

Melocoton

A Program Logic for Verified Interoperability Between OCaml and C

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Journées SCALP

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MAX PLANCK INSTITUTE
FOR SOFTWARE SYSTEMS



AARHUS
UNIVERSITY
DEPARTMENT OF COMPUTER SCIENCE

Multi-Language Programs Are Everywhere



Python

C

Fortran



C++

Rust

JavaScript

OpenSSL
Cryptography and SSL/TLS Toolkit

C

Bindings for:

- Rust
- Python
- OCaml
- Go
- ...

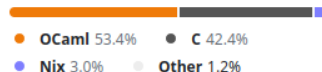
Multi-Language Programs Are Everywhere



☰ README.md

OCaml-SSL - OCaml bindings for the libssl

Languages



a mixture of C and OCaml code
connected using the OCaml **Foreign Function Interface (FFI)**

Go

...

Multi-Language Code is Unsafe

OCaml FFI code is **unsafe** and must follow **subtle FFI rules**

Buggy FFI code can produce **segfaults**, **corrupt memory**, break **type safety** and **data abstraction** guarantees of OCaml

The Goal: Verifying Multi-Language Code

How do we

verify functional correctness

of code written in

different languages?



Single-Language Functional Correctness

Hoare Logic for simple imperative languages.
Separation Logic for modularity and aliasing.

Multi-Language Functional Correctness





Multi-Language Functional Correctness

Existing work on Semantics and Logical Relations.

How do we prove functional correctness of individual, potentially unsafe libraries?

A Multi-Language Program in OCaml and C

A Multi-Language Program in OCaml and C

C business logic

```
void hash_ptr(int * x) {  
    // Implemented in OpenSSL  
    // tedious to port to OCaml  
}
```

A Multi-Language Program in OCaml and C

OCaml business logic

```
let main () =  
  let r = ref 42 in  
  hash_ref r; (*written in C*)  
  print_int !r
```

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C glue code

```
value caml_hash_ref(value r) {  
  int x = Int_val(Field(r, 0));  
  hash_ptr(&x);  
  Store_field(r, 0, Val_int(x));  
  return Val_unit;  
}
```

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A multi-language program logic for FFI

Goal: a **program logic** to prove correctness of FFI glue code

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A multi-language program logic for FFI

Goal: a **program logic** to prove correctness of FFI glue code

OCaml glue code



C glue code

```
 $\{r \mapsto_{ML} n\}$   
external hash_ref: int ref -> unit  
  = "caml_hash_ref"  
 $\{r \mapsto_{ML} m\}$ 
```

```
 $\{\gamma \mapsto_{blk[0|mut]} [n]\}$   
value caml_hash_ref(value r) {  
  int x = Int_val(Field(r, 0));  
  hash_ptr(&x);  
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}  
 $\{\gamma \mapsto_{blk[0|mut]} [m]\}$ 
```

Design choice: Language-Local Reasoning

Reuse existing program logics for OCaml and C.

Outside of glue code, one can **forget** about other languages

**Key Design Choice:
Preserve Language-Local Reasoning**

Our Contribution: Melocoton

λ_{ML+C} **Program Logic**

Glue Code Verification

λ_{ML+C} **Semantics**

Glue Code Semantics

- “The Usual Approach”: program logic on top of semantics, **but**
- **Language Interaction:** new semantics and logic for glue code

Our Contribution: Melocoton

OCaml* Program Logic

λ_{ML+C} Program Logic

C* Program Logic

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“The Usual Approach”: program logic on top of semantics, **but**

- **Language Interaction:** new semantics and logic for glue code
- **Language Locality:** embed existing semantics and logics

*simplified/idealized versions of OCaml and C

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Transfinite



The rest of this talk

1. A Crash Course on Building Separation Logics
2. Key Idea: Bridging Separation Logics with View Reconciliation
3. Application: Verifying `hash_ref`

Melocoton is based on **Separation Logic**
...but what is Separation Logic?

A Crash Course on (Building) Separation Logics



Hoare Logic

A logic for *compositional* program verification

Establishes “Hoare triples”: $\vdash \{P\} C \{Q\}$

Compositional proof rules:

$$\text{SEQ} \frac{\{P\} C_1 \{Q\} \quad \{Q\} C_2 \{R\}}{\{P\} C_1; C_2 \{R\}} \quad \dots$$

Hoare Logic

A logic for *compositional* program verification

Establishes “Hoare triples”:

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↑
Code we are verifying

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Hoare Logic

A logic for *compositional* program verification

Establishes “Hoare triples”:

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Precondition

Compositional proof rules:

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Hoare Logic

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Postcondition

Compositional proof rules:

$$\text{SEQ} \quad \frac{\{P\} C_1 \{Q\} \quad \{Q\} C_2 \{R\}}{\{P\} C_1; C_2 \{R\}} \quad \dots$$

Separation Logic

- Extension of Hoare Logic for reasoning about pointer-manipulating programs (C, OCaml, ...)
- Assertions P, Q denote **ownership** of state (=memory)
→ “ $x \mapsto v$ ” = We own x (and it points to v)
- $P * Q$ means P and Q own **disjoint** state
→ e.g. if we can assert $x \mapsto v * y \mapsto w$,
it means that $x \neq y$, i.e. **they do not alias**

Separation Logic for OCaml: Example Rules

“ $r \mapsto v$ ” = We own the OCaml reference r (and it points to v)

CREATEREF

$$\frac{}{\{\text{True}\} \text{ref } v \{ \lambda r. r \mapsto v \}}$$

READREF

$$\frac{}{\{r \mapsto v\} !r \{ \lambda v'. v' = v \wedge r \mapsto v \}}$$

WRITEREF

$$\frac{}{\{r \mapsto v\} r := w \{r \mapsto w\}}$$

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program creating a new reference

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READREF

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Ownership over the new reference



READREF

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Separation Logic: The Frame Rule

Hoare Logic is compositional wrt. different parts of a program.

Separation Logic is also compositional wrt. **disjoint parts of memory**. SL specifications are “**small footprint**”.

The following holds:

$$\frac{\frac{}{\{\text{True}\} \text{ref } v \{\lambda r. r \mapsto v\}}}{\{\text{True}\} \text{ref } v \{\lambda r. r \mapsto v\}}}{\{x \mapsto w\} \text{ref } v \{\lambda r. x \mapsto w * r \mapsto v\}}$$

Separation Logic: The Frame Rule

Hoare Logic is compositional wrt. different parts of a program.

Separation Logic is also compositional wrt. **disjoint parts of memory**. SL specifications are “**small footprint**”.

More generally, the **frame rule** holds:

$$\text{FRAME} \frac{\{P\} e \{Q\}}{\{P * R\} e \{Q * R\}}$$

Fifty Shades of Separation Logics

These core principles are **very versatile**.

Melocoton: a new SL for the **OCaml FFI**, embedding existing SLs for **OCaml** and **C**

Other SLs successfully built for **many programming languages**:

Multicore OCaml

Rust

C11+Weak Memory

WASM

Distributed systems

...



A Separation Logic For **Your Language**: Checklist

- A **Base Logic** of assertions:
 - generic connectives:
 $\exists/\forall x.P(x), P \vee Q, P \wedge Q, P \Rightarrow Q, P * Q, P \multimap Q, \dots$
 - **language-specific assertions**: $x \mapsto v$
- Triples $\vdash \{P\} e \{Q\}$ + FRAME + **proof rules** for language constructs

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a bunch of definitions

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 - **language-specific assertions**: $x \mapsto v$
- Triples $\vdash \{P\} e \{Q\} + \text{FRAME} +$ **proof rules** for language constructs
- An **Adequacy Theorem**: $\vdash \{\text{True}\} e \{\text{True}\} \Rightarrow e$ is safe.
“safe”: according to the **language semantics**

Models of Separation Logic

Prove Adequacy by defining a **model** of:

base assertions: $\llbracket P \rrbracket$ validity of triples: $\models \{P\} e \{Q\}$

such that:

$\vdash \{P\} e \{Q\} \implies \models \{P\} e \{Q\}$ (the hard part)

$\models \{\text{True}\} e \{\text{True}\} \implies e \text{ is safe}$ (trivial by def. of \models)

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predicate on memories

similar to Hoare logic

Models of Separation Logics: Base Logic

The **interesting part**: interpretation of base assertions $\llbracket P \rrbracket$

In general: $\llbracket P \rrbracket : R \rightarrow \text{Prop}$

with R **any** *Partial Commutative Monoid* equipped with \uplus

$$\begin{aligned}\llbracket \text{True} \rrbracket(r) &\triangleq \text{True} \\ \llbracket P * Q \rrbracket(r) &\triangleq \exists r_1, r_2. r = r_1 \uplus r_2 \wedge \llbracket P \rrbracket(r_1) \wedge \llbracket Q \rrbracket(r_2)\end{aligned}$$

For OCaml, pick $R = \text{Loc} \xrightarrow{\text{fin}} \text{Val}$:

$$\llbracket \ell \mapsto v \rrbracket(\sigma) \triangleq \ell \in \text{dom}(\sigma) \wedge \sigma(\ell) = v$$

Models of Separation Logics: Base Logic

The **interesting part**: interpretation of base assertions $\llbracket P \rrbracket$

In general, $\llbracket R \rrbracket = R \wedge \text{Down}$
with

You are free to pick **any PCM** R that:

- is **customized for your language semantics**
- includes **extra resources** (“ghost state”) not directly tied to program execution

For OCaml, pick $R = \text{Loc} \stackrel{\text{fin}}{\multimap} \text{Val}$:

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Iris: a Framework for Building Separation Logics

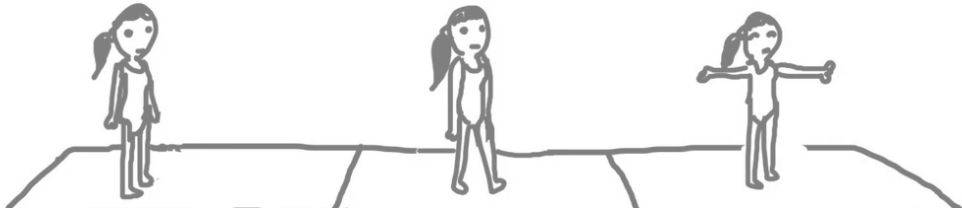


Iris provides SL building blocks as **reusable, language agnostic** Coq libraries:

- **expressive base logic** parameterized by an arbitrary PCM
- modular **pre-built PCMs**
- predefined **triples** and their **adequacy theorem**

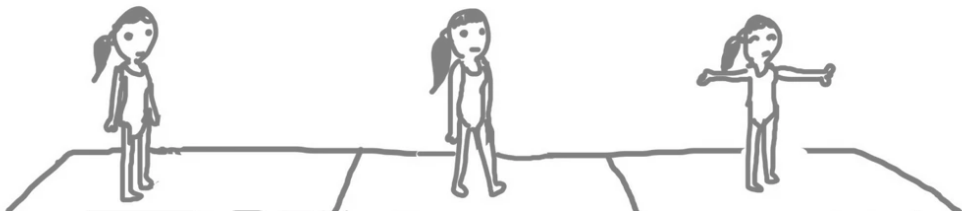
Most steps of the Checklist become `Require Import iris!`

mono-language separation logic gymnastics



**Bridging Separation Logics with
View Reconciliation**

mono-language separation logic gymnastics



**Bridging Separation Logics with
View Reconciliation**

multi-language separation logic gymnastics



Melocoton brings the Checklist to a multi-language setting

OCaml SL

$\{P\} e_{\text{ML}} \{Q\}$

$r \mapsto_{\text{ML}} v$

+

FFI SL

$\{P\} e_{\text{FFI}} \{Q\}$

$\gamma \mapsto_{\text{blk}[0|\text{mut}]} \text{blk}$

+

C SL

$\{P\} e_{\text{C}} \{Q\}$

$a \mapsto_{\text{C}} w$

OCaml semantics

$(e_{\text{ML}}, \sigma) \rightsquigarrow (e_{\text{ML}}, \sigma)$

FFI semantics

$(e_{\text{FFI}}, \rho) \rightsquigarrow (e_{\text{FFI}}, \rho)$

C semantics

$(e_{\text{C}}, m) \rightsquigarrow (e_{\text{C}}, m)$

Problem: how do we connect the different languages/logics?

Language Interaction: Different Views of the Same Data

OCaml glue code

```
external hash_ref: int ref -> unit
  = "caml_hash_ref"
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How is **OCaml data** accessed from **C glue code**?

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How is **OCaml data** accessed from **C glue code**?

High-level **OCaml values** are accessed..
..through a **low-level block representation**.

Language Interaction: Semantics

High-level **OCaml** value \sim_{ML} Low-level **block** representation

Language Interaction: Semantics

High-level **OCaml** value \sim_{ML} Low-level **block** representation

integers \sim_{ML} integers

booleans \sim_{ML} integers (0 or 1)

true \sim_{ML} *1*

Language Interaction: Semantics

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λ_{ML+C} **Semantics**

$\sigma : Heap_{ML}$

$\zeta : BlockHeap$

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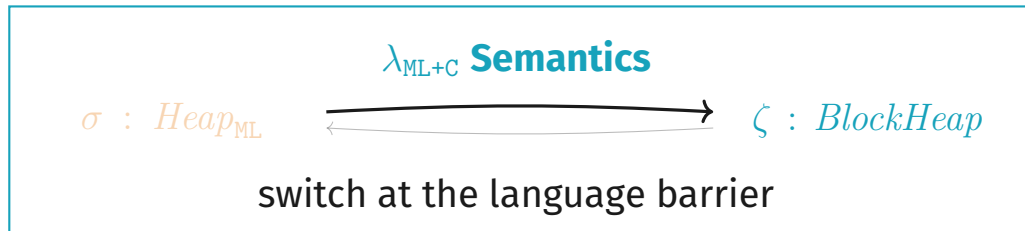
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Language Interaction: Program Logic, Take 1

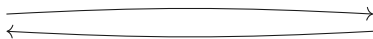


Language Interaction: Program Logic, Take 1

$\lambda_{\text{ML+C}}$ Program Logic

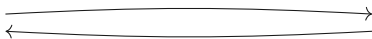
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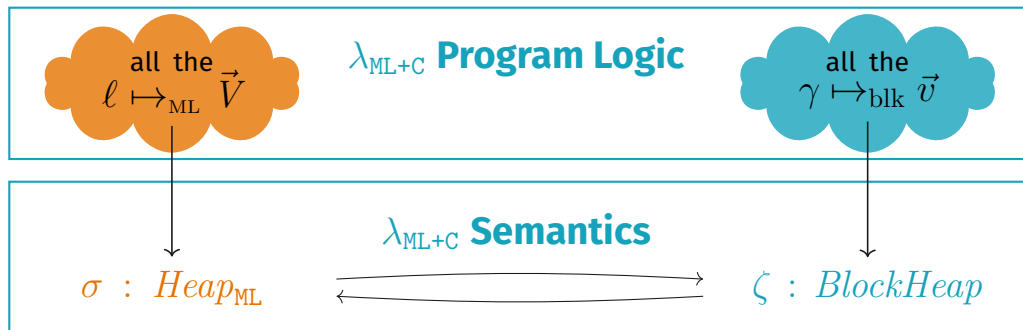


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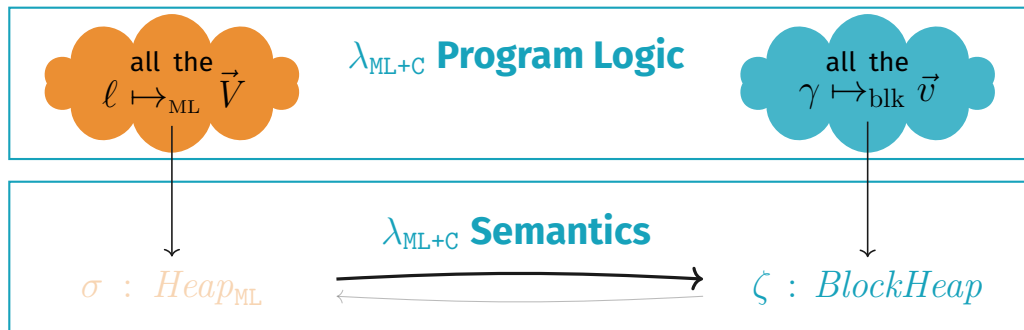
Language Interaction: Program Logic, Take 1

 $\ell \mapsto_{\text{ML}} \vec{V}$ $\lambda_{\text{ML+C}}$ **Program Logic** $\gamma \mapsto_{\text{blk}} \vec{v}$ $\sigma : \text{Heap}_{\text{ML}}$ $\lambda_{\text{ML+C}}$ **Semantics** $\zeta : \text{BlockHeap}$ 

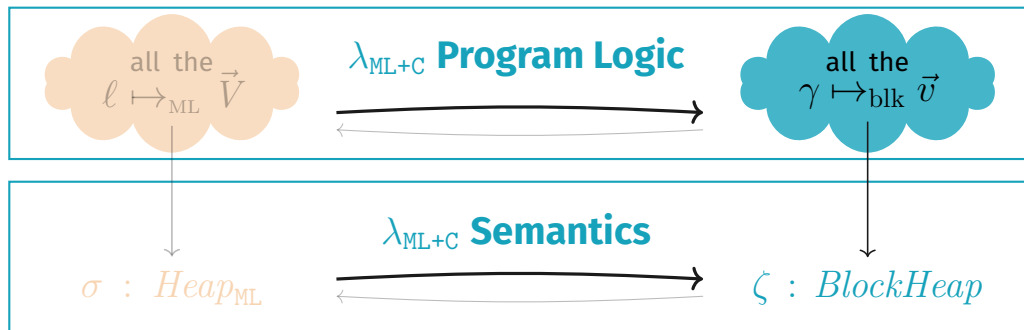
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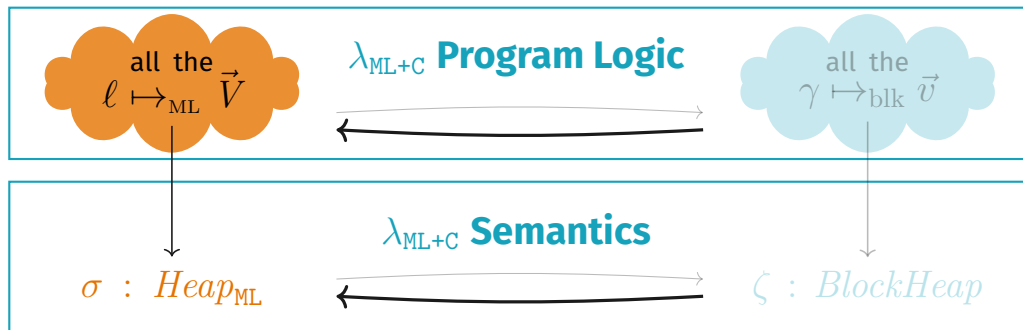
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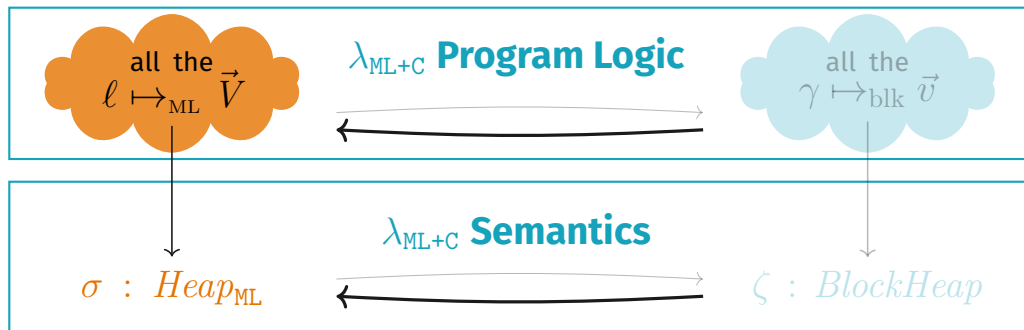
Language Interaction: Program Logic, Take 1



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Language Interaction: Program Logic, Take 1

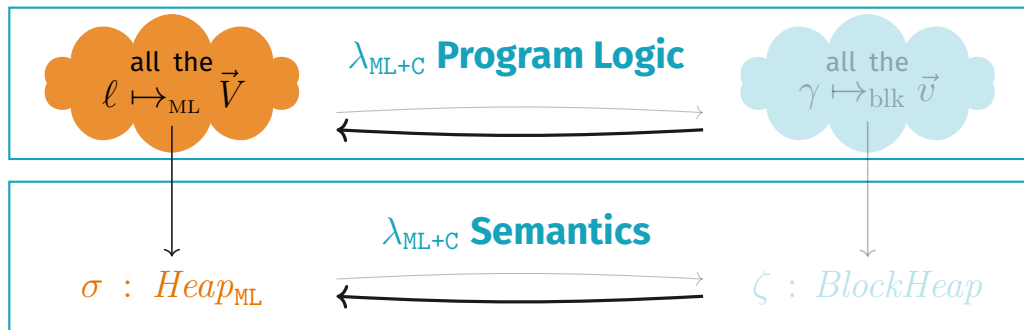


EXTCALL

{ all } C function body { all }

{ all } call into C { all }

Language Interaction: Program Logic, Take 1



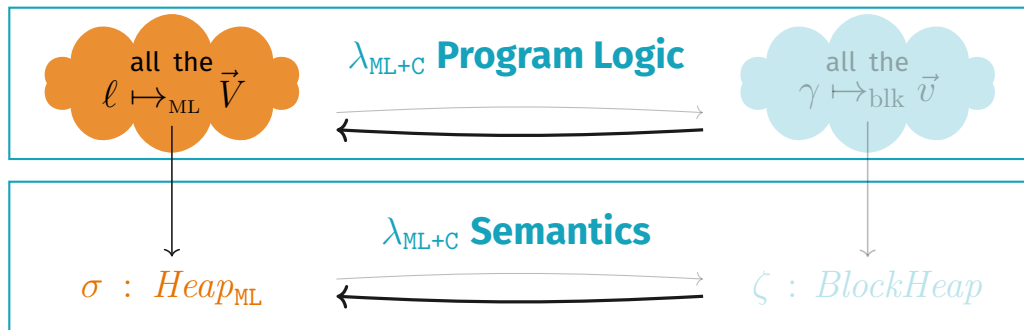
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FRAME

$$\frac{\{P\} e \{Q\}}{\{R * P\} e \{Q * R\}}$$

Language Interaction: Program Logic, Take 1



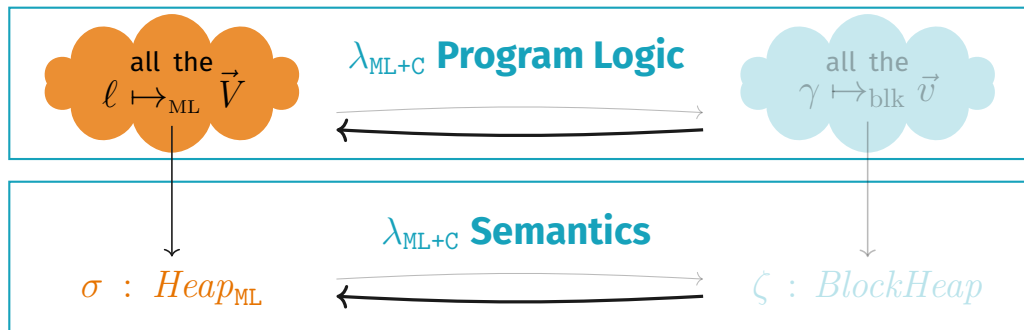
EXTCALL

$$\frac{\{ \text{all} \} \mathbf{C} \text{ function body } \{ \text{all} \}}{\{ \text{all} \} \text{ call into } \mathbf{C} \{ \text{all} \}}$$

FRAME

$$\frac{\{P\} \text{ call into } \mathbf{C} \{Q\}}{\{R * P\} \text{ call into } \mathbf{C} \{Q * R\}}$$

Language Interaction: Program Logic, Take 1



EXTCALL

$\{\text{all}\} \mathbf{C}$ function body $\{\text{all}\}$

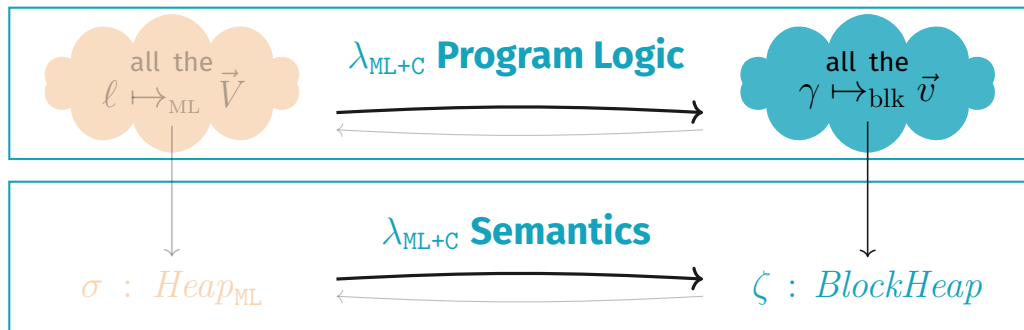
$\{\text{all}\}$ call into \mathbf{C} $\{\text{all}\}$

FRAME

$\{P\}$ call into \mathbf{C} $\{Q\}$

$\{\ell \mapsto_{\text{ML}} \vec{V} * P\}$ call into \mathbf{C} $\{Q * \ell \mapsto_{\text{ML}} \vec{V}\}$

Language Interaction: Program Logic, Take 1



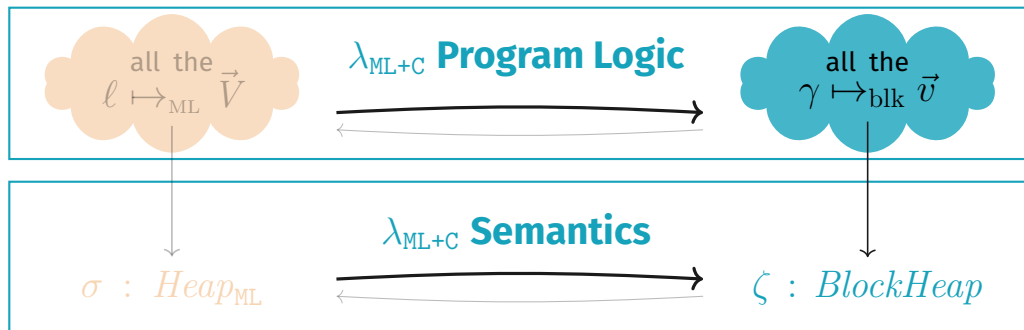
EXTCALL

$$\frac{\{\text{all}\} \mathbf{C} \text{ function body } \{\text{all}\}}{\{\text{all}\} \text{ call into } \mathbf{C} \{\text{all}\}}$$

FRAME

$$\frac{\{P\} \text{ call into } \mathbf{C} \{Q\}}{\{l \mapsto_{ML} \vec{V} * P\} \text{ call into } \mathbf{C} \{Q * l \mapsto_{ML} \vec{V}\}}$$

Language Interaction: Program Logic, Take 1



EXTCALL

$\{\text{all}\} \mathbf{C}$ function body $\{\text{all}\}$ **RAME** $\{P\}$ call into \mathbf{C} $\{Q\}$

 $\{\text{all}\}$ call into \mathbf{C} $\{\text{all}\}$ $\{\ell \mapsto_{ML} \vec{V} * P\}$ call into \mathbf{C} $\{Q * \ell \mapsto_{ML} \vec{V}\}$

Language Interaction: Program Logic, Take 1

λ_{ML+C} Program Logic

The λ_{ML+C} Semantics operate **globally** on the state



The λ_{ML+C} Program Logic needs **local** reasoning rules

EXTCALL

$\{\text{all}\} \mathbf{C}$ function body $\{\text{all}\}$

RAME

$\{P\}$ call into \mathbf{C} $\{Q\}$

$\{\text{all}\}$ call into \mathbf{C} $\{\text{all}\}$

$\{\ell \mapsto_{ML} \vec{V} * P\}$ call into \mathbf{C} $\{Q * \ell \mapsto_{ML} \vec{V}\}$

Language Interaction: More Gradual Rules

OCaml *points-tos* remain valid when switching to **C**!

Language Interaction: More Gradual Rules

OCaml *points-tos* remain valid when switching to **C**!

$$l \mapsto_{\text{ML}} \vec{V}$$

Language Interaction: More Gradual Rules

OCaml *points-tos* remain valid when switching to **C!**

$$l \mapsto_{\text{ML}} \vec{V} \quad l_1 \mapsto_{\text{ML}} \vec{V}_1$$

Language Interaction: More Gradual Rules

OCaml *points-tos* remain valid when switching to **C!**

$$l \mapsto_{\text{ML}} \vec{V} \quad \gamma_1 \mapsto_{\text{blk}} \vec{v}_1$$

Language Interaction: More Gradual Rules

OCaml points-tos *remain valid* when switching to **C!**

$$\gamma_2 \mapsto_{\text{blk}} \vec{v}_2$$

$$\ell \mapsto_{\text{ML}} \vec{V}$$

$$\gamma_1 \mapsto_{\text{blk}} \vec{v}_1$$

Language Interaction: More Gradual Rules

OCaml points-tos *remain valid* when switching to **C!**

$$\gamma_2 \mapsto_{\text{blk}} \vec{v}_2$$

$$l \mapsto_{\text{ML}} \vec{V}$$

Language Interaction: More Gradual Rules

OCaml *points-tos* remain valid when switching to **C!**

$$l \mapsto_{\text{ML}} \vec{V}$$

Language Interaction: More Gradual Rules

OCaml points-tos *remain valid* when switching to **C!**

$$l \mapsto_{\text{ML}} \vec{V}$$

View Reconciliation Rules for Converting On-Demand:

$$\begin{aligned} l \mapsto_{\text{ML}} \vec{V} &\equiv * \exists \gamma \vec{v}. \gamma \mapsto_{\text{blk}} \vec{v} * l \sim_{\text{ML}} \gamma * \vec{V} \sim_{\text{ML}} \vec{v} \\ \vec{V} \sim_{\text{ML}} \vec{v} * \gamma \mapsto_{\text{blk}} \vec{v} &\equiv * \exists l. l \mapsto_{\text{ML}} \vec{V} * l \sim_{\text{ML}} \gamma \end{aligned}$$

Language Interaction: View Reconciliation

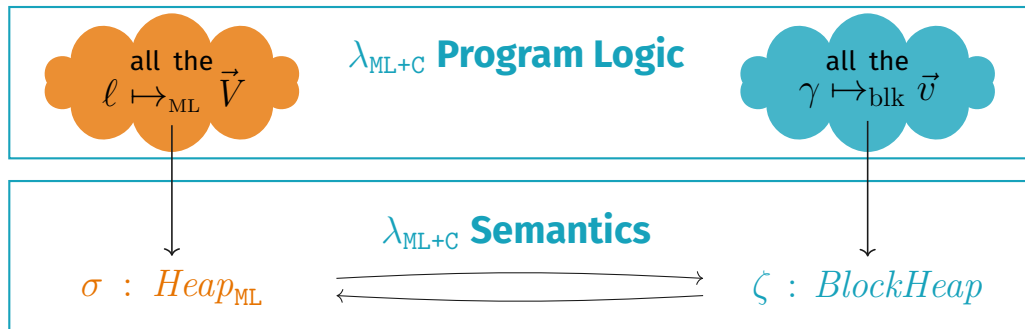
View Reconciliation Rules

$$\begin{aligned} l \mapsto_{\text{ML}} \vec{V} &\equiv * \exists \gamma \vec{v}. \gamma \mapsto_{\text{blk}} \vec{v} * l \sim_{\text{ML}} \gamma * \vec{V} \sim_{\text{ML}} \vec{v} \\ \vec{V} \sim_{\text{ML}} \vec{v} * \gamma \mapsto_{\text{blk}} \vec{v} &\equiv * \exists l . l \mapsto_{\text{ML}} \vec{V} * l \sim_{\text{ML}} \gamma \end{aligned}$$

Language Interaction: View Reconciliation

View Reconciliation Rules

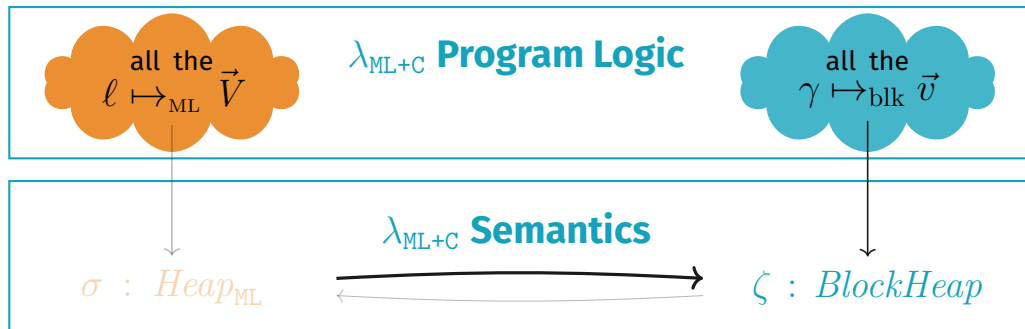
$$\begin{aligned} l \mapsto_{\text{ML}} \vec{V} &\equiv * \exists \gamma \vec{v}. \gamma \mapsto_{\text{blk}} \vec{v} * l \sim_{\text{ML}} \gamma * \vec{V} \sim_{\text{ML}} \vec{v} \\ \vec{V} \sim_{\text{ML}} \vec{v} * \gamma \mapsto_{\text{blk}} \vec{v} &\equiv * \exists l . l \mapsto_{\text{ML}} \vec{V} * l \sim_{\text{ML}} \gamma \end{aligned}$$



Language Interaction: View Reconciliation

View Reconciliation Rules

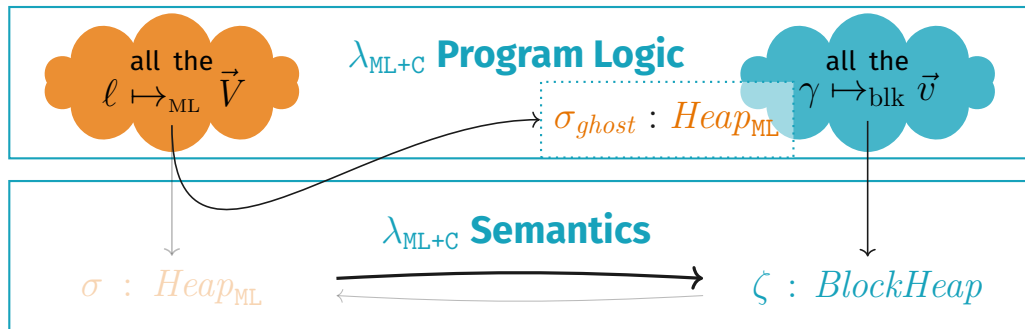
$$\begin{aligned} l \mapsto_{\text{ML}} \vec{V} &\equiv * \exists \gamma \vec{v}. \gamma \mapsto_{\text{blk}} \vec{v} * l \sim_{\text{ML}} \gamma * \vec{V} \sim_{\text{ML}} \vec{v} \\ \vec{V} \sim_{\text{ML}} \vec{v} * \gamma \mapsto_{\text{blk}} \vec{v} &\equiv * \exists l . l \mapsto_{\text{ML}} \vec{V} * l \sim_{\text{ML}} \gamma \end{aligned}$$



Language Interaction: View Reconciliation

View Reconciliation Rules

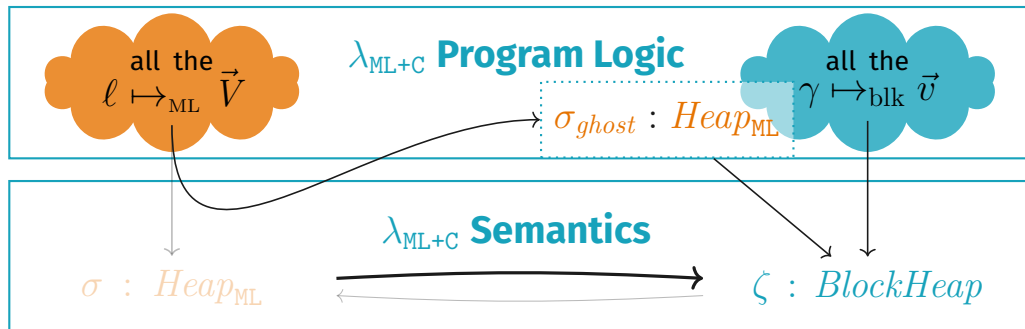
$$\begin{aligned} l \mapsto_{\text{ML}} \vec{V} &\equiv * \exists \gamma \vec{v}. \gamma \mapsto_{\text{blk}} \vec{v} * l \sim_{\text{ML}} \gamma * \vec{V} \sim_{\text{ML}} \vec{v} \\ \vec{V} \sim_{\text{ML}} \vec{v} * \gamma \mapsto_{\text{blk}} \vec{v} &\equiv * \exists l. l \mapsto_{\text{ML}} \vec{V} * l \sim_{\text{ML}} \gamma \end{aligned}$$



Language Interaction: View Reconciliation

View Reconciliation Rules

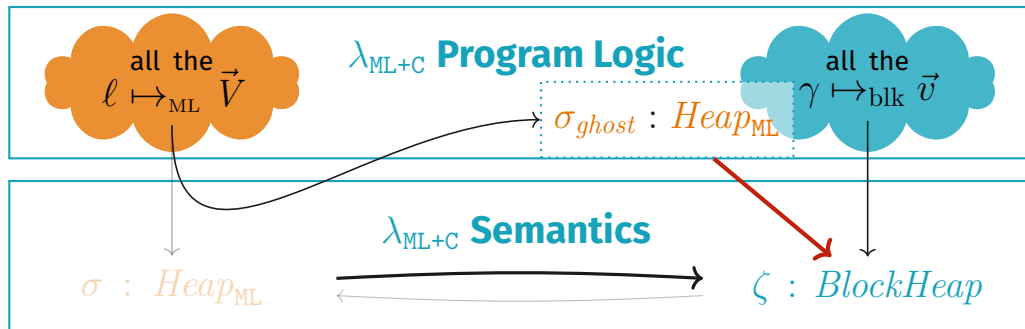
$$\begin{aligned}
 l \mapsto_{\text{ML}} \vec{V} &\equiv * \exists \gamma \vec{v}. \gamma \mapsto_{\text{blk}} \vec{v} * l \sim_{\text{ML}} \gamma * \vec{V} \sim_{\text{ML}} \vec{v} \\
 \vec{V} \sim_{\text{ML}} \vec{v} * \gamma \mapsto_{\text{blk}} \vec{v} &\equiv * \exists l. l \mapsto_{\text{ML}} \vec{V} * l \sim_{\text{ML}} \gamma
 \end{aligned}$$



Language Interaction: View Reconciliation

View Reconciliation Rules

$$\begin{aligned} l \mapsto_{\text{ML}} \vec{V} &\equiv * \exists \gamma \vec{v}. \gamma \mapsto_{\text{blk}} \vec{v} * l \sim_{\text{ML}} \gamma * \vec{V} \sim_{\text{ML}} \vec{v} \\ \vec{V} \sim_{\text{ML}} \vec{v} * \gamma \mapsto_{\text{blk}} \vec{v} &\equiv * \exists l. l \mapsto_{\text{ML}} \vec{V} * l \sim_{\text{ML}} \gamma \end{aligned}$$



Application: Verifying `hash_ref` with Melocoton

Verifying hash_ref with Melocoton

OCaml glue code

```
external hash_ref: int ref -> unit
  = "caml_hash_ref"
```

C glue code

```
value caml_hash_ref(value v) {
  int x = Int_val(Field(v, 0));
  hash_ptr(&x);
  Store_field(v, 0, Val_int(x));
  return Val_unit;
}
```

Verifying `hash_ref` with Melocoton

OCaml glue code

```
external hash_ref: int ref -> unit
  = "caml_hash_ref"

  { $r \mapsto_{ML} n$ }
  hash_ref(r)
  { $\exists m. r \mapsto_{ML} m$ }
```

C glue code

```
value caml_hash_ref(value v) {
  int x = Int_val(Field(v, 0));
  hash_ptr(&x);
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}
```

Verifying hash_ref with Melocoton

OCaml glue code

```
external hash_ref: int ref -> unit
  = "caml_hash_ref"

  {r ↦ML n}
    hash_ref(r)
  {∃m. r ↦ML m}
```

C glue code

```
value caml_hash_ref(value v) {
  int x = Int_val(Field(v, 0));
  hash_ptr(&x);
  Store_field(v, 0, Val_int(x));
  return Val_unit;
}
```

EXTCALL

$$\frac{\{P * x \sim_{\text{ML}} v\} f(v) \{\lambda v'. \exists y. y \sim_{\text{ML}} v' * Q(y)\}}{\{P\} \text{external } "f"(x) \{\lambda y. Q(y)\}}$$

Verifying hash_ref with Melocoton

OCaml glue code

```
external hash_ref: int ref -> unit
  = "caml_hash_ref"

  { $r \mapsto_{ML} n$ }
  hash_ref(r)
  { $\exists m. r \mapsto_{ML} m$ }
```

C glue code

```
value caml_hash_ref(value v) {
  { $r \mapsto_{ML} n * r \sim_{ML} v$ }
  int x = Int_val(Field(v, 0));
  hash_ptr(&x);
  Store_field(v, 0, Val_int(x));
  return Val_unit;
  { $\exists m. r \mapsto_{ML} m * \exists y. y \sim_{ML} Val\_unit$ }
}
```

EXTCALL

$$\frac{\{P * x \sim_{ML} v\} f(v) \{\lambda v'. \exists y. y \sim_{ML} v' * Q(y)\}}{\{P\} \text{external "f"}(x) \{\lambda y. Q(y)\}}$$

Verifying hash_ref with Melocoton

OCaml glue code

```
external hash_ref: int ref -> unit
  = "caml_hash_ref"

  { $r \mapsto_{ML} n$ }
  hash_ref(r)
  { $\exists m. r \mapsto_{ML} m$ }
```

C glue code

```
value caml_hash_ref(value v) {
  { $r \mapsto_{ML} n * r \sim_{ML} v$ }
  int x = Int_val(Field(v, 0));
  hash_ptr(&x);
  Store_field(v, 0, Val_int(x));
  return Val_unit;
  { $\exists m. r \mapsto_{ML} m * () \sim_{ML} Val\_unit$ }
}
```

EXTCALL

$$\frac{\{P * x \sim_{ML} v\} f(v) \{\lambda v'. \exists y. y \sim_{ML} v' * Q(y)\}}{\{P\} \text{external "f"}(x) \{\lambda y. Q(y)\}}$$

Verifying hash_ref with Melocoton

OCaml glue code

```
external hash_ref: int ref -> unit
  = "caml_hash_ref"

  {r ↦ML n}
  hash_ref(r)
  {∃m. r ↦ML m}
```

C glue code

```
value caml_hash_ref(value v) {
  {r ↦ML n * r ~ML v}
  {v ↦blk [n] * r ~ML v}
  int x = Int_val(Field(v, 0));
  hash_ptr(&x);
  Store_field(v, 0, Val_int(x));
  return Val_unit;

  {∃m. r ↦ML m * () ~ML Val_unit}
}
```

VIEW RECONCILIATION (1)

$$l \mapsto_{\text{ML}} \vec{V} \equiv * \exists \gamma \vec{v}. \gamma \mapsto_{\text{blk}} \vec{v} * l \sim_{\text{ML}} \gamma * \vec{V} \sim_{\text{ML}} \vec{v}$$

Verifying hash_ref with Melocoton

OCaml glue code

```
external hash_ref: int ref -> unit
  = "caml_hash_ref"

  {r ↦ML n}
  hash_ref(r)
  {∃m. r ↦ML m}
```

C glue code

```
value caml_hash_ref(value v) {
  {r ↦ML n * r ~ML v}
  {v ↦blk [n] * r ~ML v}
  int x = Int_val(Field(v, 0));
  hash_ptr(&x);
  Store_field(v, 0, Val_int(x));
  return Val_unit;

  {∃m. v ↦blk [m] * r ~ML v}
  {∃m. r ↦ML m * () ~ML Val_unit}
}
```

VIEW RECONCILIATION (2)

$$\vec{V} \sim_{\text{ML}} \vec{v} * \gamma \mapsto_{\text{blk}} \vec{v} \equiv * \exists l . l \mapsto_{\text{ML}} \vec{V} * l \sim_{\text{ML}} \gamma$$

Verifying hash_ref with Melocoton

OCaml glue code

```
external hash_ref: int ref -> unit
  = "caml_hash_ref"

  { $r \mapsto_{ML} n$ }
  hash_ref(r)
  { $\exists m. r \mapsto_{ML} m$ }
```

C glue code

```
value caml_hash_ref(value v) {
  { $r \mapsto_{ML} n * r \sim_{ML} v$ }
  { $v \mapsto_{blk} [n] * r \sim_{ML} v$ }
  int x = Int_val(Field(v, 0));
  hash_ptr(&x);
  Store_field(v, 0, Val_int(x));
  return Val_unit;

  { $\exists m. v \mapsto_{blk} [m] * r \sim_{ML} v$ }
  { $\exists m. r \mapsto_{ML} m * () \sim_{ML} Val\_unit$ }
}
```

Field SPECIFICATION

$\{\gamma \mapsto_{blk} [\dots v_i \dots]\} \text{Field}(\gamma, i) \{\lambda v'. v' = v_i \wedge \gamma \mapsto_{blk} [\dots v_i \dots]\}$

Verifying hash_ref with Melocoton

OCaml glue code

```
external hash_ref: int ref -> unit
  = "caml_hash_ref"

  { $r \mapsto_{ML} n$ }
  hash_ref(r)
  { $\exists m. r \mapsto_{ML} m$ }
```

C glue code

```
value caml_hash_ref(value v) {
  { $r \mapsto_{ML} n * r \sim_{ML} v$ }
  { $v \mapsto_{blk} [n] * r \sim_{ML} v$ }
  int x = Int_val(Field(v, 0));
  hash_ptr(&x);
  Store_field(v, 0, Val_int(x));
  return Val_unit;

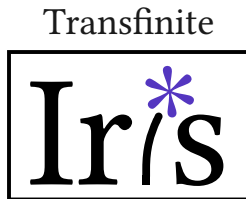
  { $\exists m. v \mapsto_{blk} [m] * r \sim_{ML} v$ }
  { $\exists m. r \mapsto_{ML} m * () \sim_{ML} Val\_unit$ }
}
```

Store_field SPECIFICATION

$\{\gamma \mapsto_{blk} [\dots v_i \dots]\} \text{Store_field}(\gamma, i, v') \{\gamma \mapsto_{blk} [\dots v' \dots]\}$

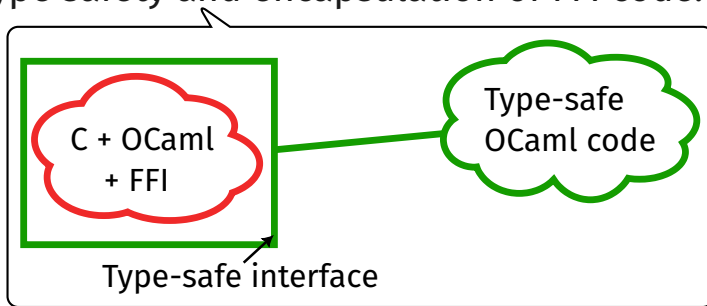
But wait, there is more!

- Language-local reasoning for **external calls**.
- Additional **OCaml FFI features**: garbage collection, registering roots, custom blocks, callbacks, etc.
- **Case studies** utilising all of these features.
- **Semantic model of OCaml types** (a logical relation) to verify type safety and encapsulation of FFI code.



But wait, there is more!

- Language-local reasoning for **external calls**.
- Additional **OCaml FFI features**: garbage collection, registering roots, custom blocks, callbacks, etc.
- **Case studies** utilising all of these features.
- **Semantic model of OCaml types** (a logical relation) to verify type safety and encapsulation of FFI code.



Extend Melocoton to model all of the OCaml FFI

exceptions, multithreading, “zero-copy” operations on byte arrays, ...

Build code-analysis tools based on Melocoton

Allow OCaml programmers to check correctness of their FFI glue code

Ideally, both verification and bug finding tools

Language Locality: Embed Existing Languages

OCaml Program Logic

λ_{ML+C} Program Logic

Glue Code Verification

C Program Logic

OCaml Semantics

λ_{ML+C} Semantics

Glue Code Semantics

C Semantics

Language Interaction: View Reconciliation Rules

$$\begin{aligned} l \mapsto_{ML} \vec{V} &\equiv \exists \gamma \vec{v}. \gamma \mapsto_{blk} \vec{v} * l \sim_{ML} \gamma * \vec{V} \sim_{ML} \vec{v} \\ \vec{V} \sim_{ML} \vec{v} * \gamma \mapsto_{blk} \vec{v} &\equiv \exists l. l \mapsto_{ML} \vec{V} * l \sim_{ML} \gamma \end{aligned}$$

<https://melocoton-project.github.io>