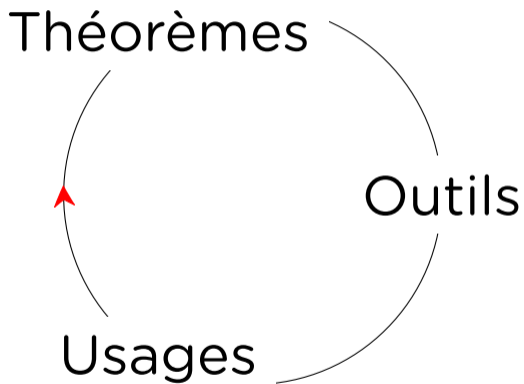


Équipe Analyse et Conception de Systèmes

Responsables : Pierre-Évariste Dagand (2021-2024)
Ralf Treinen (2017-2021)

7,2 permanents : 1 PR, 3,2 MC, 1,2 DR, 1,8 CR
1,7 ATER, 0 PostDoc, 5,8 Doc, 0,5 Émérites
Total : 16,2 membres

Thématiques et enjeux



Thématiques et enjeux

Logiciel d'infrastructure

- Protocole de routage Babel
- Projet CoLiS
- Community-coq

(verif)

(Juliusz Chroboczek)

(Ralf Treinen)

(Théo Zimmermann*)

Systemes concurrents

- Systeme de Markov concurrent
- Préordres de tests
- Réseaux booléens asynchrones

(algebre, verif)

(Samy Abbes)

(Giovanni Bernardi)

(Paul Ruet)

Thématiques et enjeux

Langages de programmation

(algèbre)

- Types ensemblistes
- Types gardés

(Giuseppe Castagna)
(Adrien Guatto)

Assistant de preuve Coq

(algèbre, preuves)

- Coq & MetaCoq
- Expressions régulières certifiées
- Interpolants uniformes certifiés

(Matthieu Sozeau*)
(Pierre Letouzey)
(Hugo Férée)

Thématiques et enjeux

Paradigmes émergents

(preuves)

- Ingénierie des preuves à grande échelle (Emilio J. Gallego)
- Réseaux d'interaction (Jean Krivine*)
- Programmes incrémentaux (Yann Régis-Gianas*)

Enseignement & Société

- Notes “Outils Logiques”¹, *etc.* (Roberto Amadio)
- Initiative de Recherche et Innovation sur le Logiciel Libre (Roberto Di Cosmo*)

1. <https://cel.hal.science/cel-00163821/>

Vie et organisation

Animation scientifique

- Séminaire pôle PPS
- Groupe de travail Programmation
- Séminaire IRILL

Évolution thématique

- Promotions : S. Zacchioli^(PU), T. Zimmerman^(MCF)
- Disponibilités : Y. Régis-Gianas^(MCF), J. Krivine^(CR)
- Départ : M. Sozeau^(CR)
- Arrivées : H. Férée^(MCF), A. Guatto^(MCF), P.-E. Dagand^(CR)
G. Baudart^(CR), G. Scherer^(CR), J. Krivine^(CR)

Projection

Programmes

- Conception de langages
- Programmation certifiée
- Documents mathématiques interactifs

Systèmes

- Systèmes concurrents
- Systèmes biologiques
- Protocole de routage Babel

Responsable : Jean Krivine (2024)

Besoins

Actualisation de la ligne scientifique

- Porteuse de sens collectif
- Attractivité nationale & internationale
- Positionnement GAFAM & start-up

Recrutement rang A

- Rééquilibrage : 5 rangs B / 7,2 permanents
- Actualisation scientifique
- Accompagnement rangs B

Scientific focus :
Concurrent probabilistic systems

Samy Abbes

Équipe ACS — Évaluation HCERES, 29 novembre 2023

Framework: the partial order semantics for concurrency

A stateless model

- ▶ An alphabet Σ of **actions**
- ▶ Some pairs of actions are declared **concurrent**

a and b are concurrent $\iff (a, b) \in I$

$I \subseteq \Sigma \times \Sigma$ I is symmetric and irreflexive

- ▶ **Executions** of the system are *words up to commutation of contiguous concurrent actions*

i.e., elements of the **trace monoid**: $\mathcal{M} = \Sigma^* / \mathcal{R}$

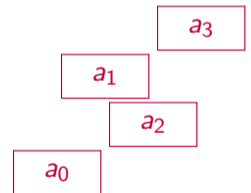
where \mathcal{R} is the congruence on Σ^* generated by I

Framework: the partial order semantics for concurrency

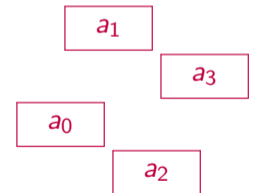
Example: the dimer model

$$\Sigma = \{a_0, \dots, a_3\} \quad (a_i, a_j) \in I \iff |i - j| > 1$$

word $a_0 a_2 a_1 a_3$



word $a_2 a_0 a_3 a_1$



trace

$$a_0 \cdot a_2 \cdot a_1 \cdot a_3 = a_2 \cdot a_0 \cdot a_3 \cdot a_1$$



Framework: the partial order semantics for concurrency

More realistic: state models

- ▶ Defined by the action of a trace monoid \mathcal{M} on a finite set X of states with an absorbing sink state \perp

$$X \times \mathcal{M} \rightarrow X \qquad (\alpha \cdot x) \cdot y = \alpha \cdot (x \cdot y) \qquad \perp \cdot x = \perp$$

- ▶ For each state $\alpha \in X$:

$$\mathcal{M}_\alpha = \{x \in \mathcal{M} : \alpha \cdot x \neq \perp\}$$

is the set of trajectories of the system starting from α

- ▶ **Example** : a bounded Petri with X as the set of markings and \mathcal{M} is generated by the transitions of the net

Probabilistic questions

General questions

- ▶ Are there natural probabilistic layers for concurrent trajectories of size n ?
- ▶ Are there natural probabilistic layers for infinite concurrent trajectories ?
 - ▶ What are the probabilistic parameters ?
 - ▶ What are the probabilistic properties ?
- ▶ For applications: is there a convergence of k -size layers for finite trajectories toward the probabilistic layer for infinite trajectories ?

Some answers

Stateless models: trace monoids

- ▶ **Without concurrency:** memoryless measures on infinite words with $|\Sigma| = n$ are parametrized by the $(n - 1)$ -dimensional simplex

$$\forall i \in \{1, \dots, n\} \quad p_i \geq 0 \qquad p_1 + \dots + p_n = 1$$

- ▶ **With concurrency:** memoryless measures on infinite traces with $|\Sigma| = n$ **do exist** and are parametrized by an algebraic closed surface of the following form

$$\forall i \in \{1, \dots, n\} \quad \underbrace{h_i(p_1, \dots, p_n)}_{\substack{\text{polynomial} \\ \text{of degree} < d}} \geq 0 \qquad \underbrace{h_0(p_1, \dots, p_n)}_{\substack{\text{polynomial} \\ \text{of degree } d}} = 0$$

where d is the highest concurrency degree of the monoid

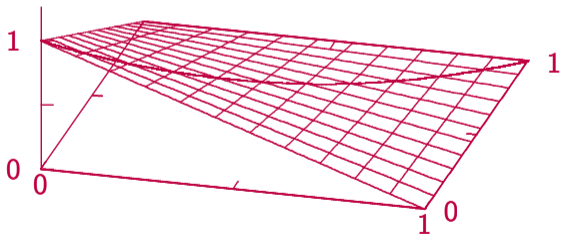
Some answers

Graphical representation of the probabilistic parameters in (p_0, p_1, p_2) -space for the 3-slots dimer model

$$\Sigma = \{a_0, a_1, a_2\}$$

$$a_0 a_2 = a_2 a_0$$

$$1 - p_0 - p_1 - p_2 + p_0 p_2 = 0$$



There is a **unique** solution where all parameters are equal, which defines the unique **uniform** measure on infinite traces

Some answers

Application: computing the average parallelism in a trace monoid

$$\begin{aligned}\tau(x) &= \text{concurrency rate of the finite trajectory } x \\ &= \frac{\text{minimal number of rounds to execute } x}{|x|}\end{aligned}$$

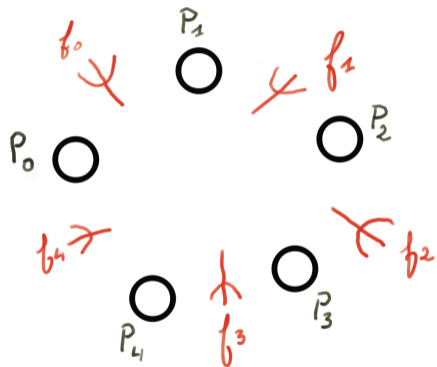
$$\tau_n(\mathcal{M}) = \text{average of } \tau_x \text{ for } x \in \mathcal{M} \text{ and } |x| = n$$

$$\tau_{\mathcal{M}} = \lim_{n \rightarrow +\infty} \tau_n(\mathcal{M})$$

Thanks to the **uniform measure**, $\tau_{\mathcal{M}}$ can be computed by an explicit formula depending on the coefficients of the Möbius polynomial of the monoid \mathcal{M} (number of concurrency cliques of size $0, 1, \dots$)

Some answers

The 5-philosophers/5-forks model: an example with states



In an endless play:

p = probability for philosopher P_0 to grab the two forks f_0 and f_4 and start eating

$$p = \frac{5 - \sqrt{5}}{10} \approx 0.2764 > 0.2$$

The randomization is **Markovian** rather than **memoryless**

Résumé synthétique

Équipe Analyse et Conception de Systèmes (ACS)

- 16,2 membres dont 7,2 permanents
- 1 groupe de travail régulier & séminaire PPS
- Projets structurants : ANR Asesyc, CoLiS, DCore, Rapido ; Inria Picube
- 29,67 articles de journaux (pro-rata)
- 40,5 articles de conférences (pro-rata)
- 67 publications communes avec PP
- 16 projets de logiciel libre
- 8,17 thèses (2 prix de thèse GDR GPL)
- Prix Science Ouverte du Logiciel Libre pour Coq
- Test of Time Award (Concur)