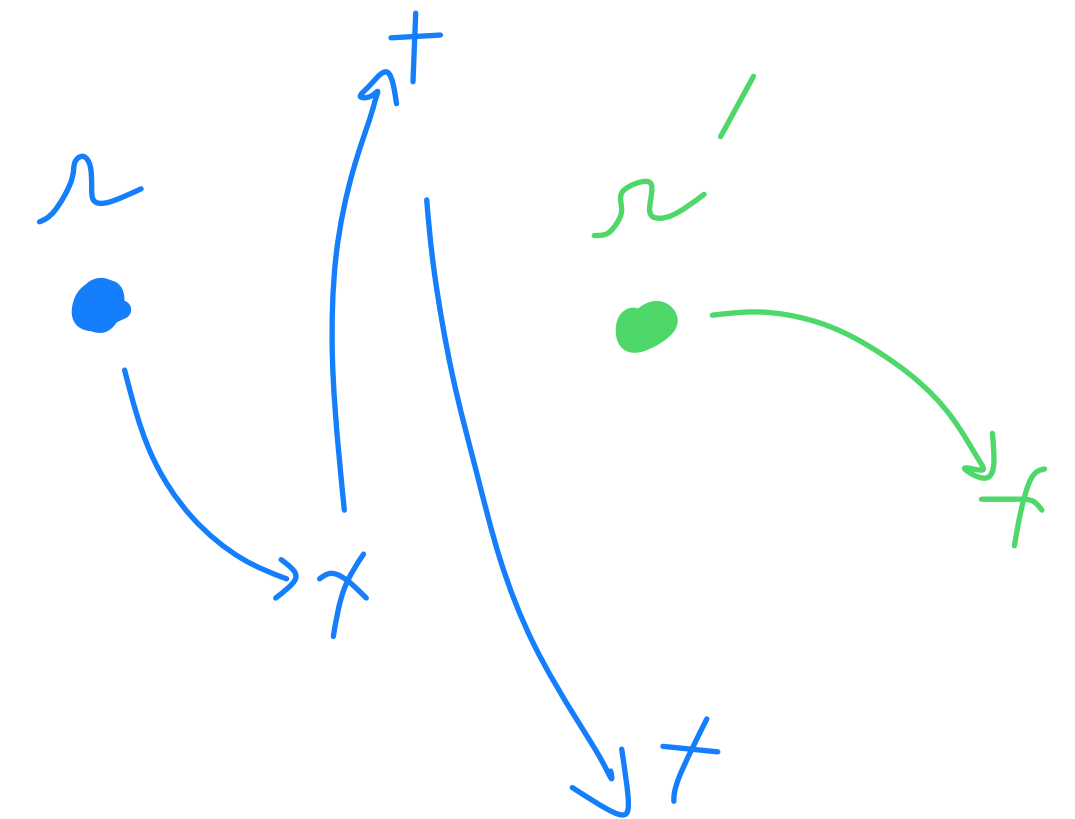
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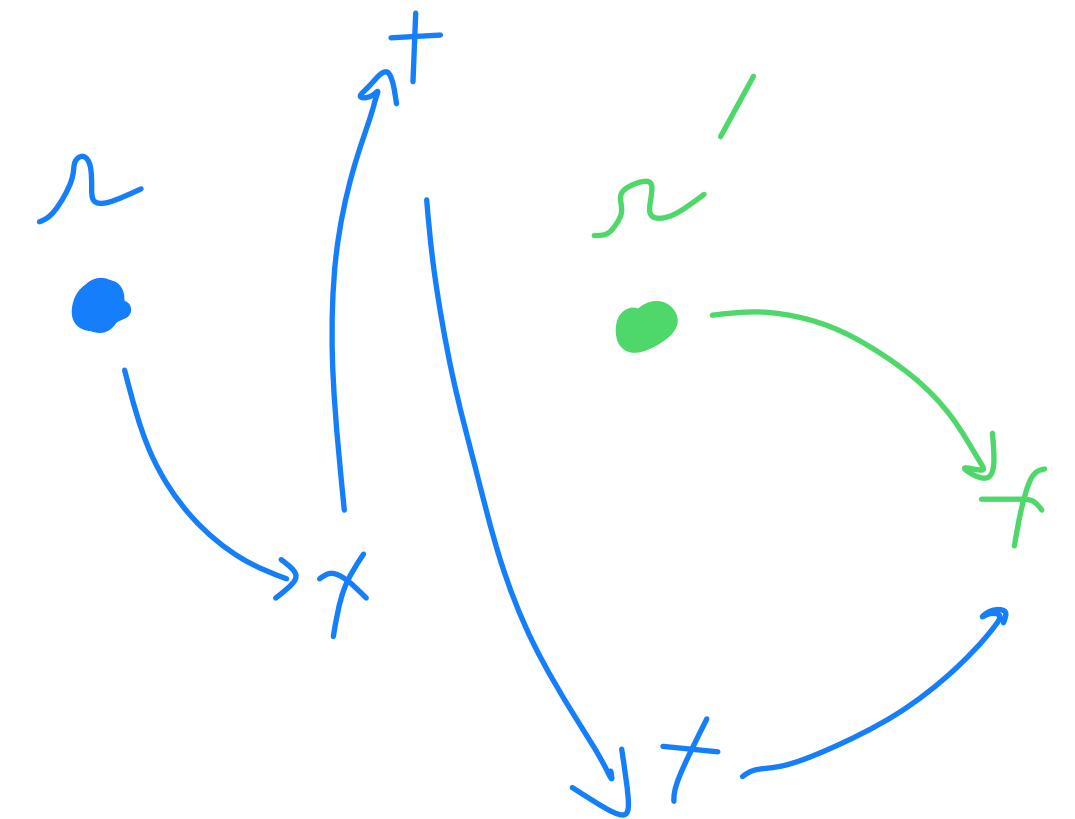
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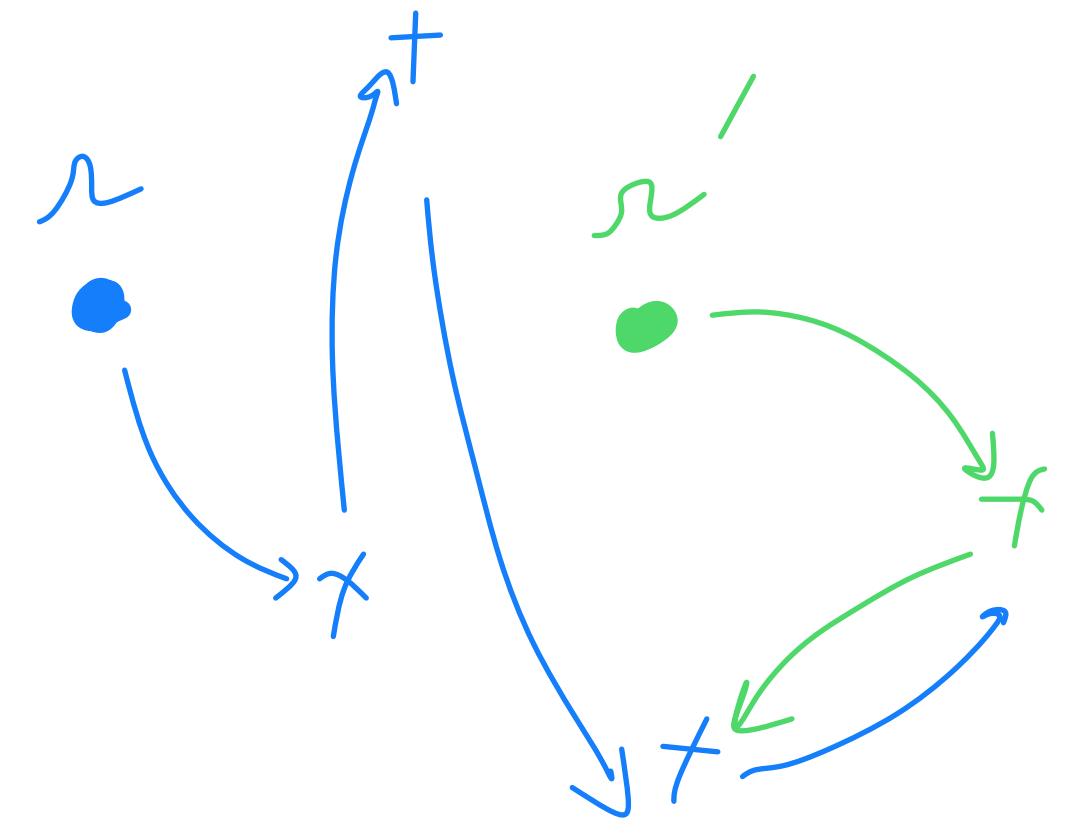
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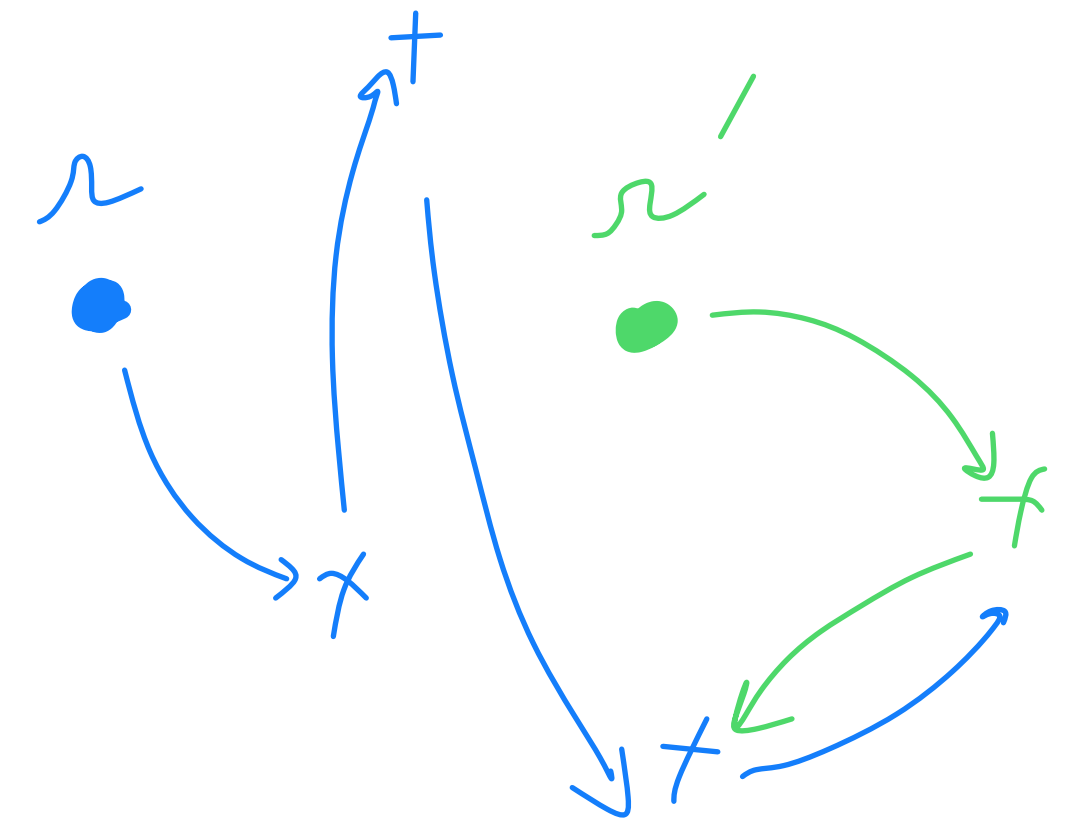
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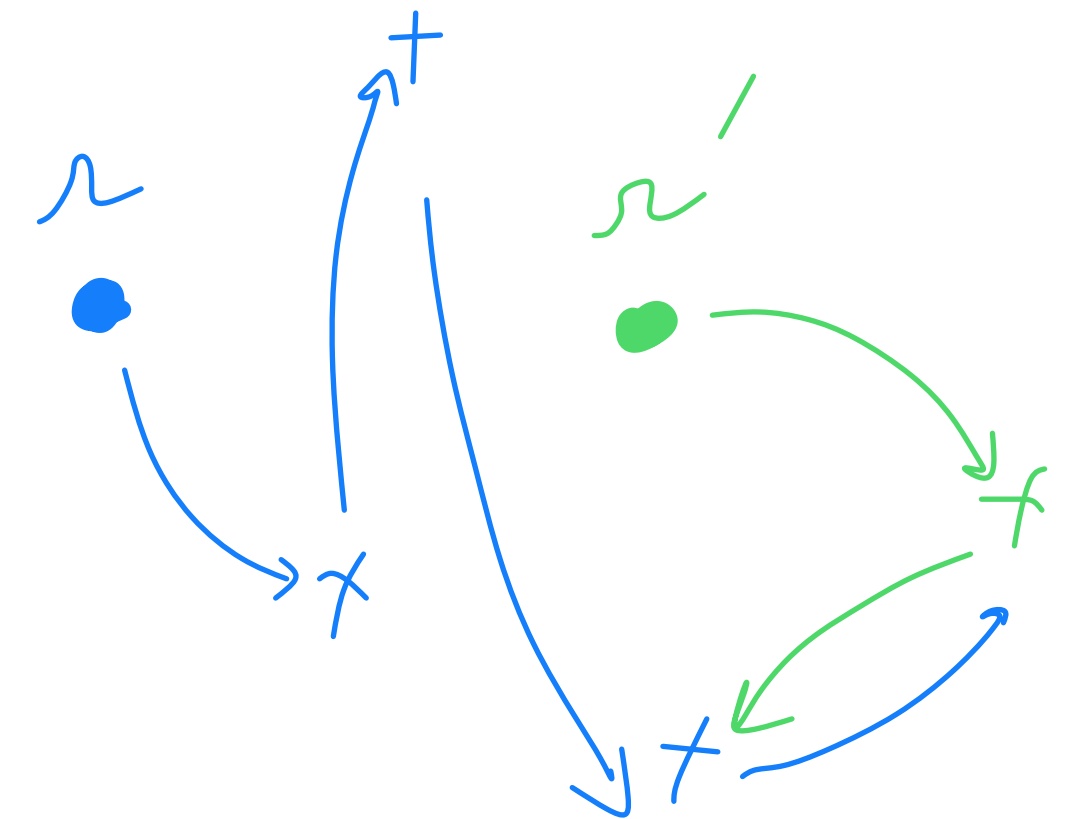
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After each round the robots are not gathered.



Solution with 2 robots

[SSS2020]

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Maybe it seems impossible at first because both robots see the same thing,
hence do the same thing:

Solution with 2 robots

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If they decide to move to the middle

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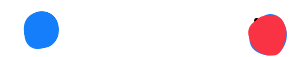


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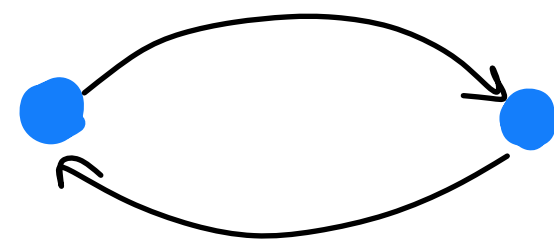
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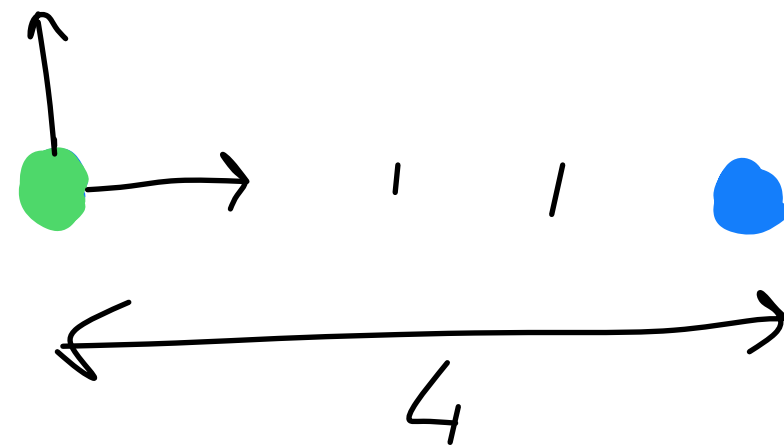
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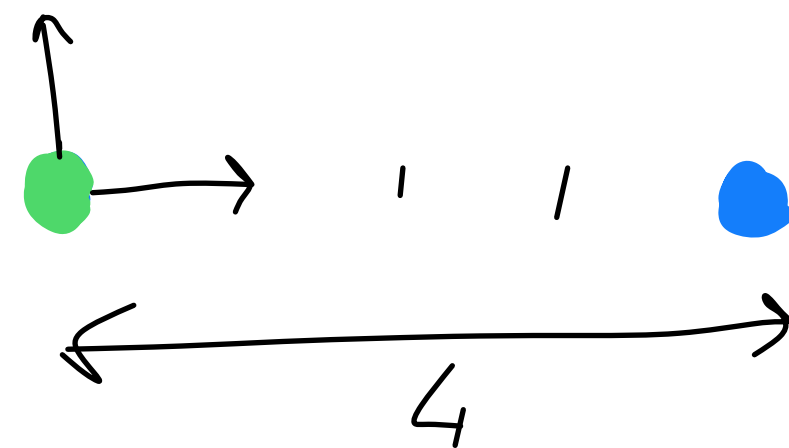
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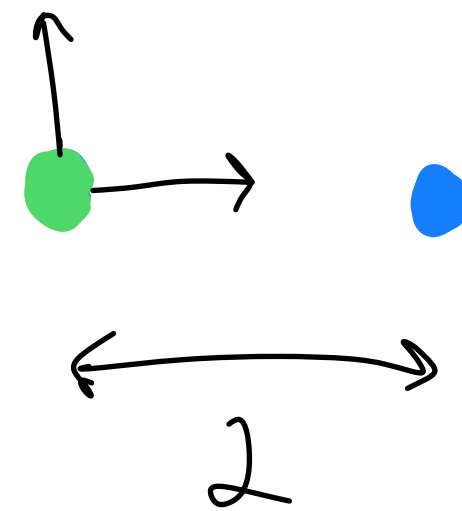
Solution with 2 robots

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After



Solution with 2 robots

[SSS2020]

But if r moves to the middle "alone", r's view has changed!!

And if robots swap their positions, their views have changed!!

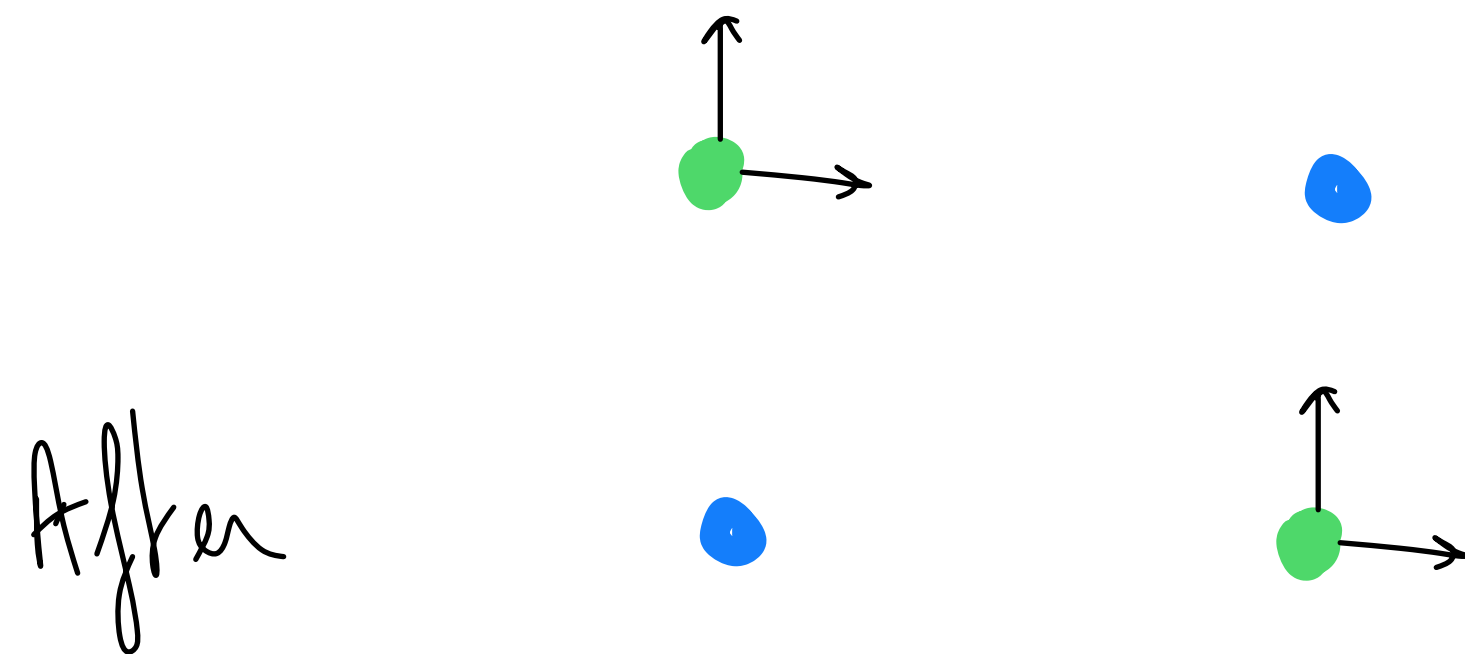


Solution with 2 robots

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Solution with 2 robots

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And if robots swap their positions, their views have changed!!

So the key is to use the distance between the robots and the orientation of the axe, because those are fixed.

Solution with 2 robots

[SSS2020]

If d is the distance between the two robots (seen by robot r , executing the algorithm)

Solution with 2 robots

[SSS2020]

If d is the distance between the two robots (seen by robot r , executing the algorithm)

Let $i \in \mathbb{Z}$ such that $d \in [2^{-i}, 2^{1-i})$

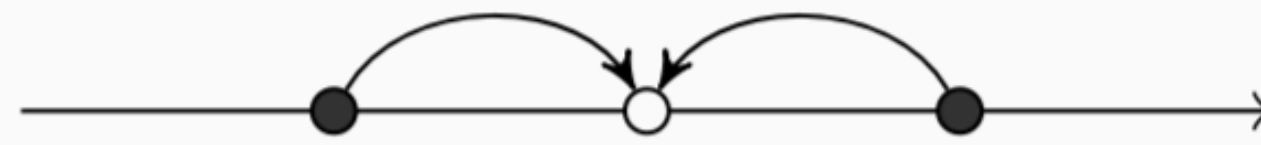
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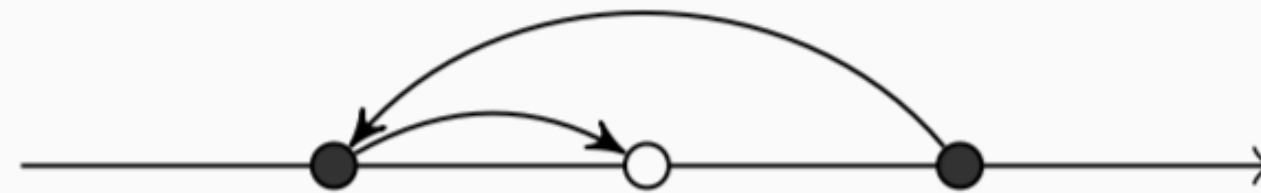
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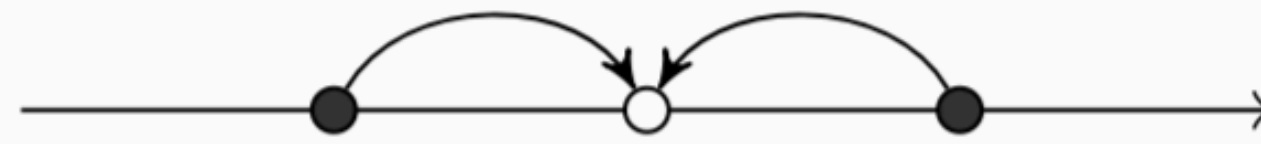
case $i \equiv 0 \pmod{4}$



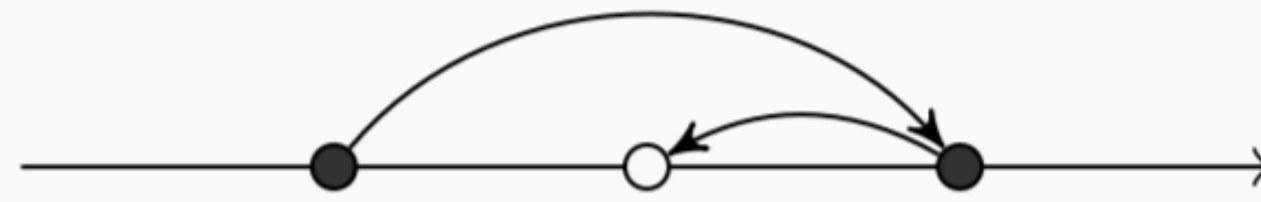
case $i \equiv 1 \pmod{4}$



case $i \equiv 2 \pmod{4}$



case $i \equiv 3 \pmod{4}$



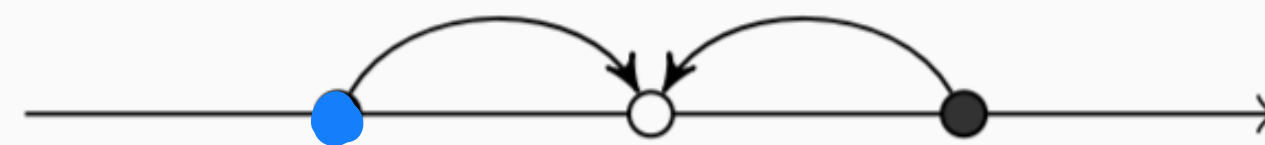
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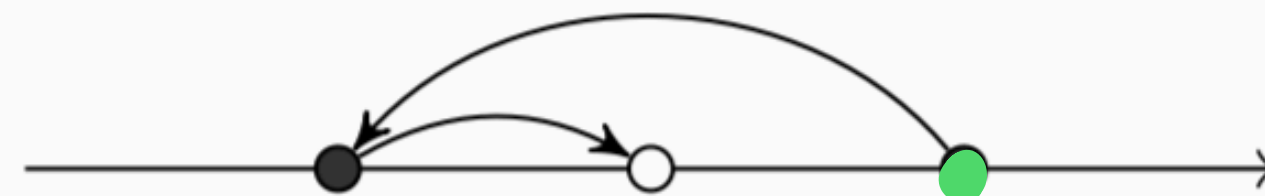
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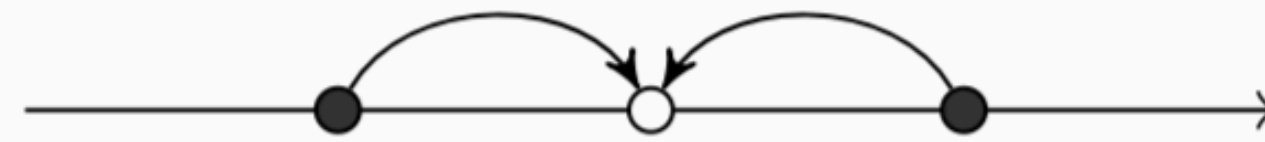
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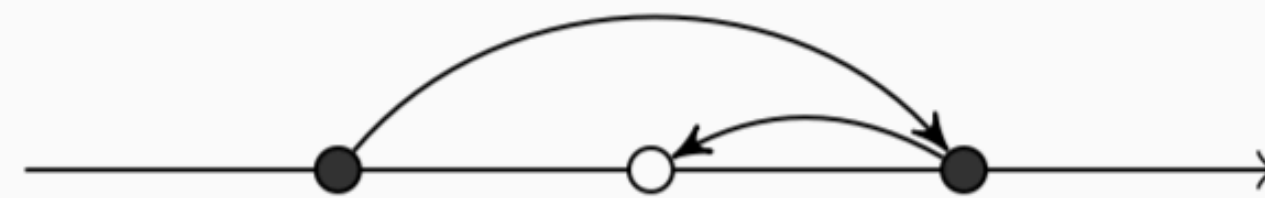
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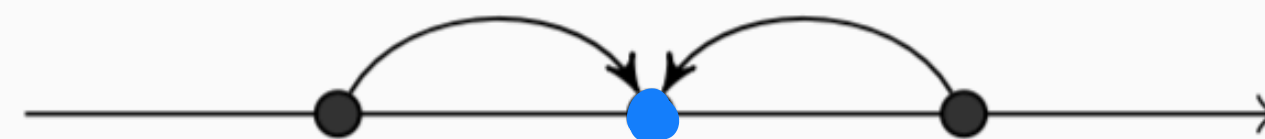
Solution with 2 robots

[SSS2020]

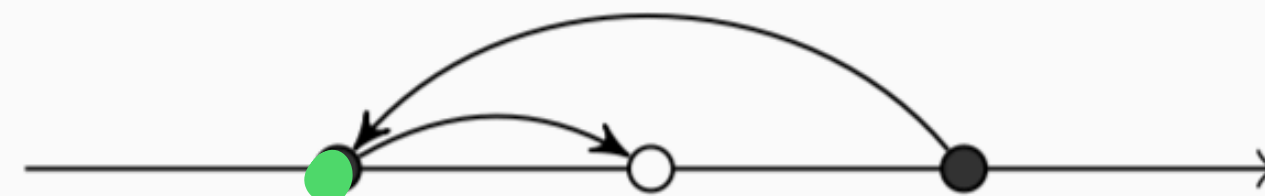
If d is the distance between the two robots (seen by robot r , executing the algorithm)

Let $i \in \mathbb{Z}$ such that $d \in [2^{-i}, 2^{1-i})$

case $i \equiv 0 \pmod{4}$



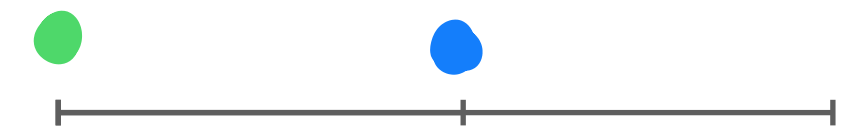
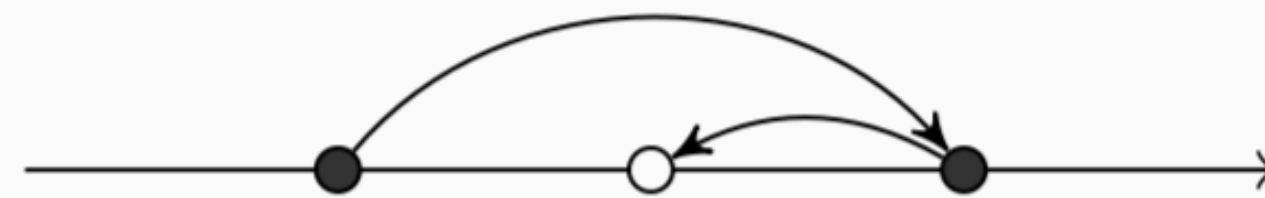
case $i \equiv 1 \pmod{4}$



case $i \equiv 2 \pmod{4}$



case $i \equiv 3 \pmod{4}$



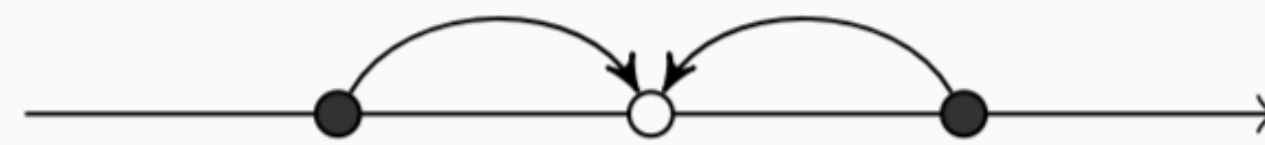
Solution with 2 robots

[SSS2020]

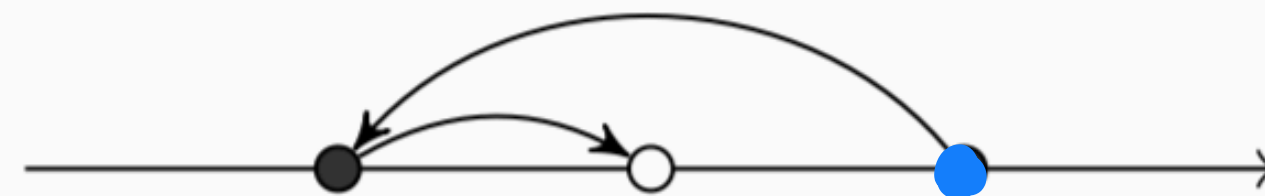
If d is the distance between the two robots (seen by robot r , executing the algorithm)

Let $i \in \mathbb{Z}$ such that $d \in [2^{-i}, 2^{1-i})$

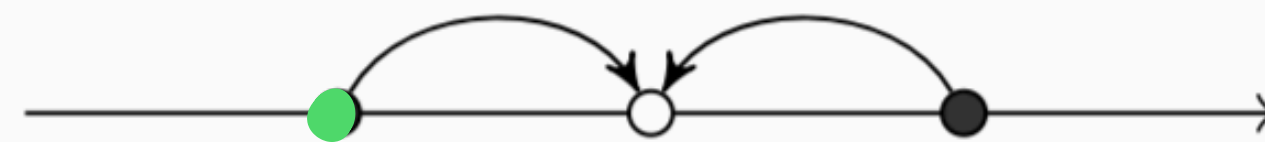
case $i \equiv 0 \pmod{4}$



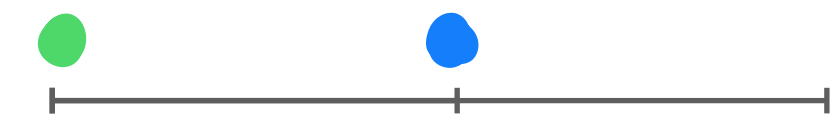
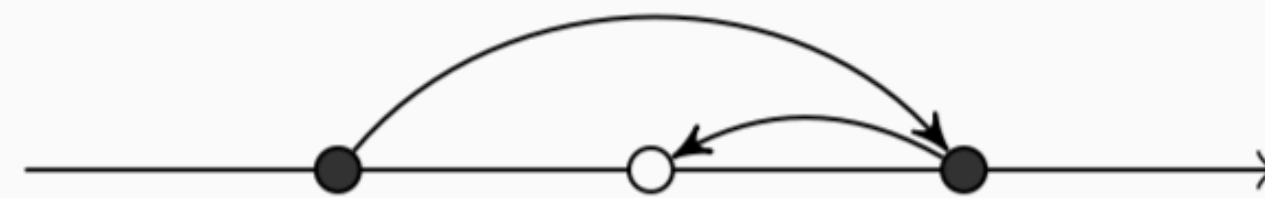
case $i \equiv 1 \pmod{4}$



case $i \equiv 2 \pmod{4}$



case $i \equiv 3 \pmod{4}$



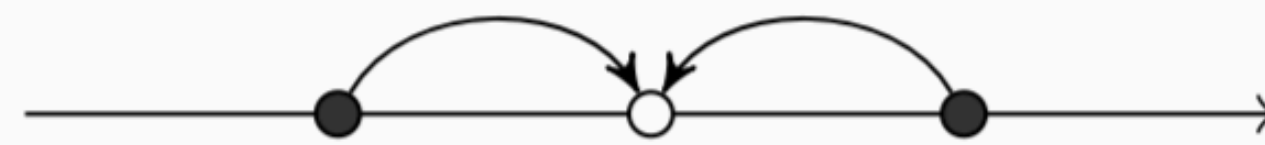
Solution with 2 robots

[SSS2020]

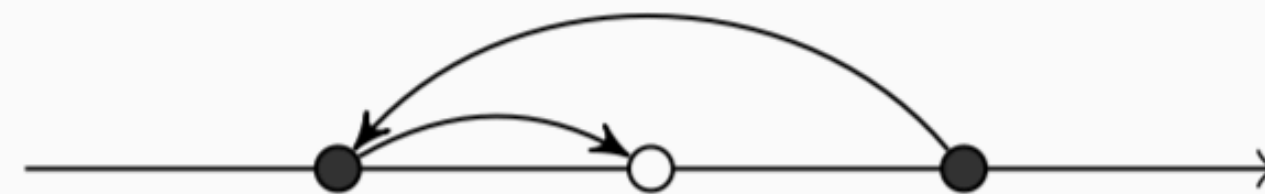
If d is the distance between the two robots (seen by robot r , executing the algorithm)

Let $i \in \mathbb{Z}$ such that $d \in [2^{-i}, 2^{1-i})$

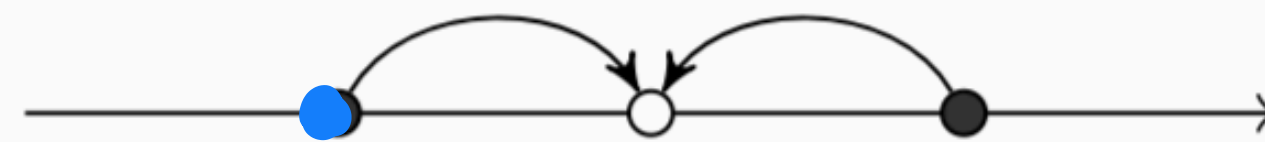
case $i \equiv 0 \pmod{4}$



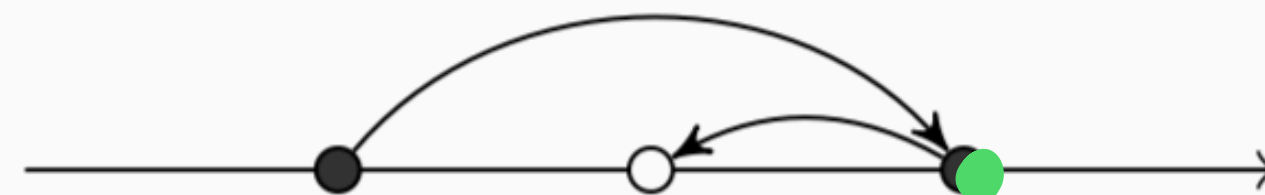
case $i \equiv 1 \pmod{4}$



case $i \equiv 2 \pmod{4}$



case $i \equiv 3 \pmod{4}$



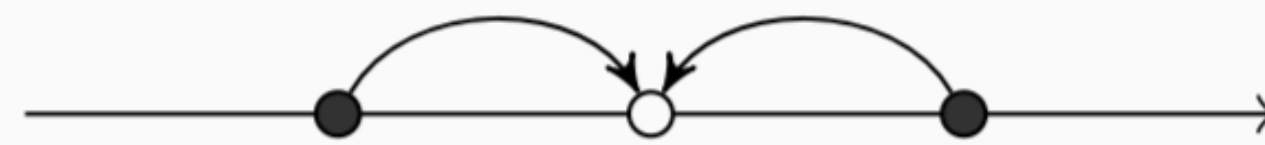
Solution with 2 robots

[SSS2020]

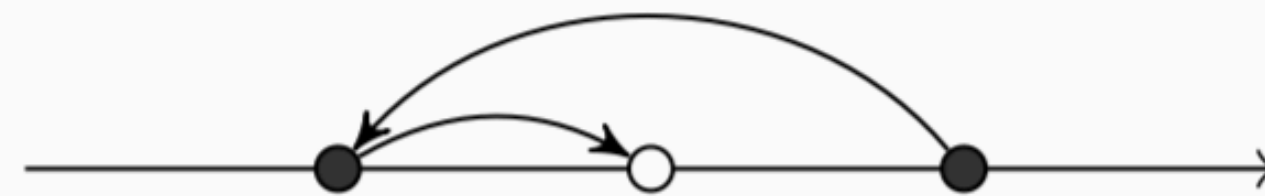
If d is the distance between the two robots (seen by robot r , executing the algorithm)

Let $i \in \mathbb{Z}$ such that $d \in [2^{-i}, 2^{1-i})$

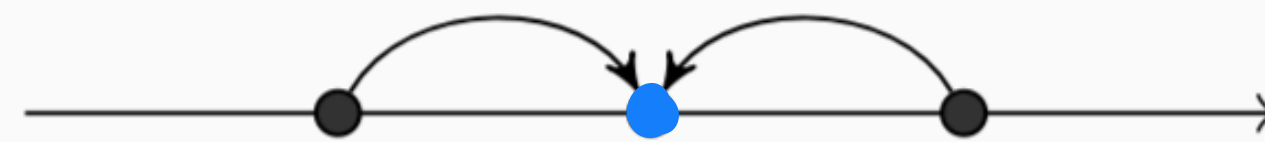
case $i \equiv 0 \pmod{4}$



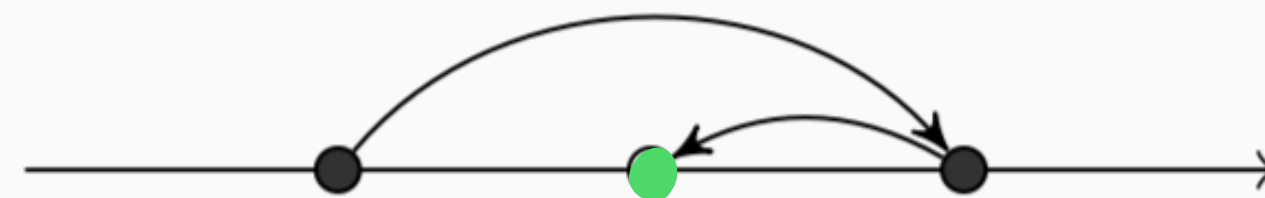
case $i \equiv 1 \pmod{4}$



case $i \equiv 2 \pmod{4}$



case $i \equiv 3 \pmod{4}$



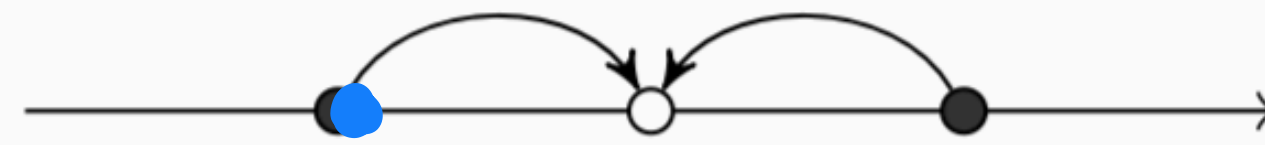
Solution with 2 robots

[SSS2020]

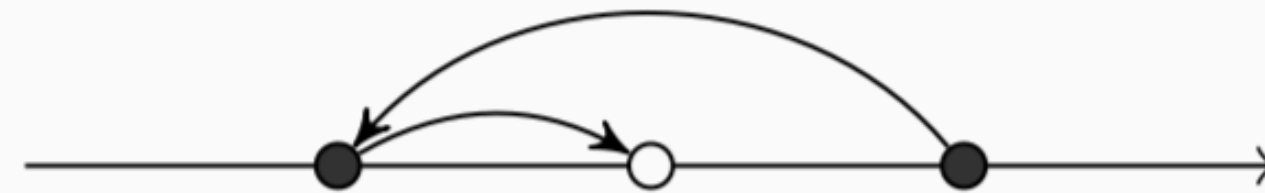
If d is the distance between the two robots (seen by robot r , executing the algorithm)

Let $i \in \mathbb{Z}$ such that $d \in [2^{-i}, 2^{1-i})$

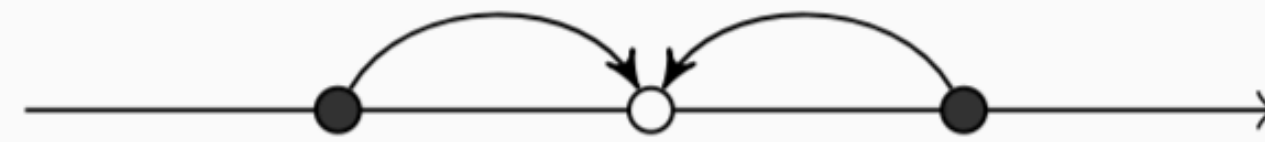
case $i \equiv 0 \pmod{4}$



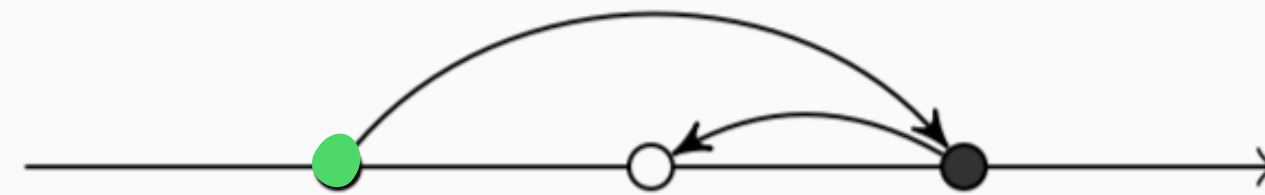
case $i \equiv 1 \pmod{4}$



case $i \equiv 2 \pmod{4}$



case $i \equiv 3 \pmod{4}$



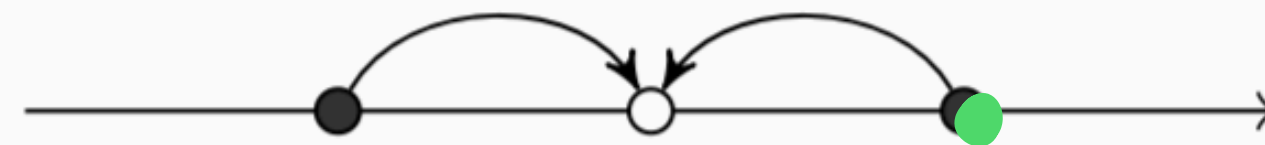
Solution with 2 robots

[SSS2020]

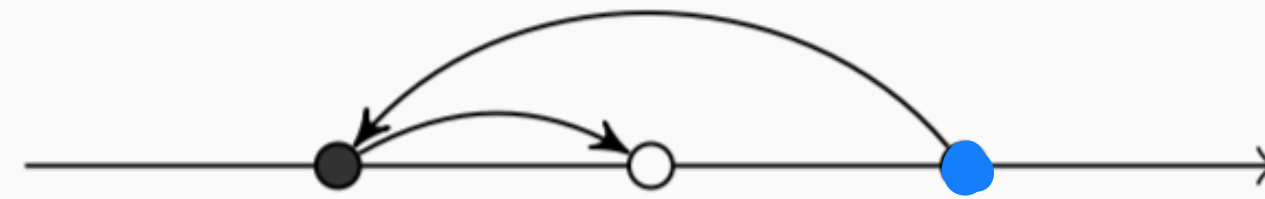
If d is the distance between the two robots (seen by robot r , executing the algorithm)

Let $i \in \mathbb{Z}$ such that $d \in [2^{-i}, 2^{1-i})$

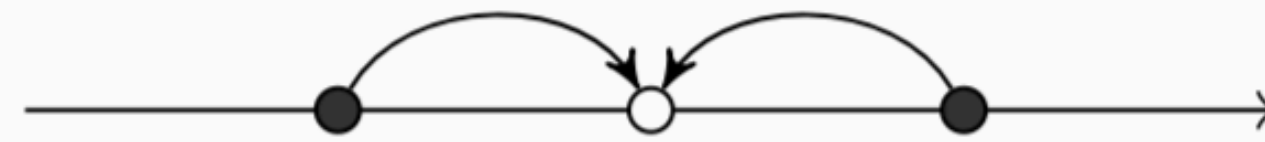
case $i \equiv 0 \pmod{4}$



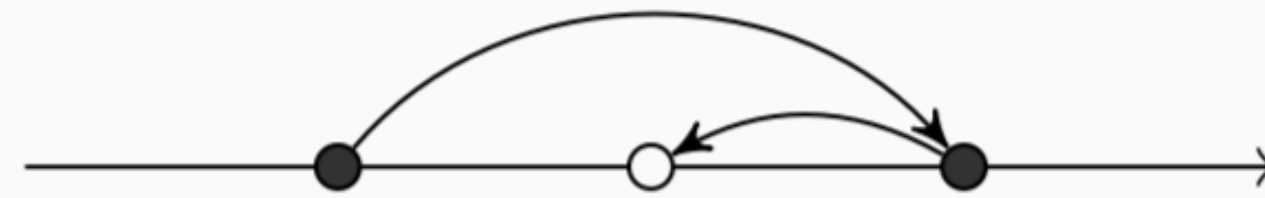
case $i \equiv 1 \pmod{4}$



case $i \equiv 2 \pmod{4}$



case $i \equiv 3 \pmod{4}$



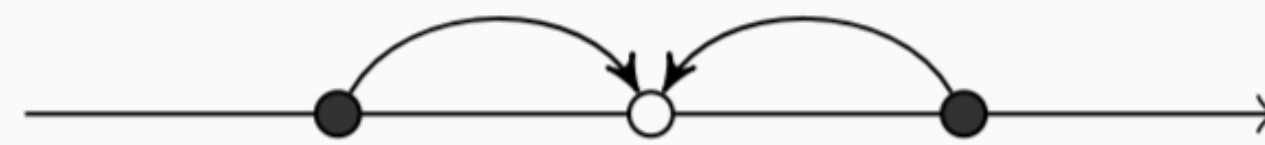
Solution with 2 robots

[SSS2020]

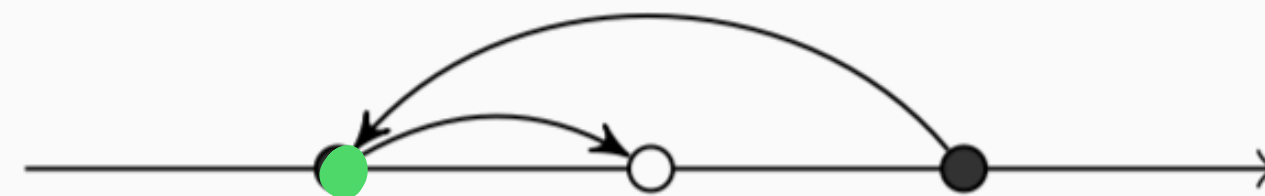
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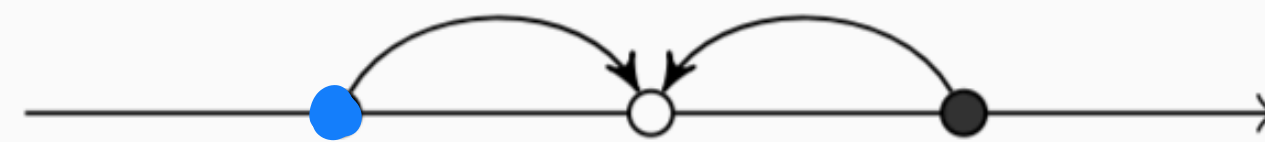
case $i \equiv 0 \pmod{4}$



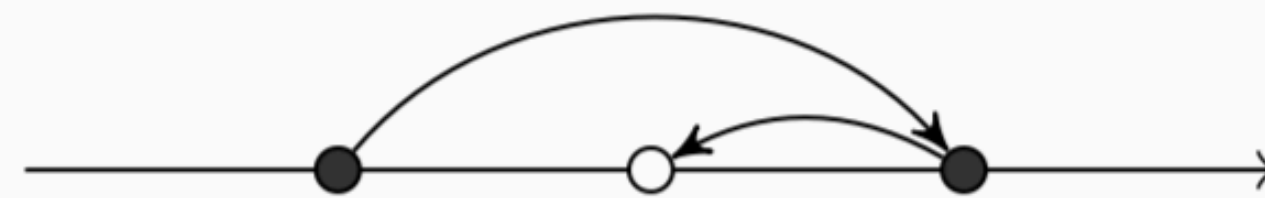
case $i \equiv 1 \pmod{4}$



case $i \equiv 2 \pmod{4}$



case $i \equiv 3 \pmod{4}$



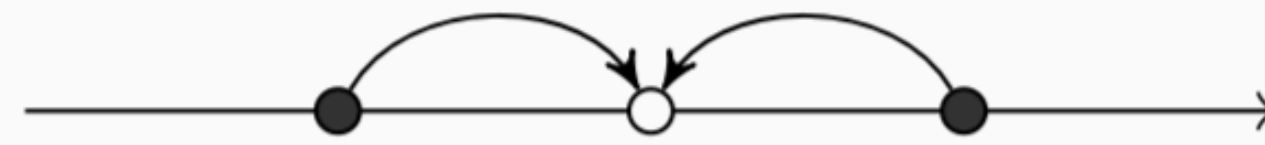
Solution with 2 robots

[SSS2020]

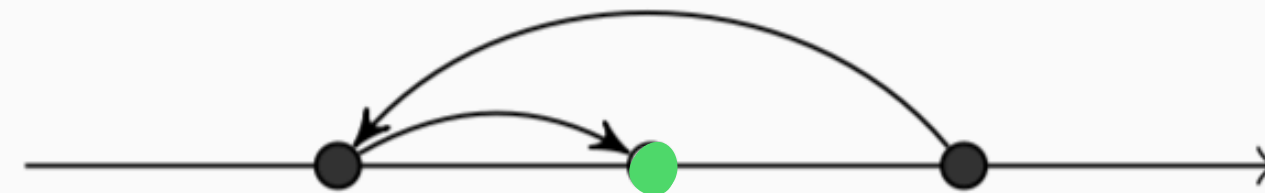
If d is the distance between the two robots (seen by robot r , executing the algorithm)

Let $i \in \mathbb{Z}$ such that $d \in [2^{-i}, 2^{1-i})$

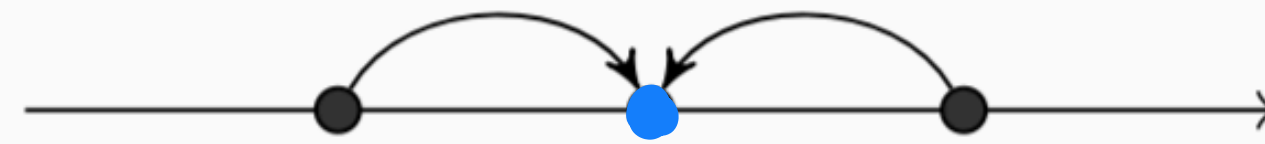
case $i \equiv 0 \pmod{4}$



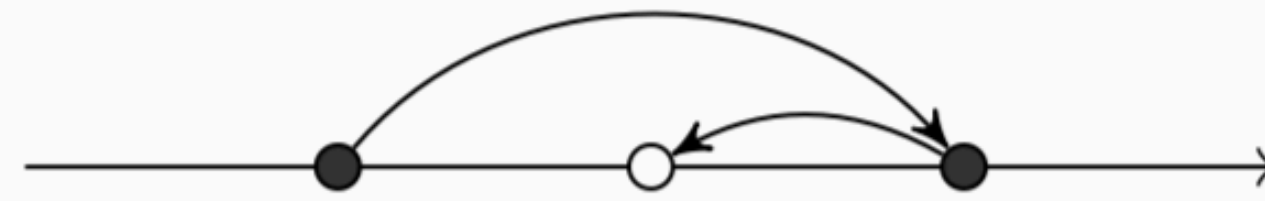
case $i \equiv 1 \pmod{4}$



case $i \equiv 2 \pmod{4}$



case $i \equiv 3 \pmod{4}$



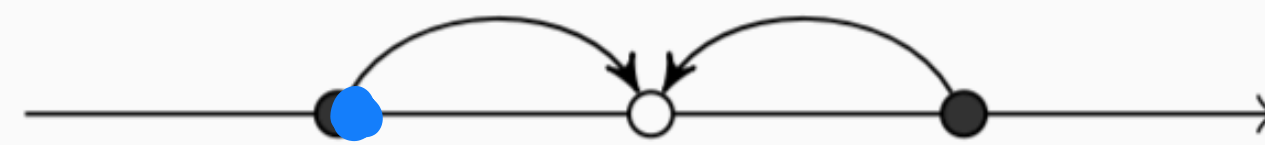
Solution with 2 robots

[SSS2020]

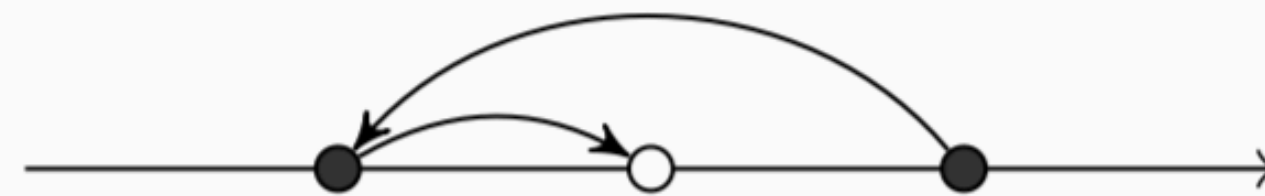
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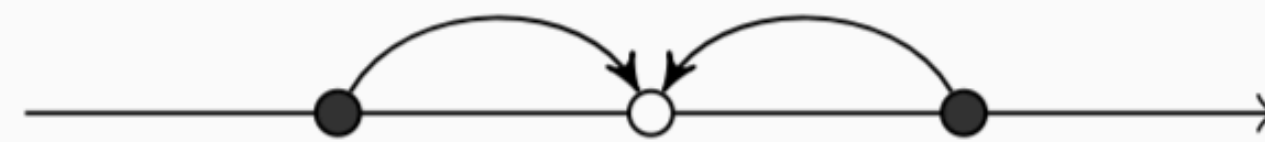
case $i \equiv 0 \pmod{4}$



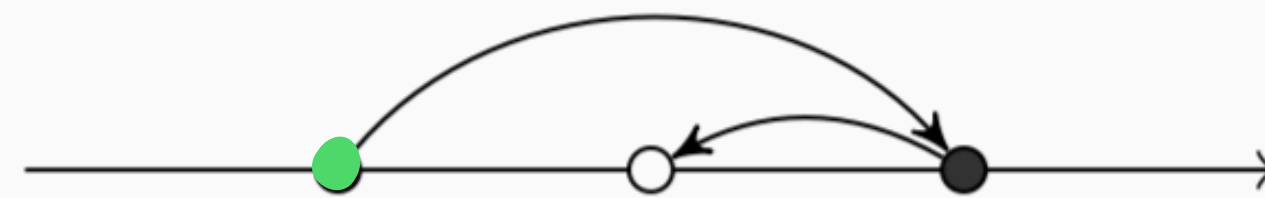
case $i \equiv 1 \pmod{4}$



case $i \equiv 2 \pmod{4}$



case $i \equiv 3 \pmod{4}$



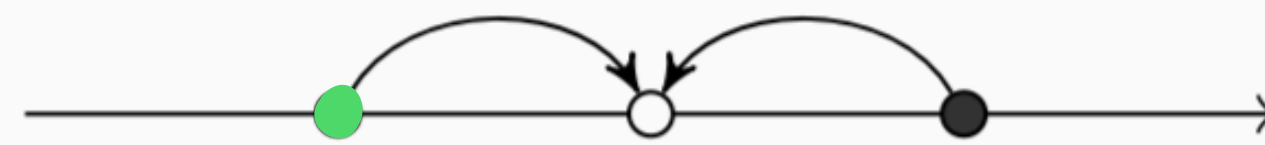
Solution with 2 robots

[SSS2020]

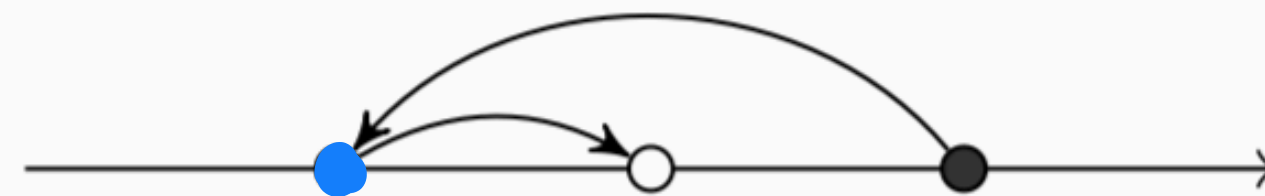
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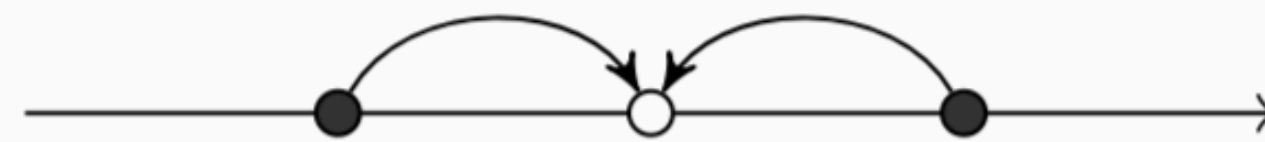
case $i \equiv 0 \pmod{4}$



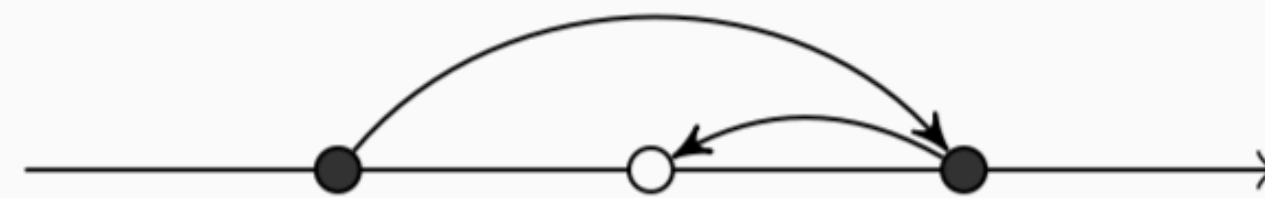
case $i \equiv 1 \pmod{4}$



case $i \equiv 2 \pmod{4}$



case $i \equiv 3 \pmod{4}$



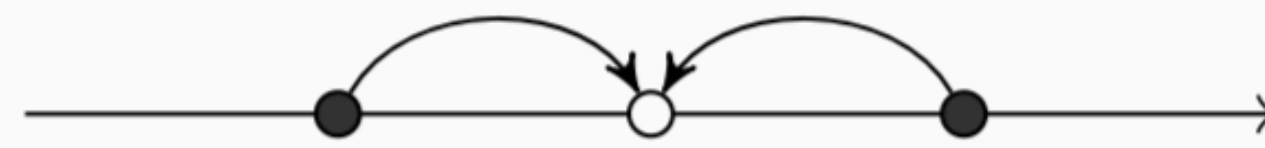
Solution with 2 robots

[SSS2020]

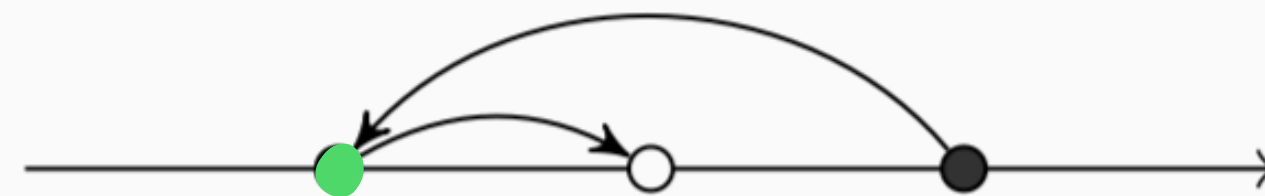
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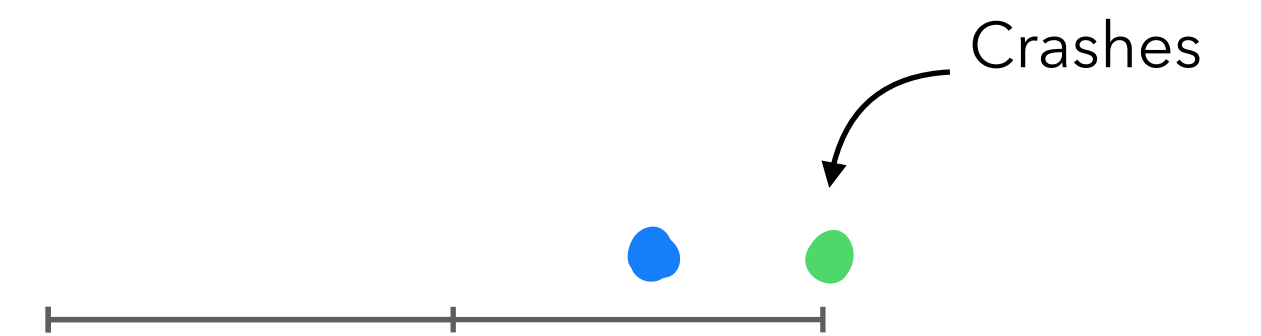
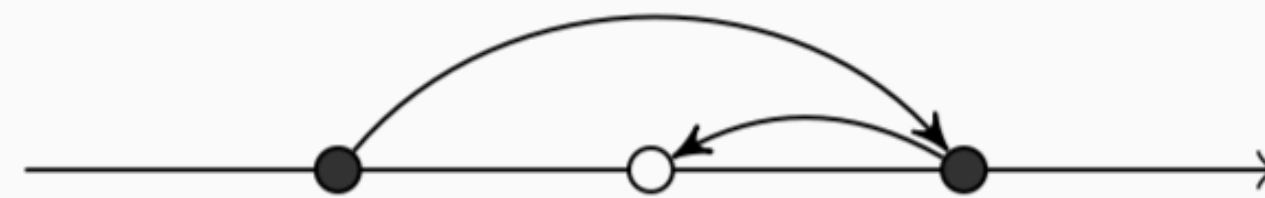
case $i \equiv 1 \pmod{4}$



case $i \equiv 2 \pmod{4}$



case $i \equiv 3 \pmod{4}$



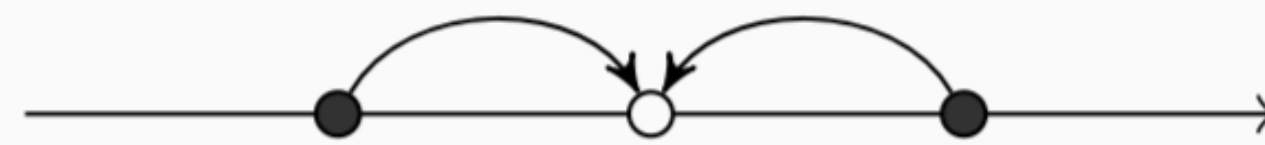
Solution with 2 robots

[SSS2020]

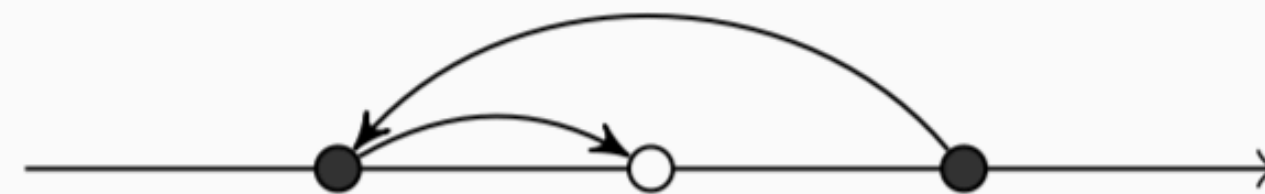
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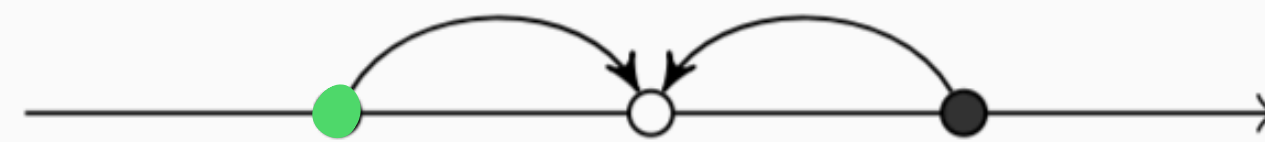
case $i \equiv 0 \pmod{4}$



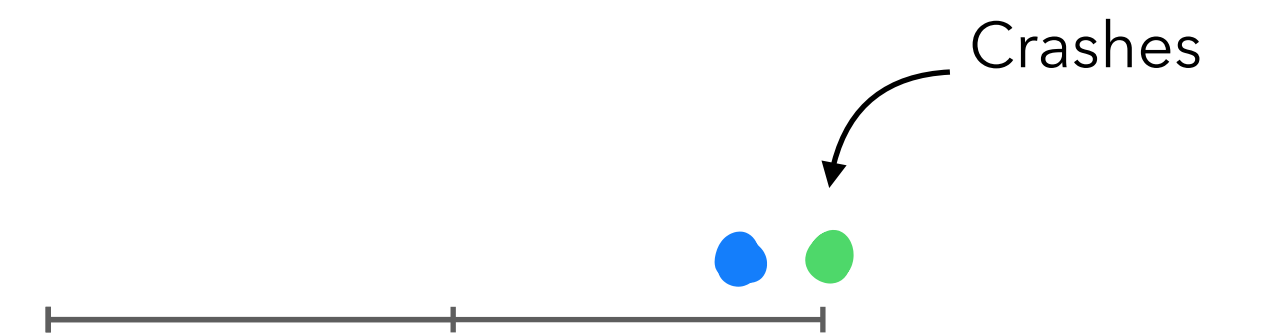
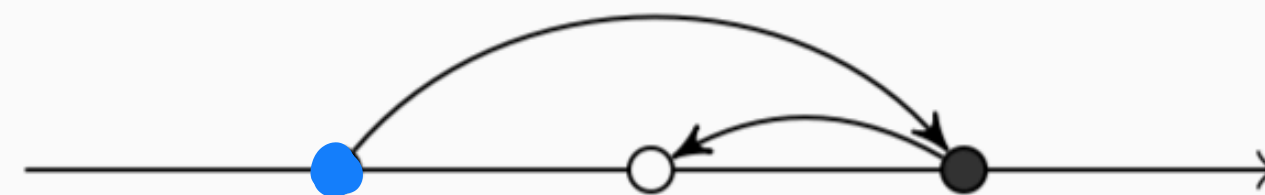
case $i \equiv 1 \pmod{4}$



case $i \equiv 2 \pmod{4}$



case $i \equiv 3 \pmod{4}$



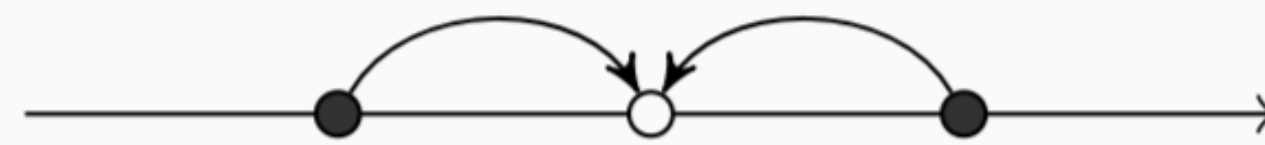
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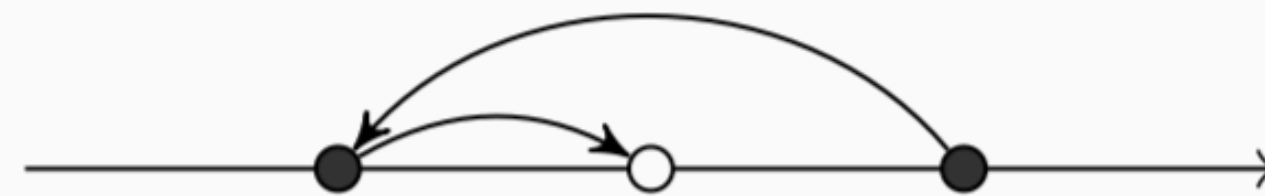
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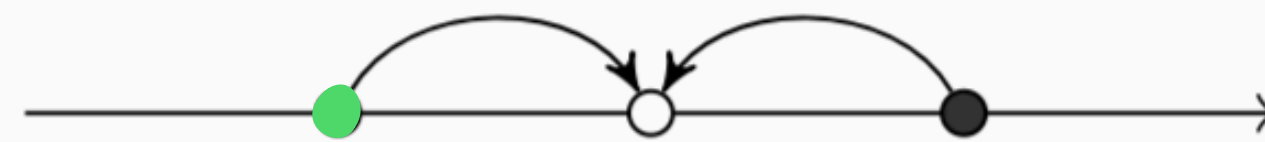
case $i \equiv 0 \pmod{4}$



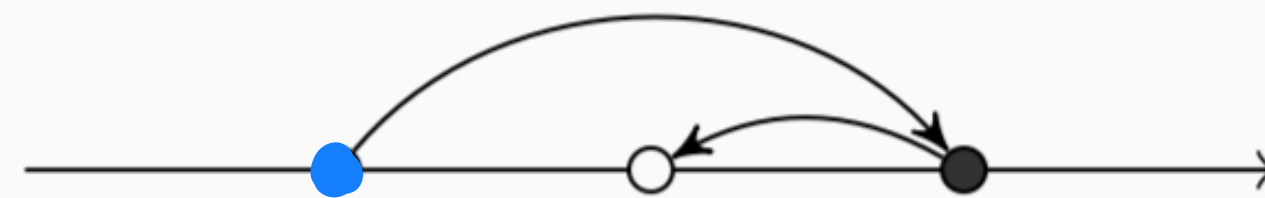
case $i \equiv 1 \pmod{4}$



case $i \equiv 2 \pmod{4}$



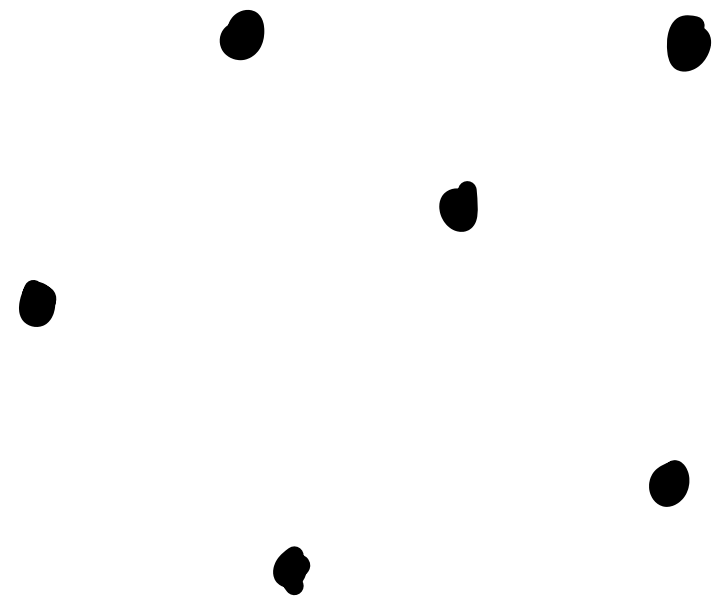
case $i \equiv 3 \pmod{4}$



Solution with $n > 2$ robots

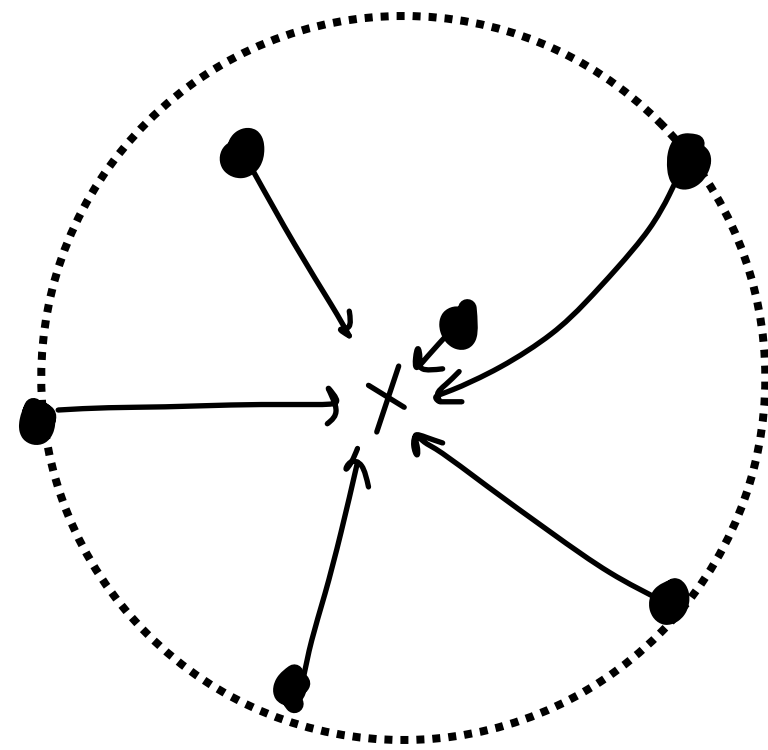
How to start

$$n > 2$$



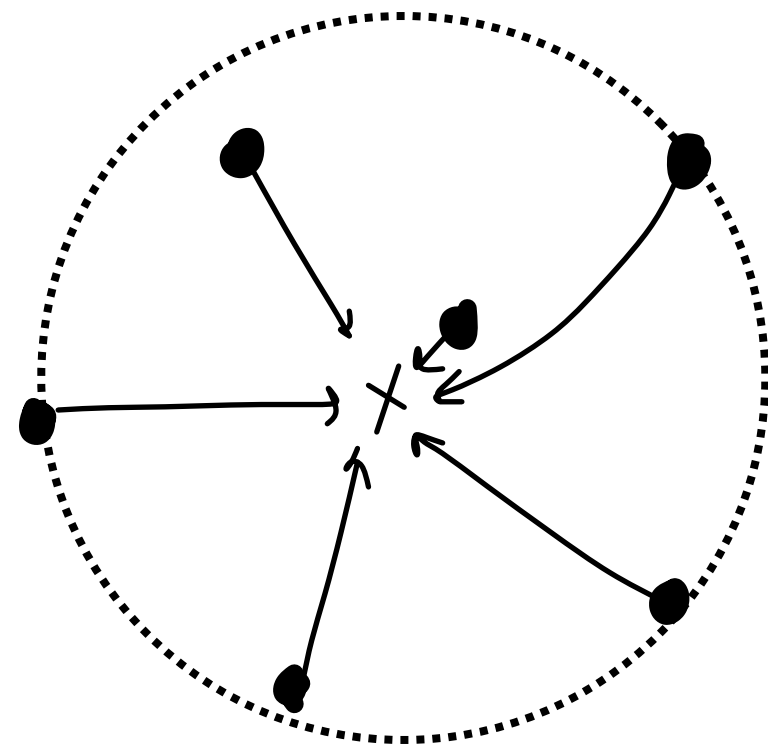
How to start

$n > 2$



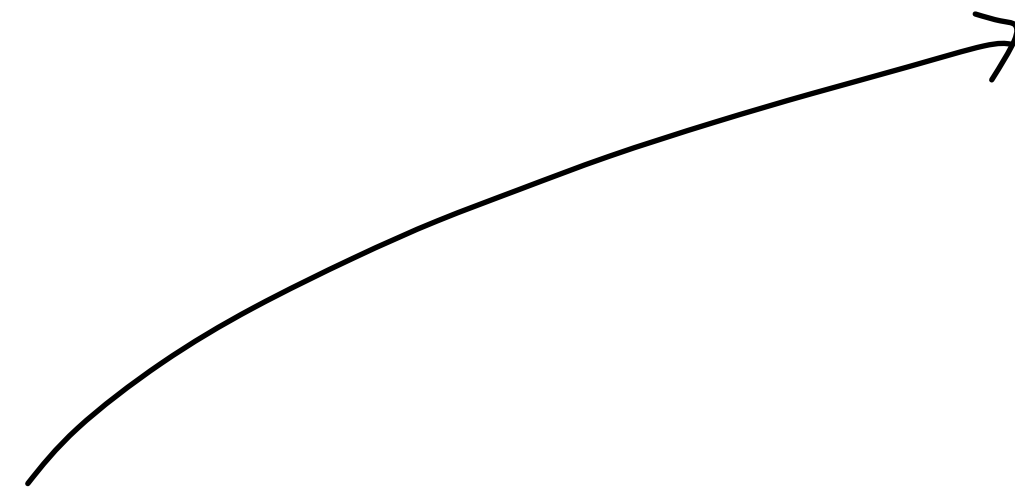
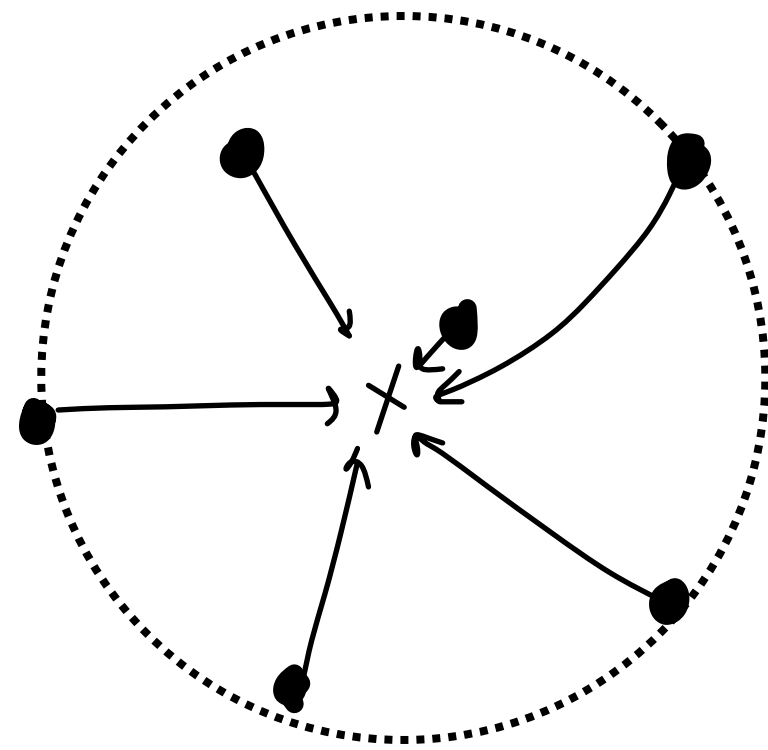
How to start

$n > 2$



How to start

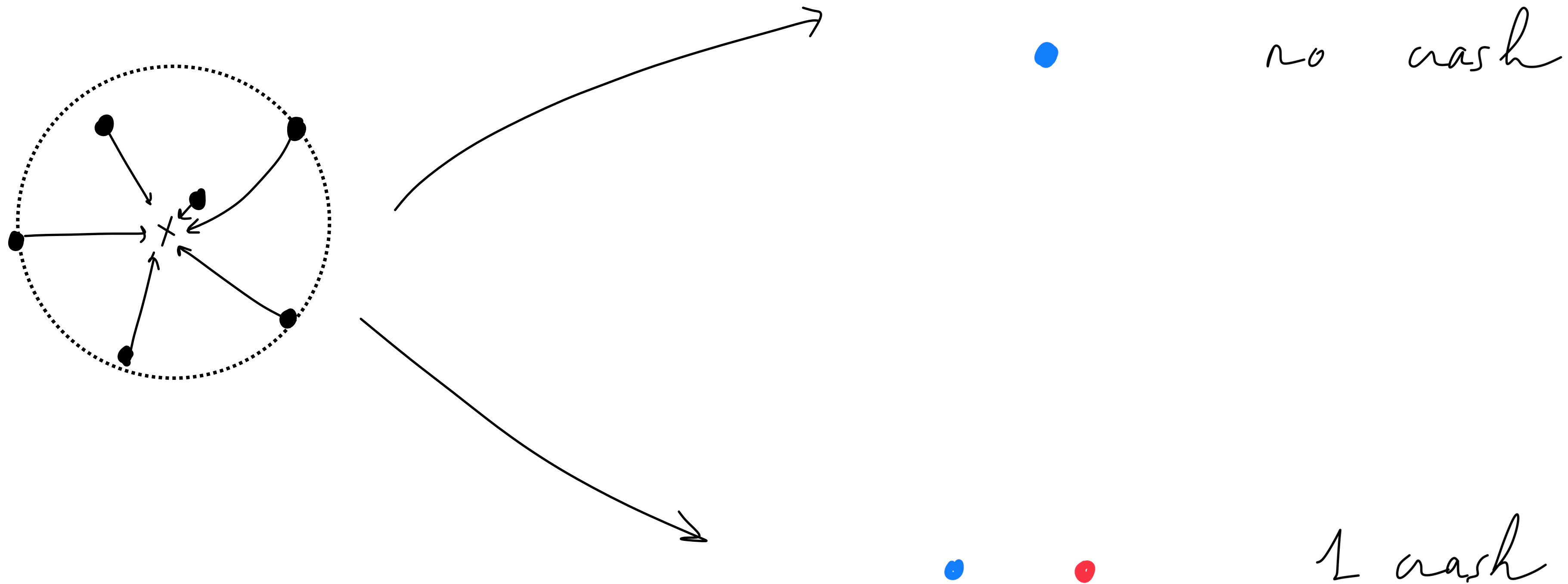
$n > 2$



no crash

How to start

$n > 2$



What we would like to do

- If all the robots are correct we want all of them to execute move to middle

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$i = 1$



What we would like to do

- If all the robots are correct we want all of them to execute move to middle

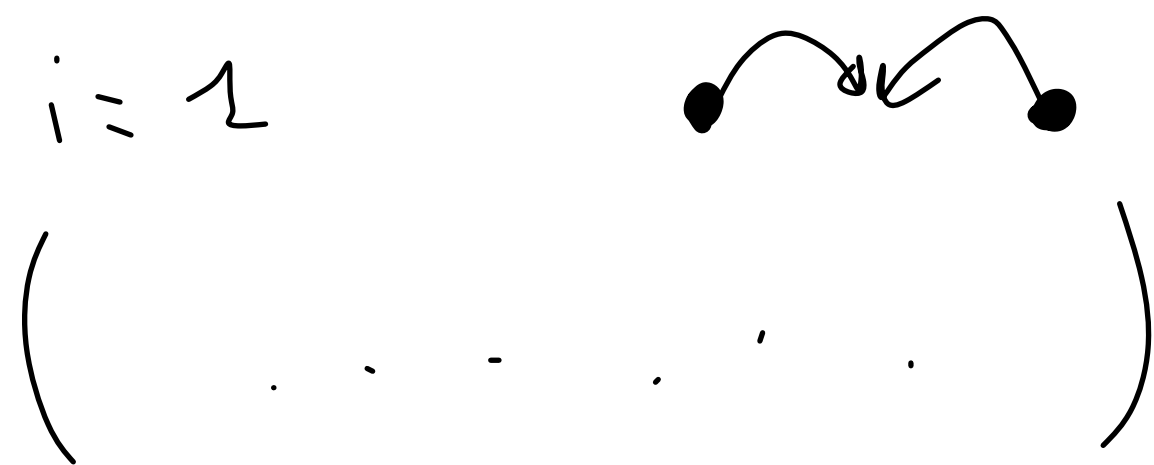
$i = 1$



← works if all robots have the same level

What we would like to do

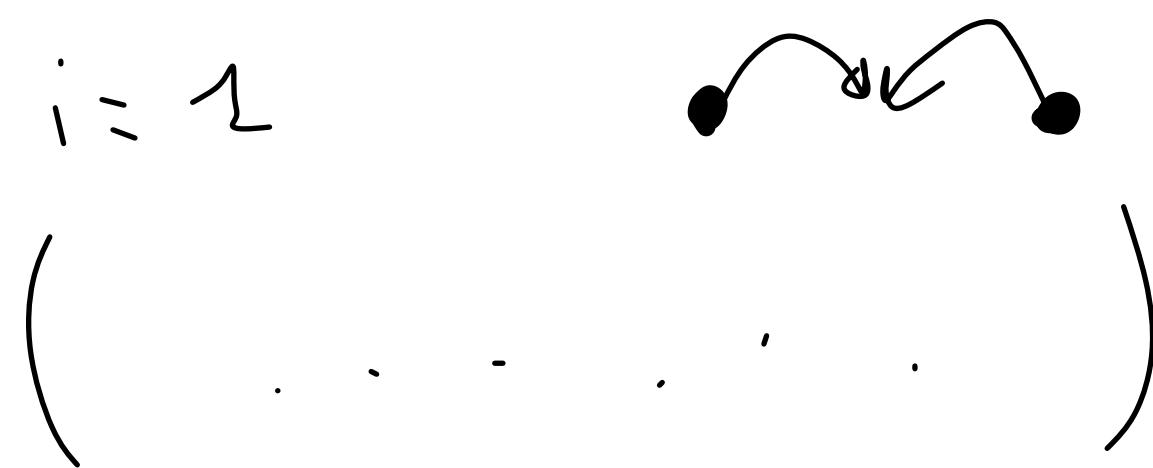
- If all the robots are correct we want all of them to execute move to middle



← works if all robots have the same level

What we would like to do

- If all the robots are correct we want all of them to execute move to middle



← works if all robots have the same level



What we would like to do

- If all the robots are correct we want all of them to execute move to middle



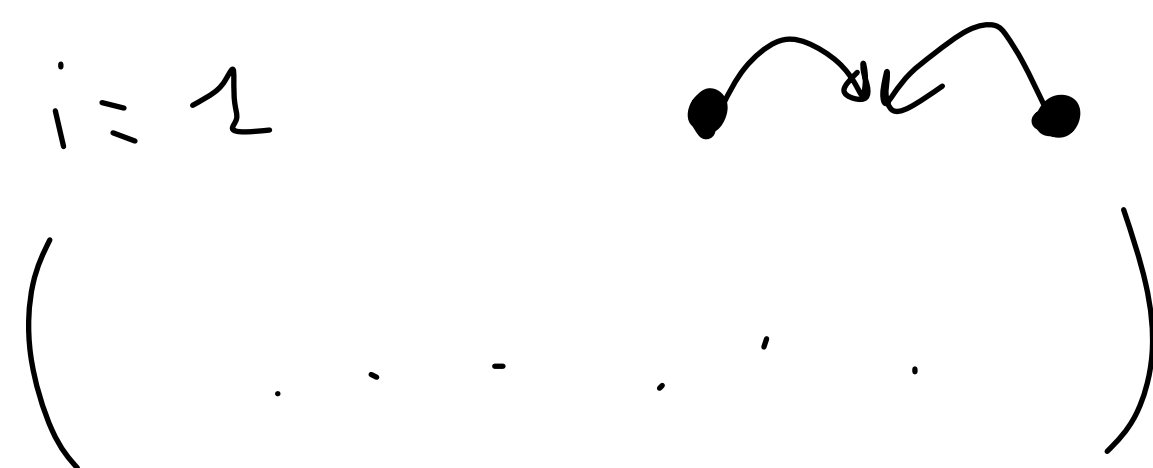
← works if all robots have the same level



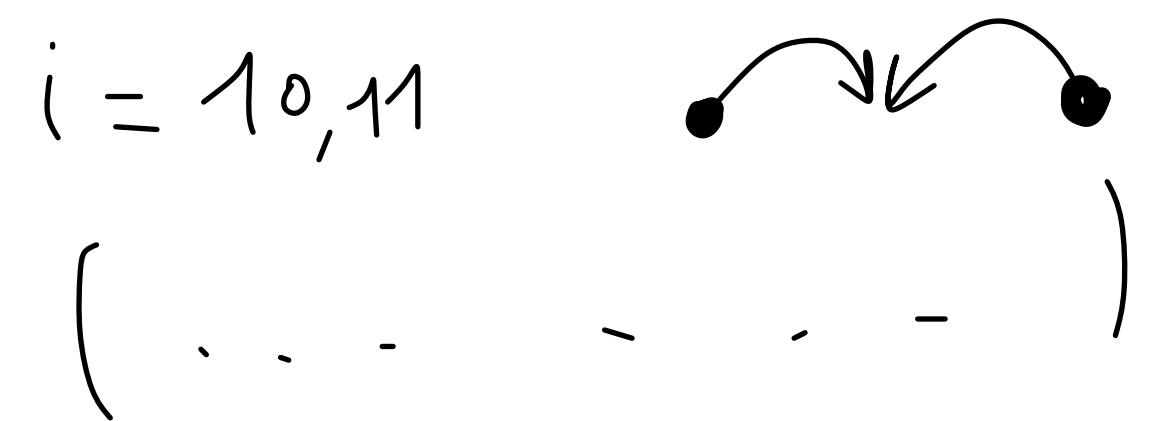
← works if $\Delta_{\text{level}} \leq 2$

What we would like to do

- If all the robots are correct we want all of them to execute move to middle



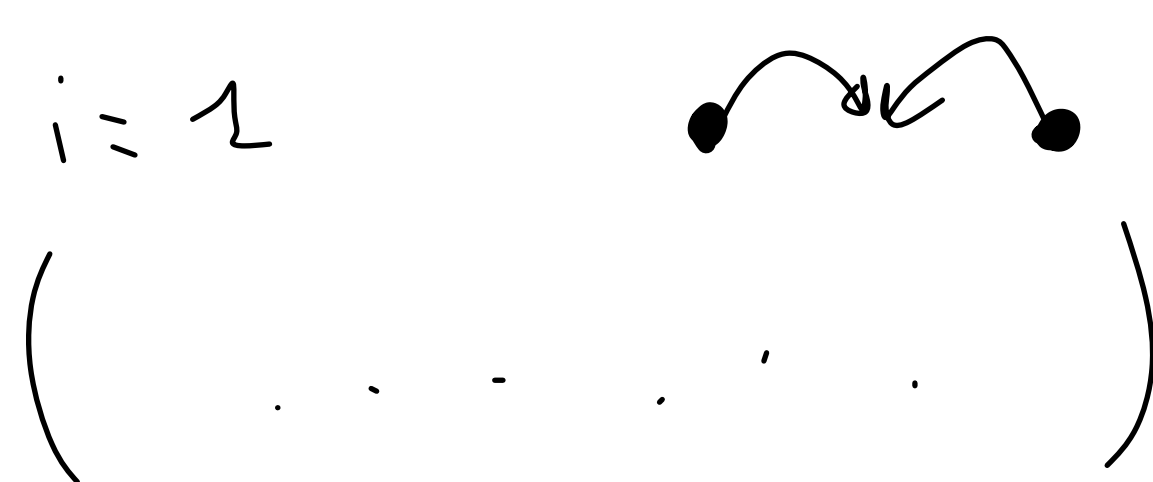
← works if all robots have the same level



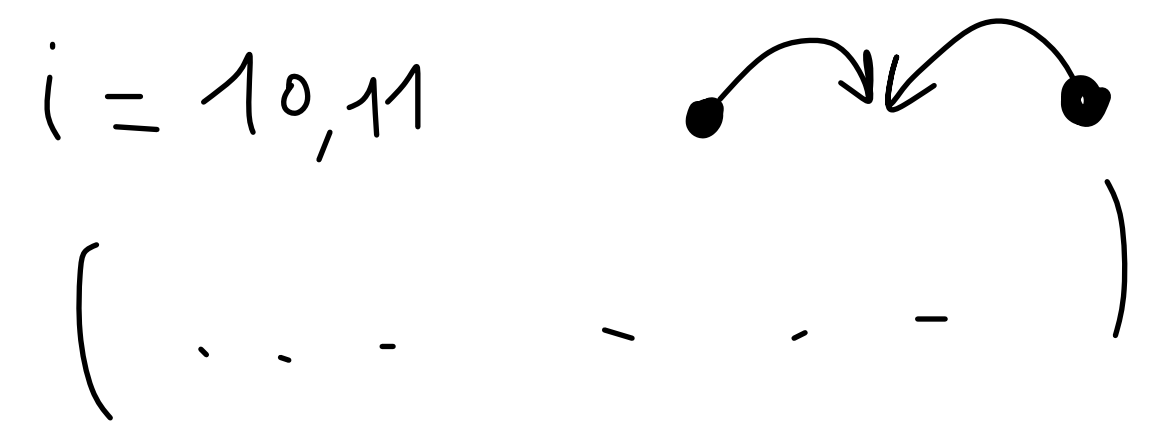
← works if $\Delta_{level} \leq 2$

What we would like to do

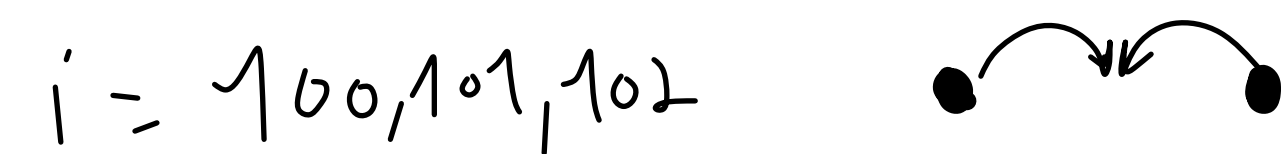
- If all the robots are correct we want all of them to execute move to middle



← works if all robots have the same level

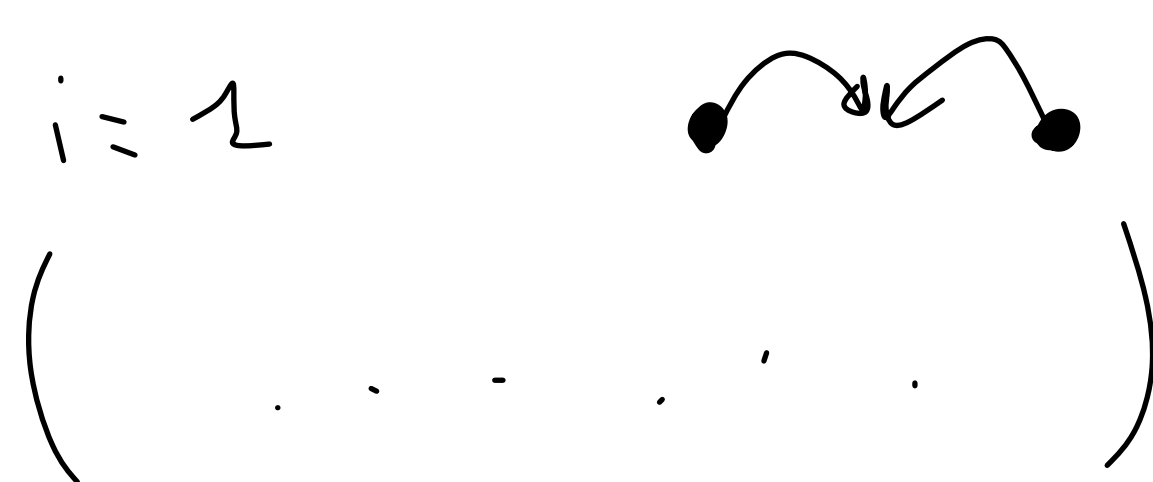


← works if $\Delta_{level} \leq 2$

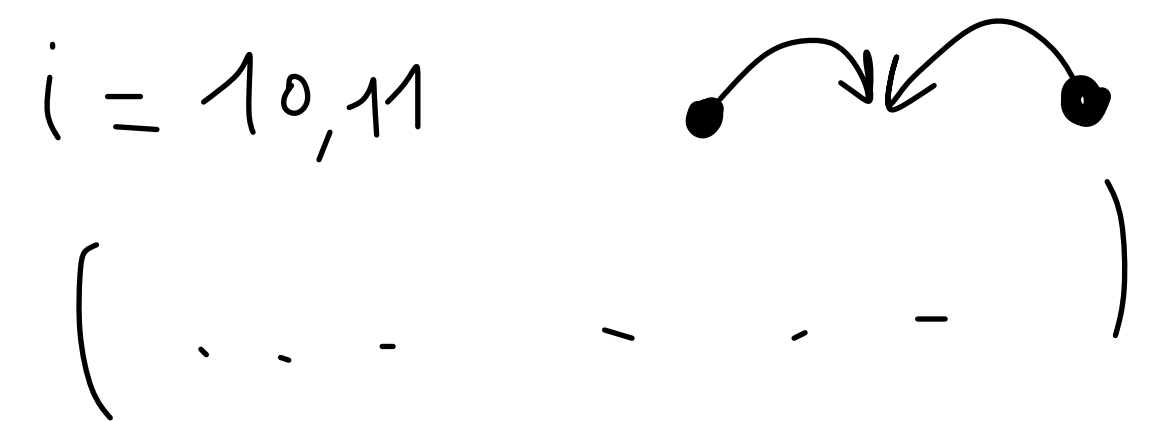


What we would like to do

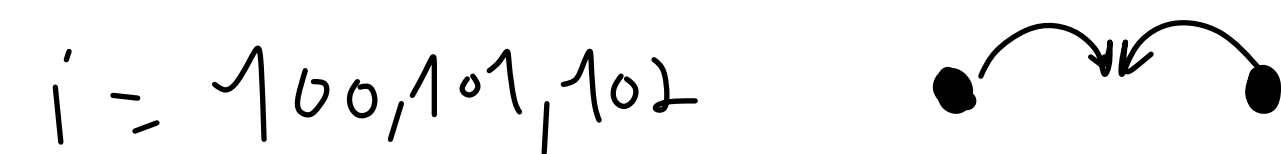
- If all the robots are correct we want all of them to execute move to middle



← works if all robots have the same level



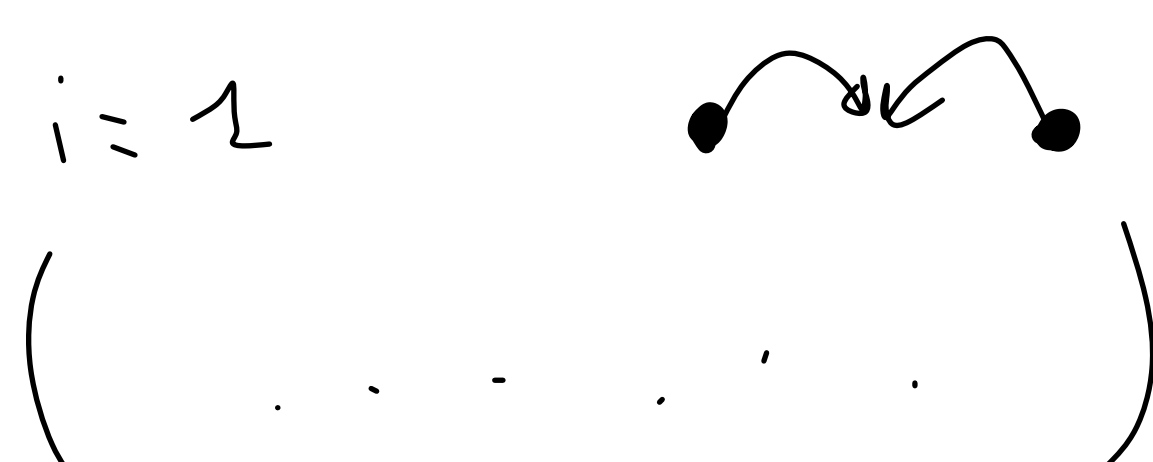
← works if $\Delta_{\text{level}} \leq 2$



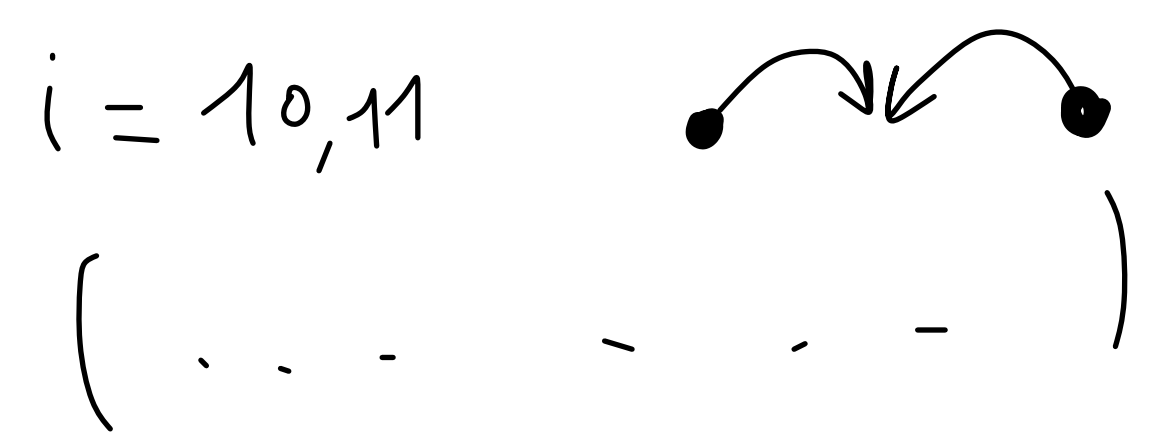
$\Delta_{\text{level}} \leq 3$

What we would like to do

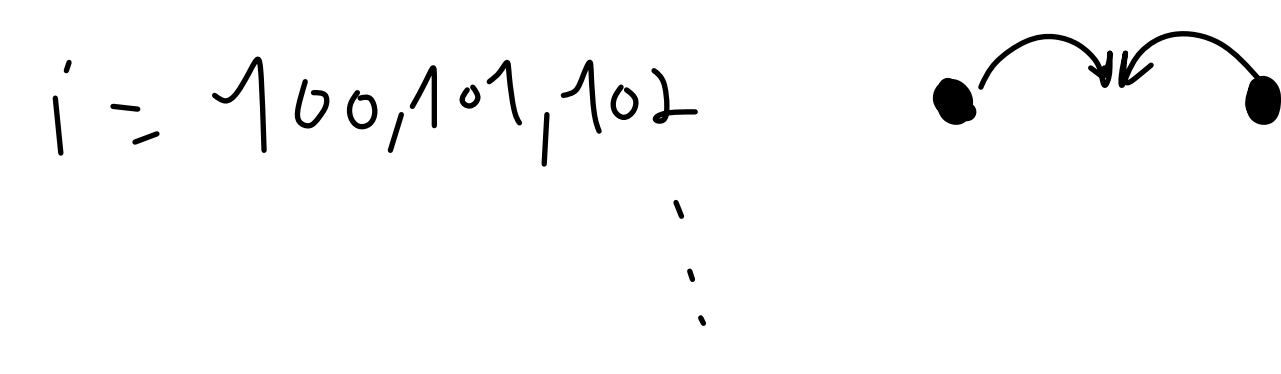
- If all the robots are correct we want all of them to execute move to middle



← works if all robots have the same level



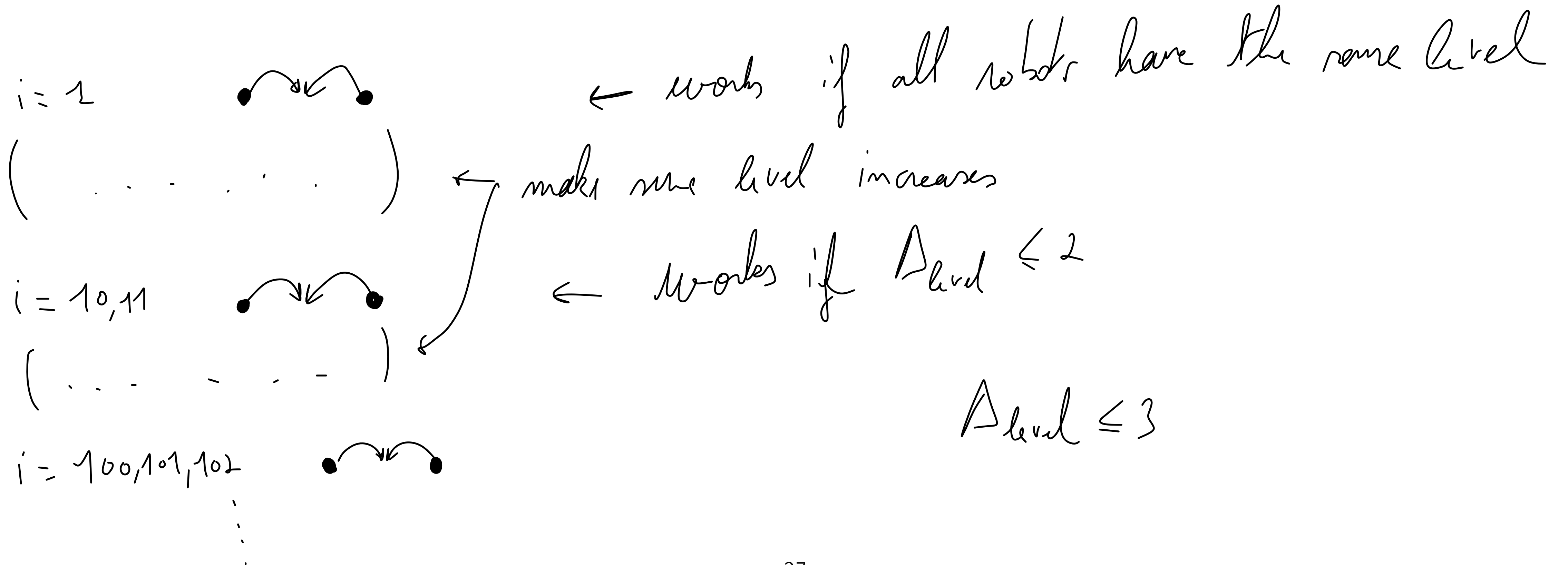
← works if $\Delta_{level} \leq 2$



$\Delta_{level} \leq 3$

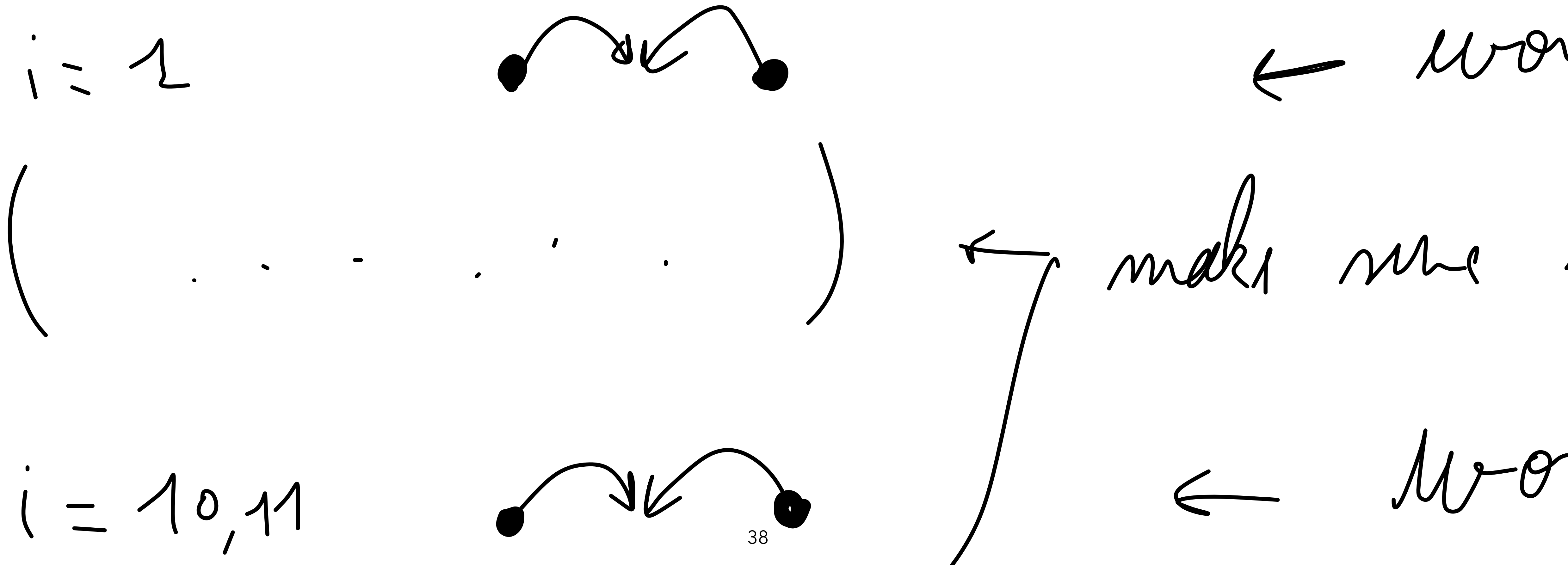
What we would like to do

- If all the robots are correct we want all of them to execute move to middle



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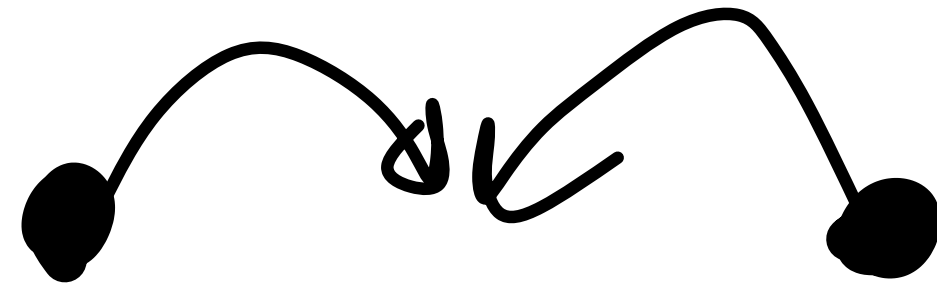
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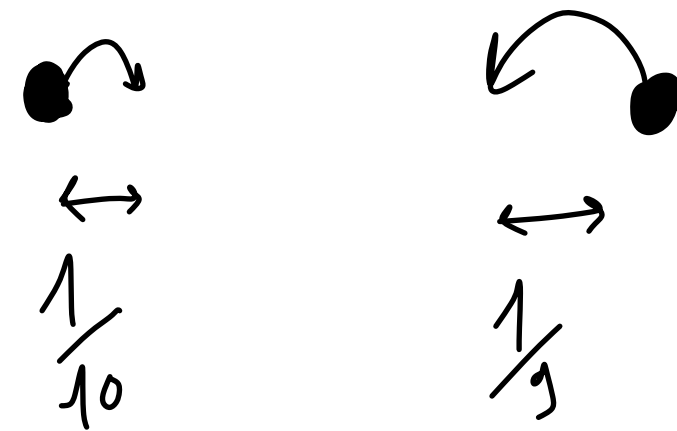
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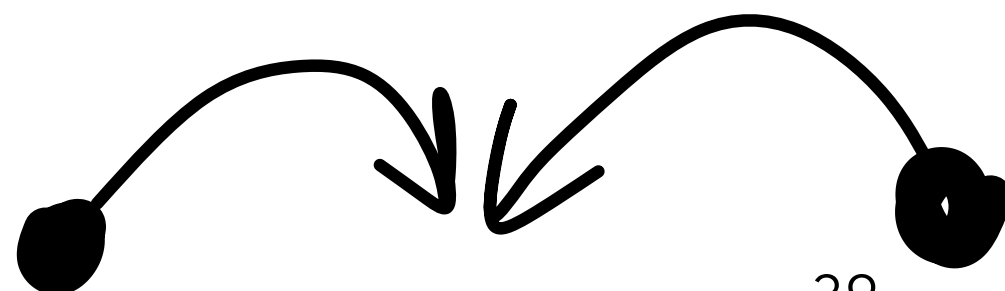
$i = 1$



$i = 2$



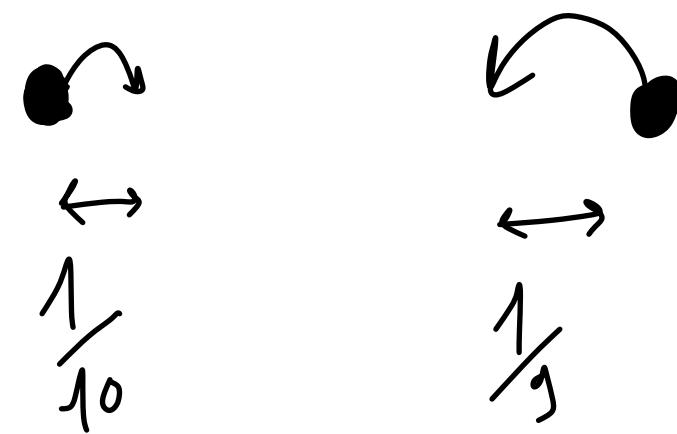
$i = 10, 11$



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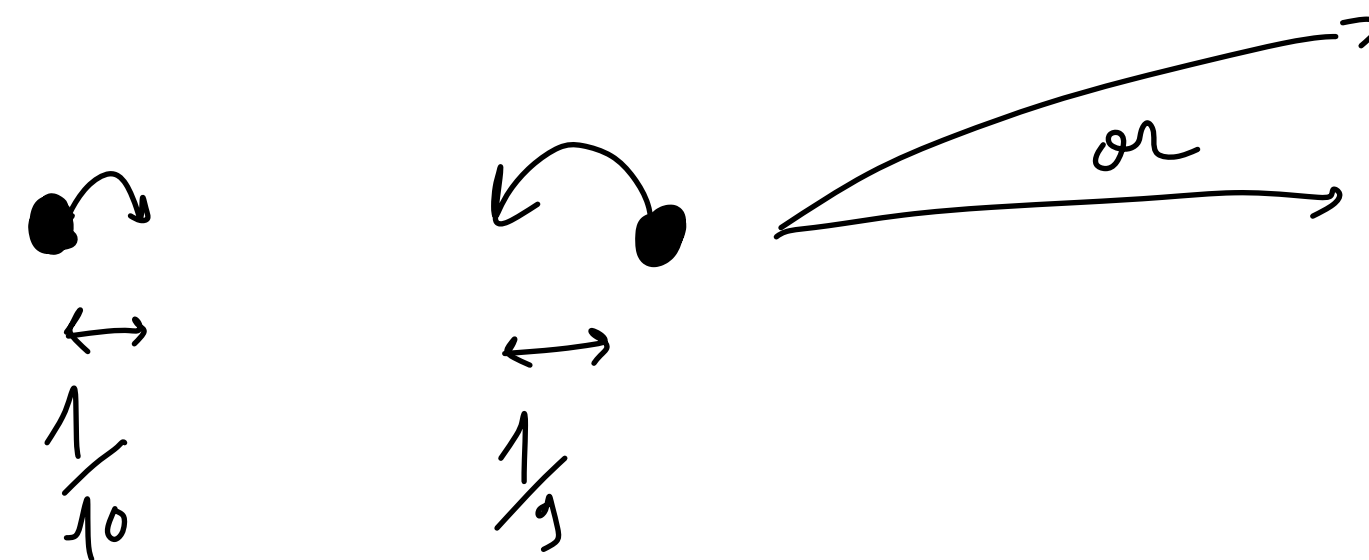
$i = 2$



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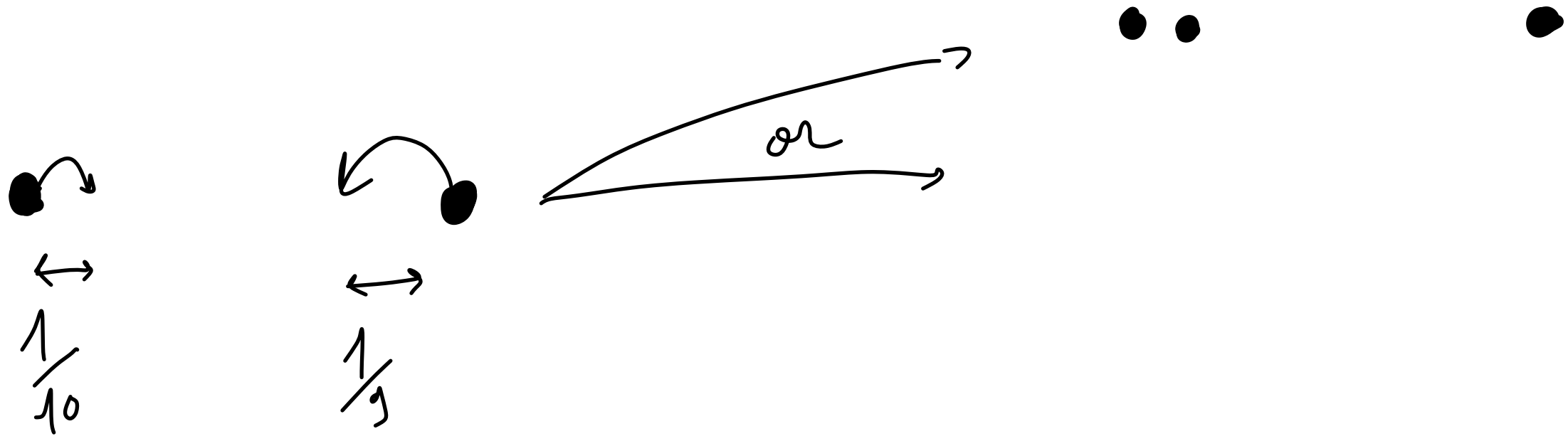
$i = 2$



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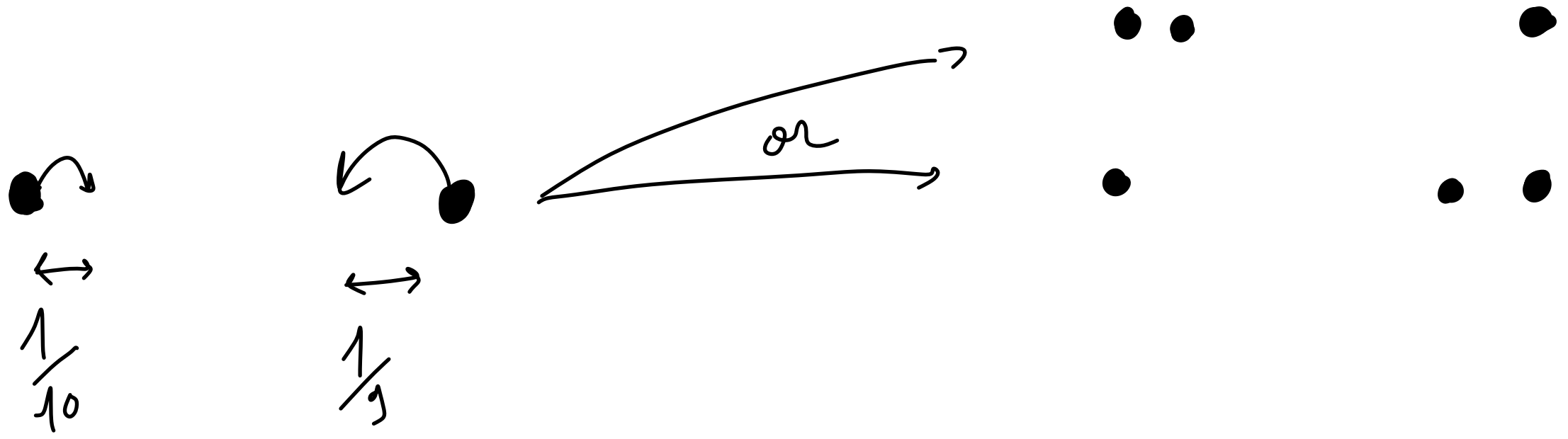
$i = 2$



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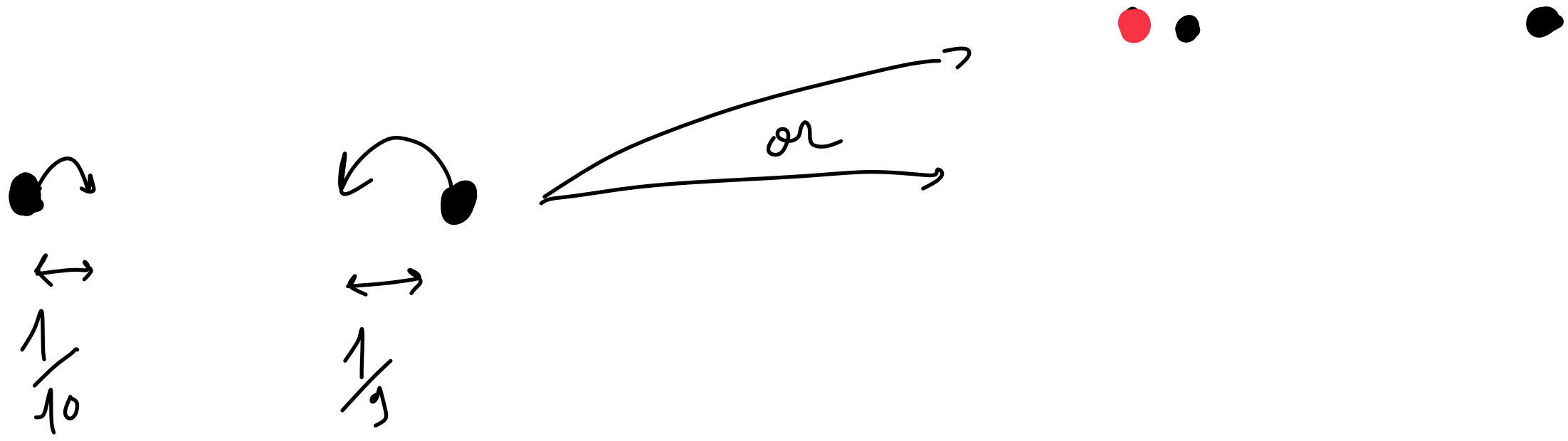
$i = 2$



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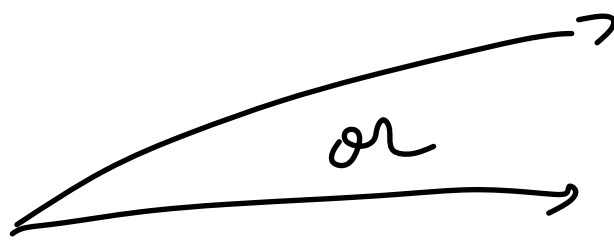
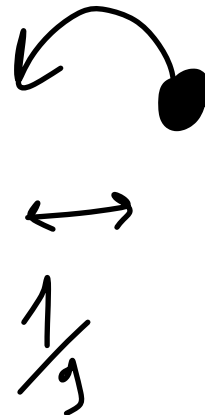
$i = 2$



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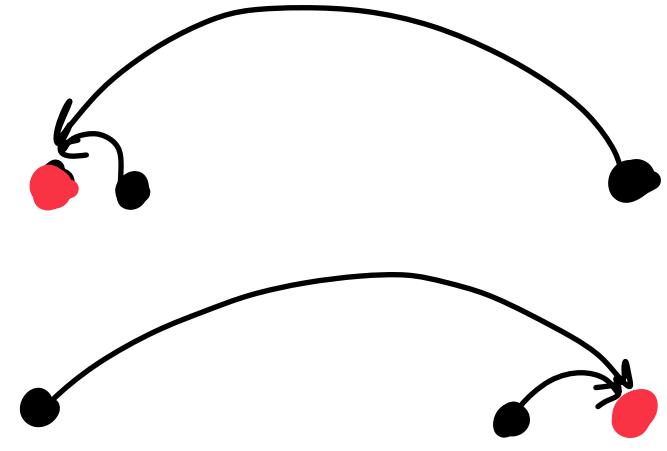
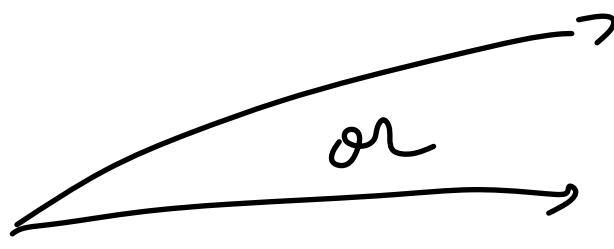
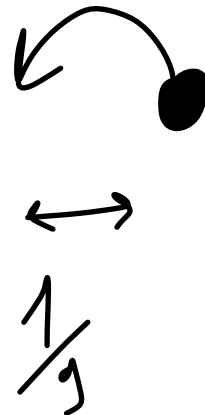
$i = 2$



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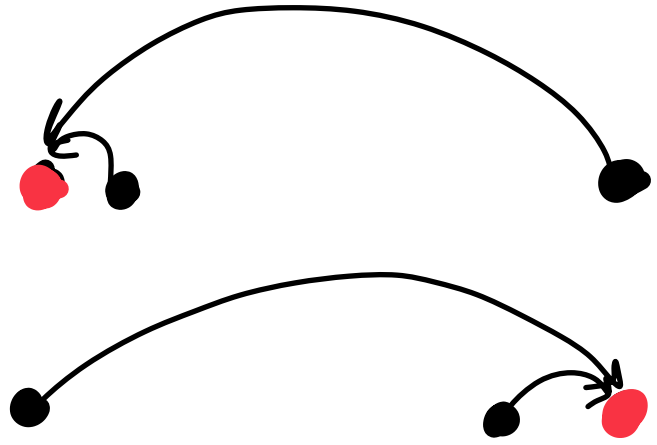
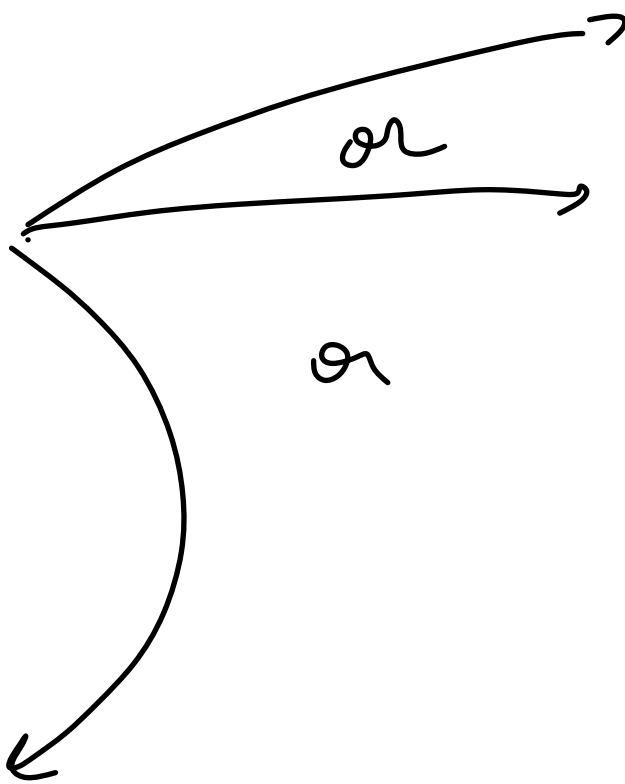
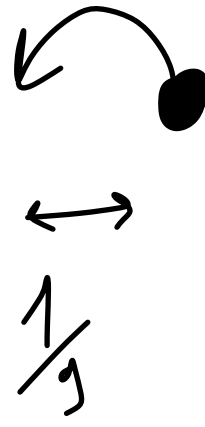
$i = 2$



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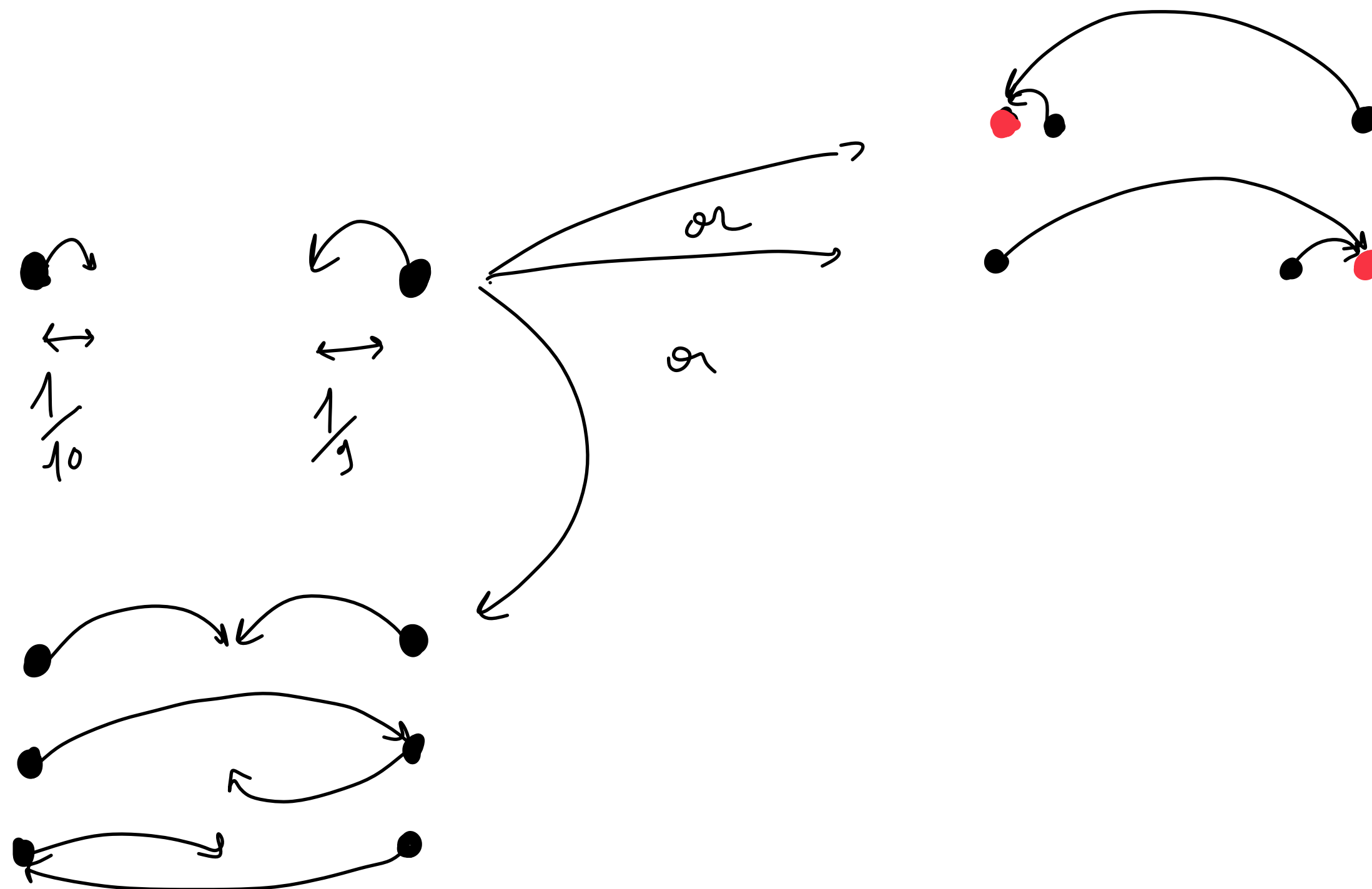
$i = 2$



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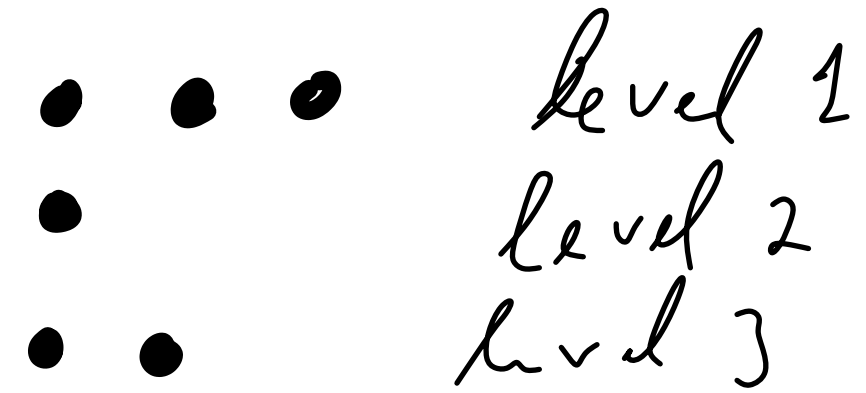
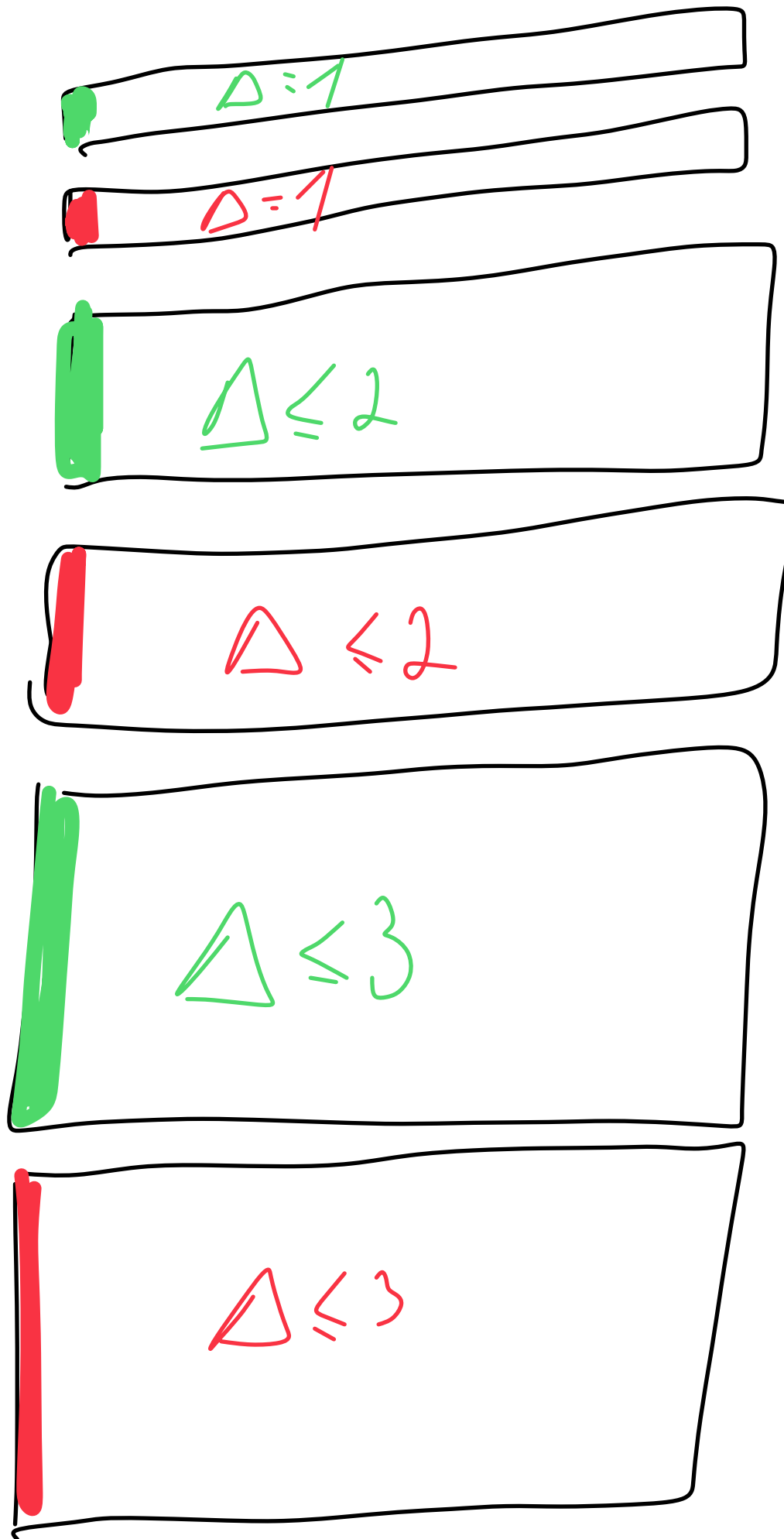
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$i = 2$
 $i = 3$
 $i = 4$
 $i = 5$



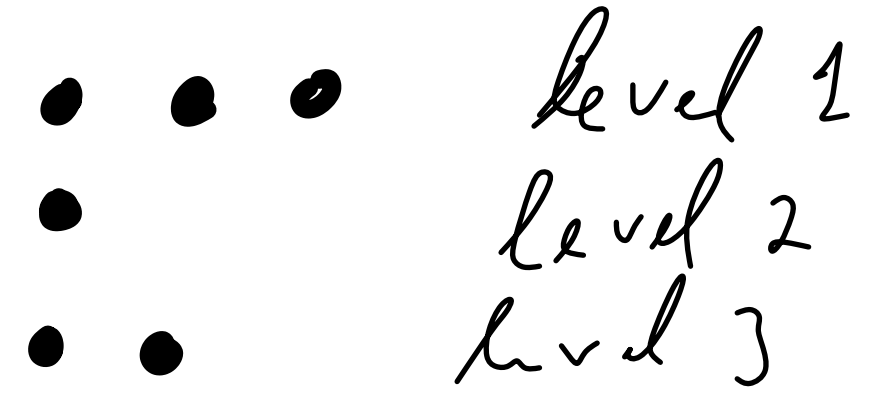
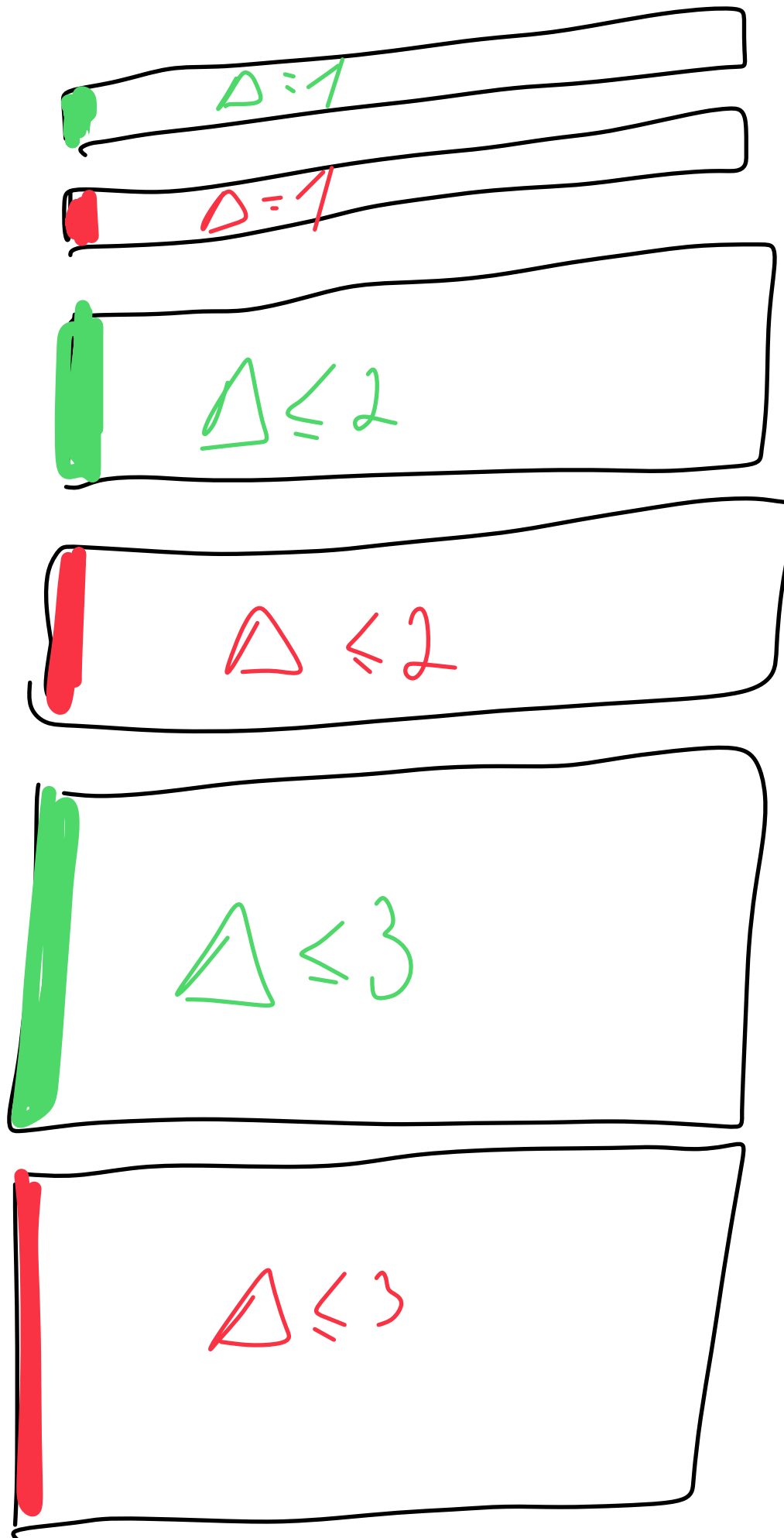
The Level-Slicing Technic

level i



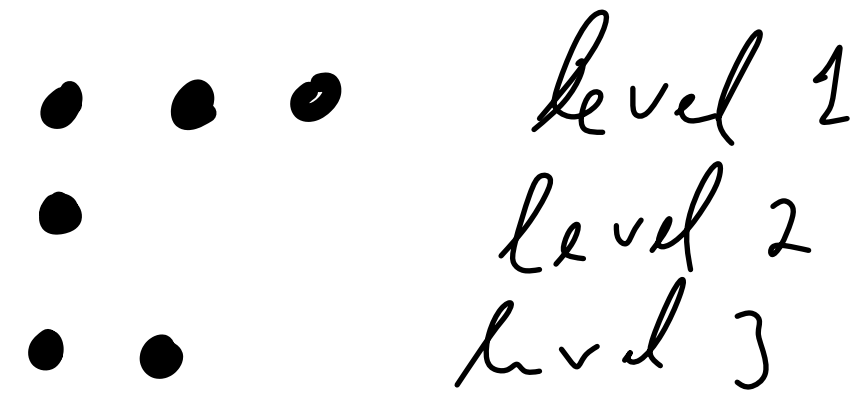
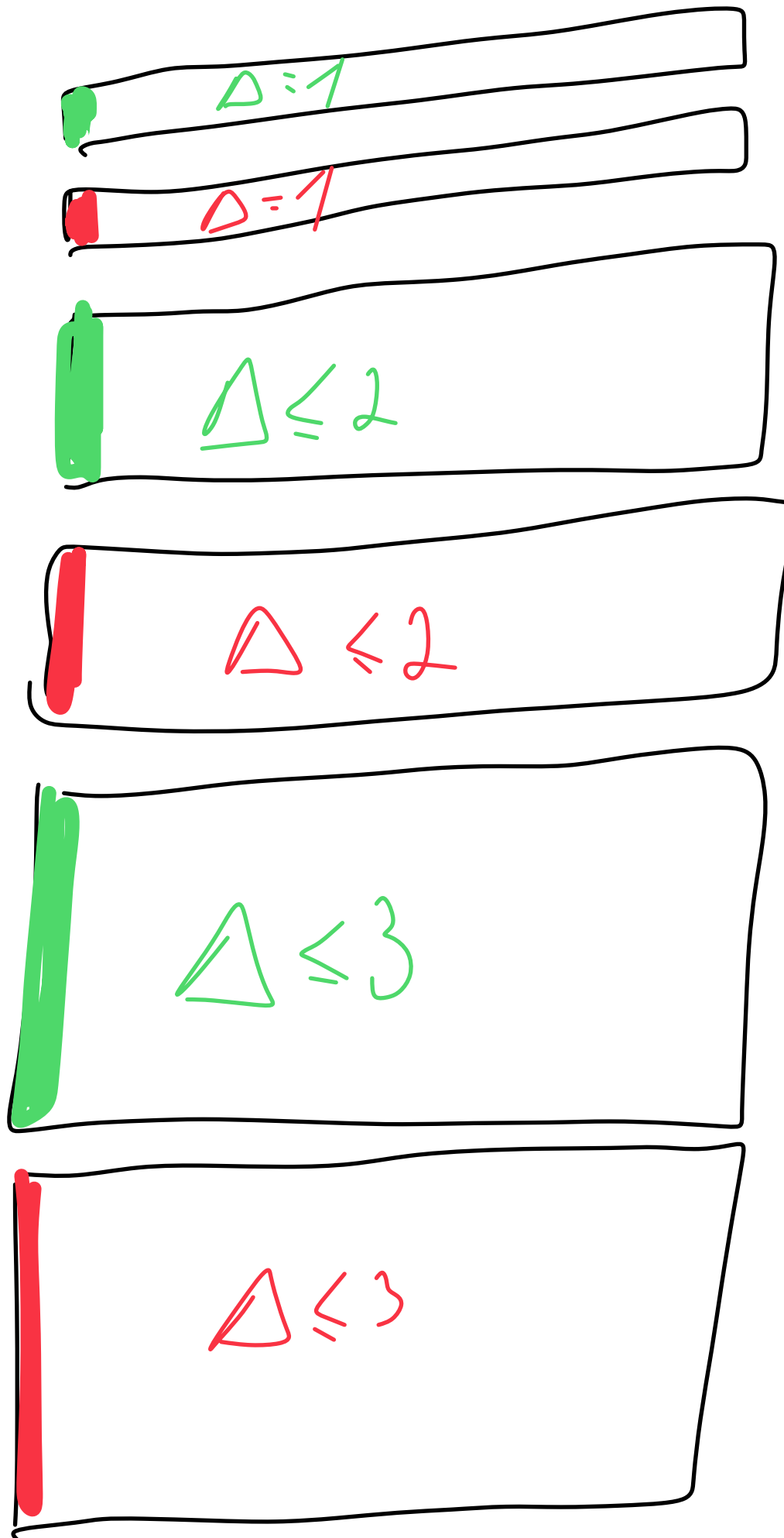
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level i



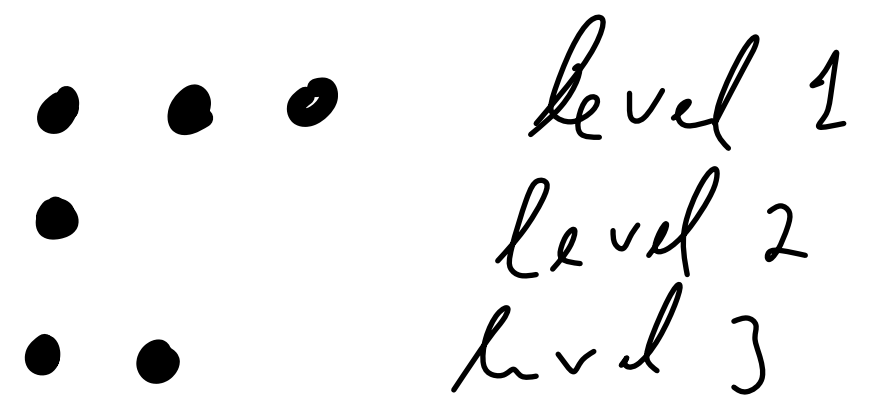
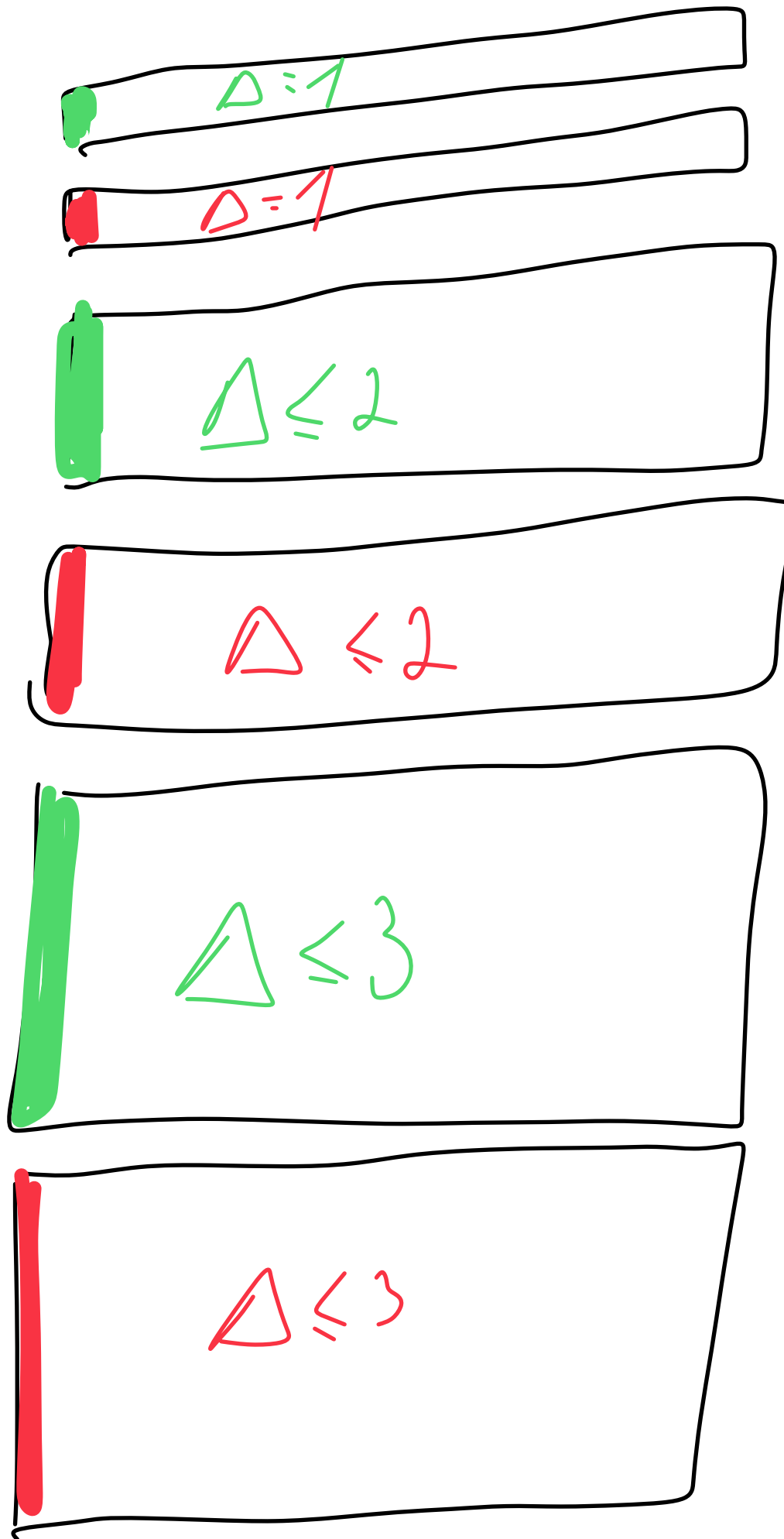
The Level-Slicing Technic

level i



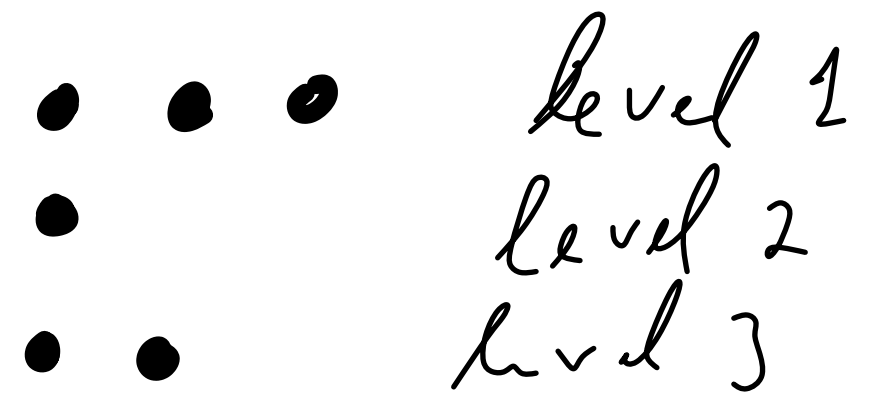
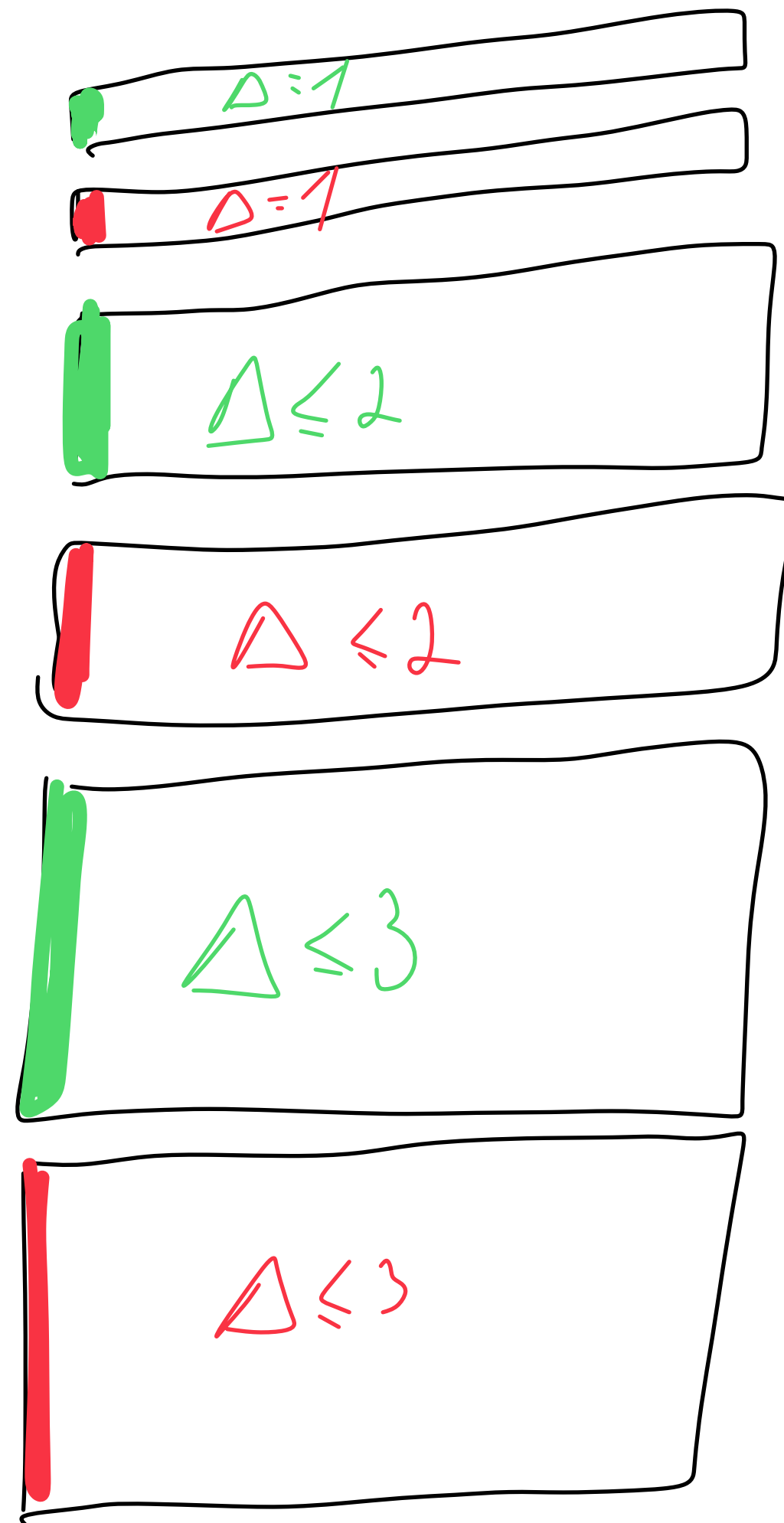
The Level-Slicing Technic

level i



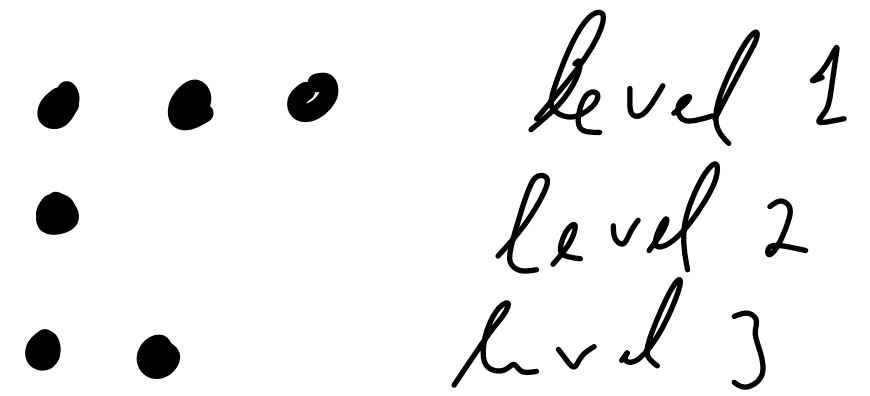
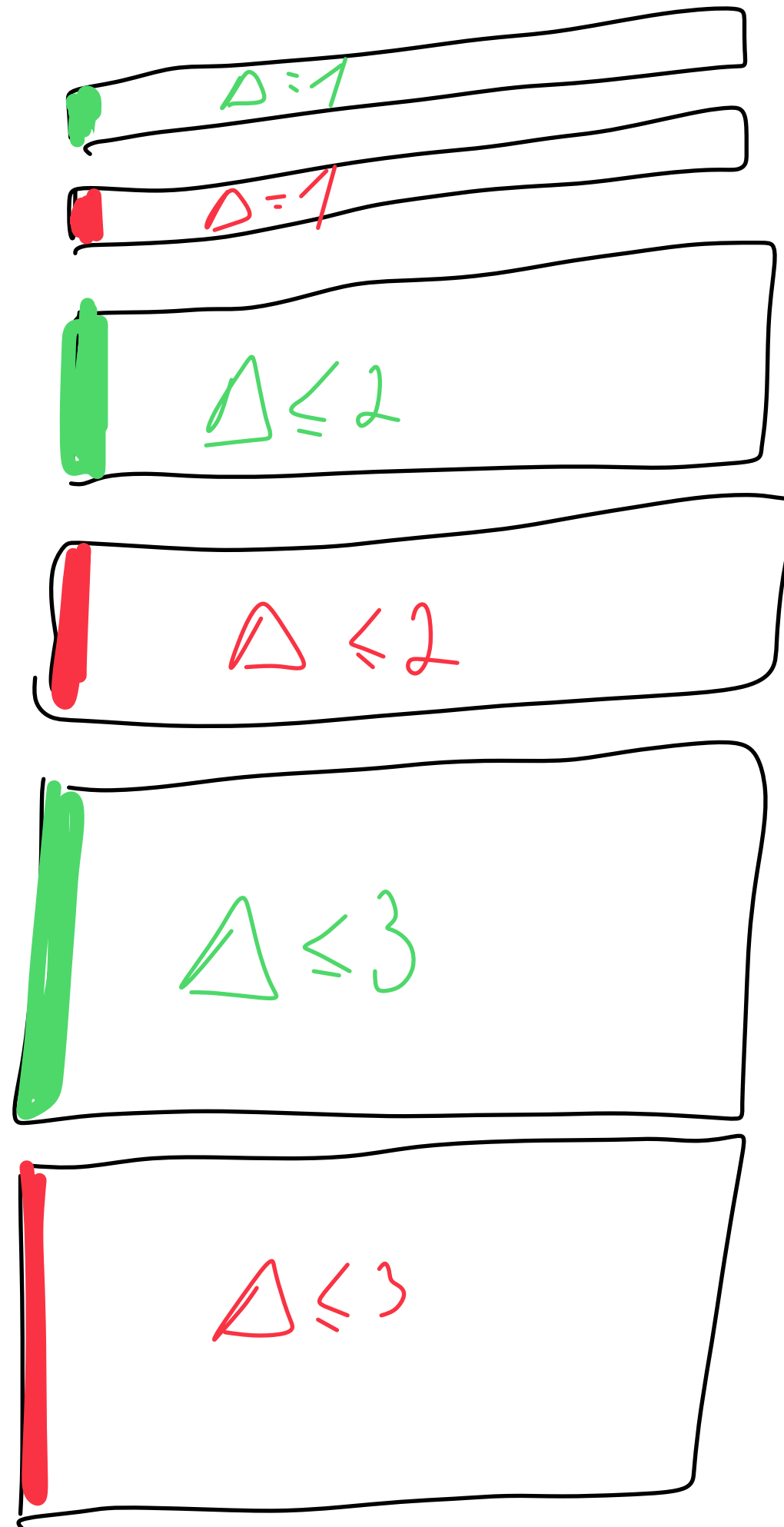
The Level-Slicing Technic

level i



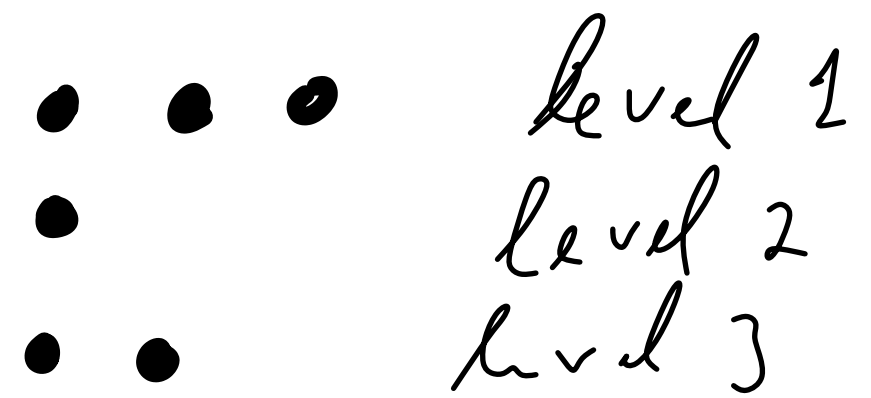
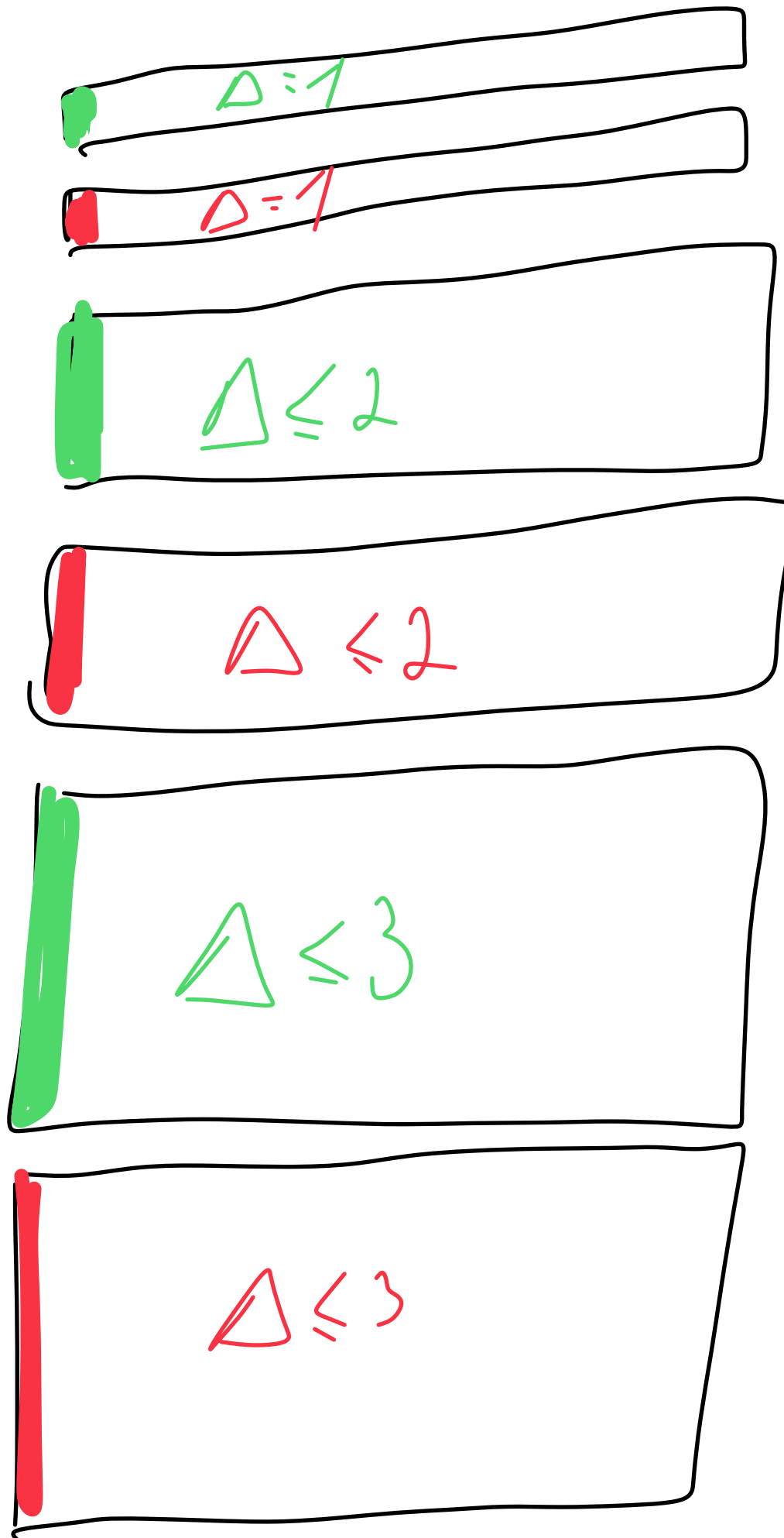
The Level-Slicing Technic

level i



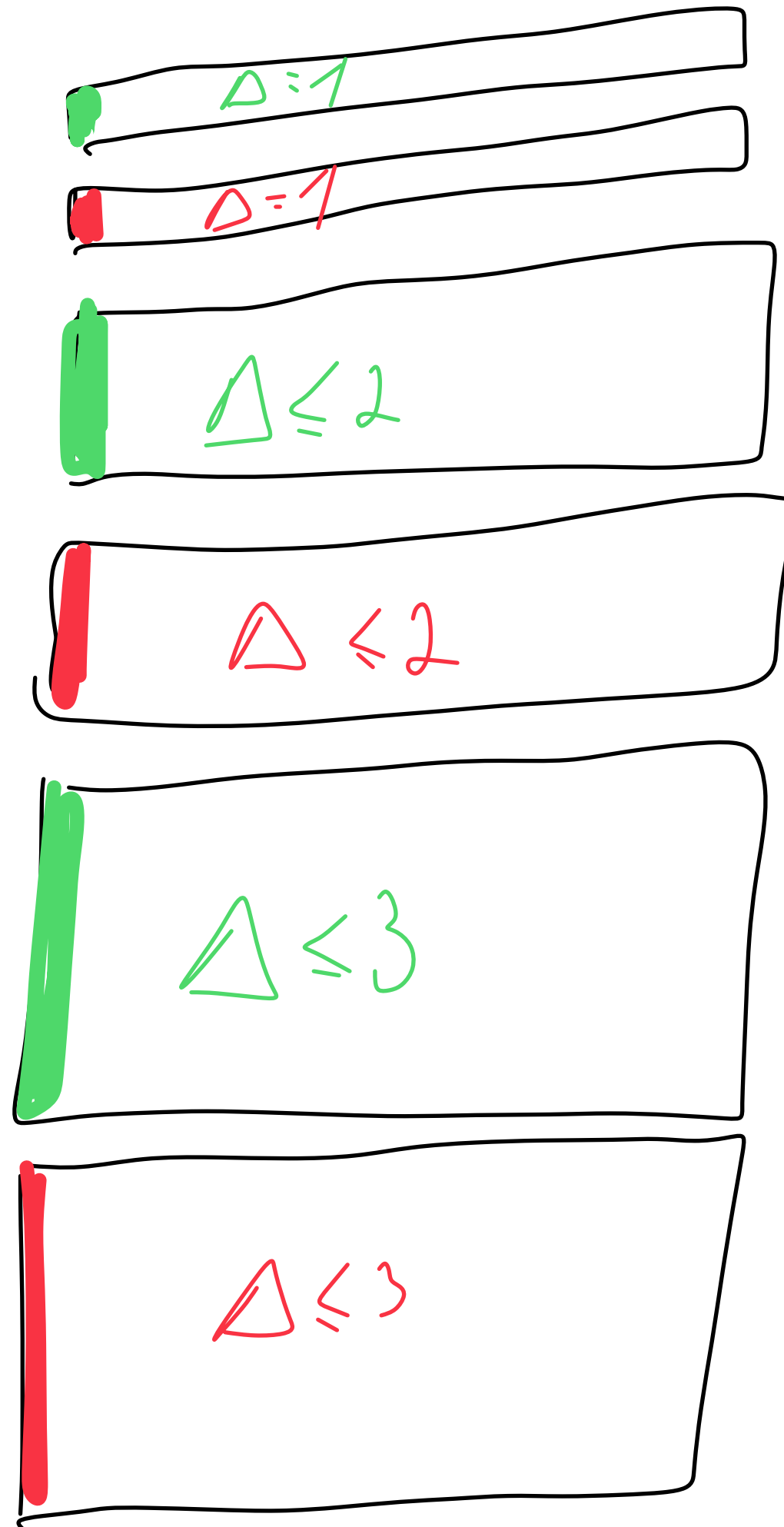
The Level-Slicing Technic

level i

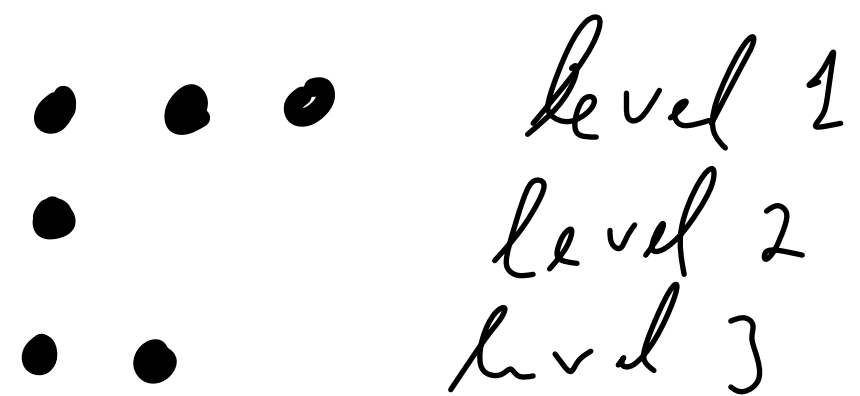


The Level-Slicing Technic

level i



⋮



Conclusion

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Thank you!