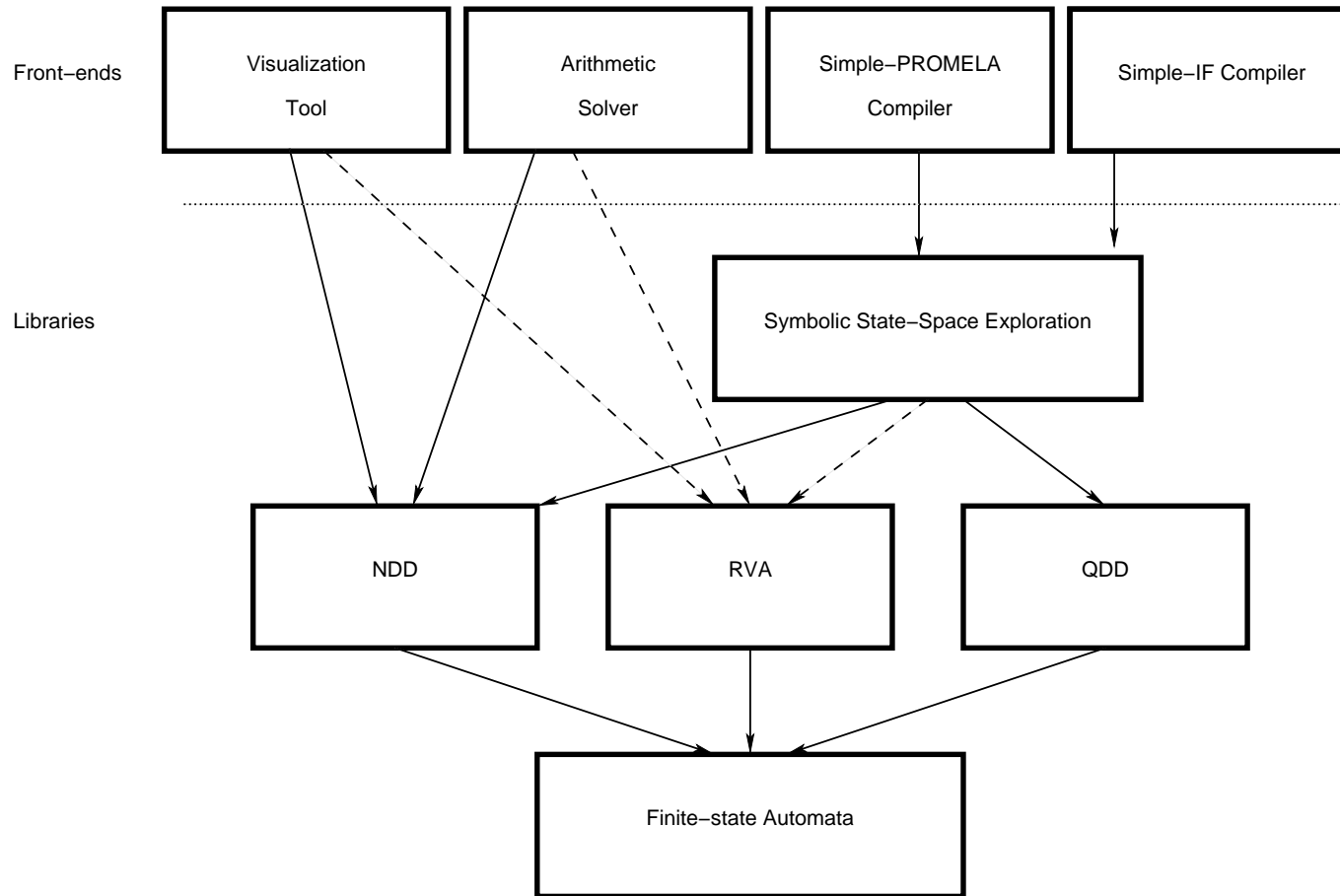


# PGM protocol: Experiments with LASH

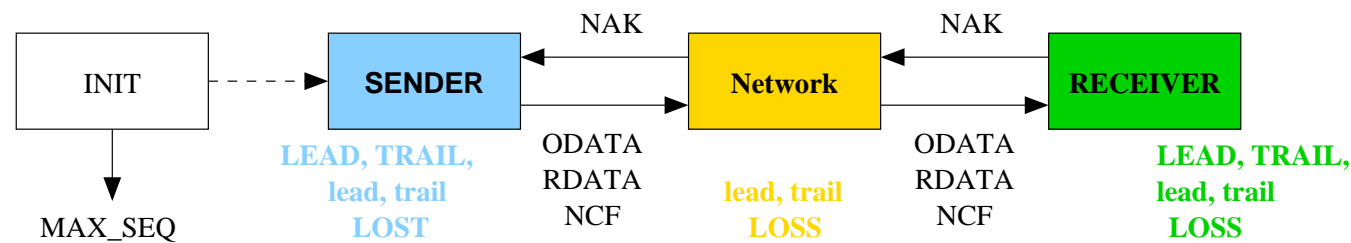
Louis Latour

Université de Liège

# 1. LASH toolkit



## 2. Protocol Model

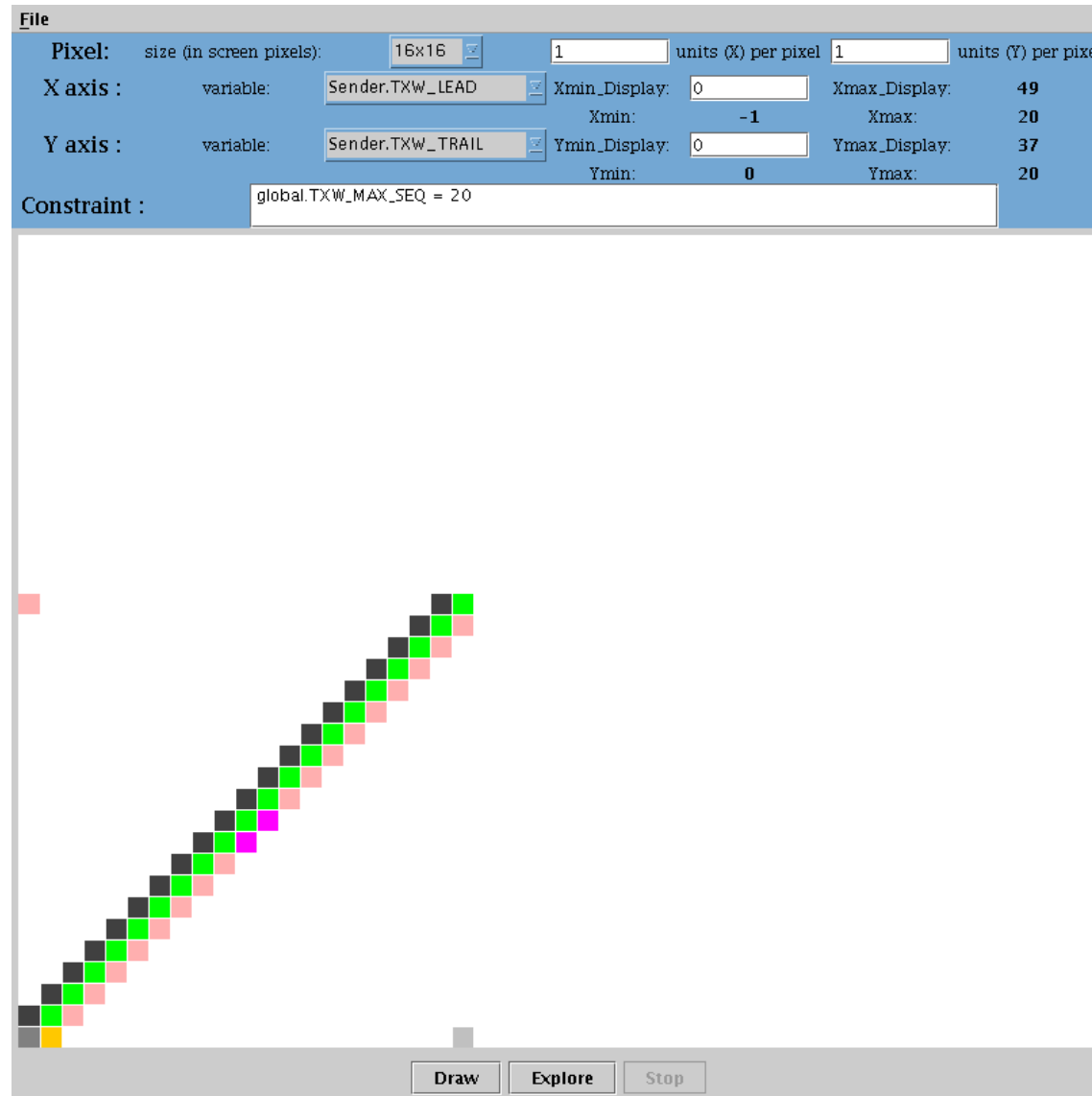


- Messages transferred through SYNCHRONIZATION
- 1 LOSS (at a given sequence number)
- NO SPMs
- NO signal, NO clock
- Sender Window size: variable but bounded, non-deterministic advance (TRAIL and LEAD)
- Receiver Window size: variable and unbounded, non-deterministic advance (TRAIL only)
- + Meta-transitions.

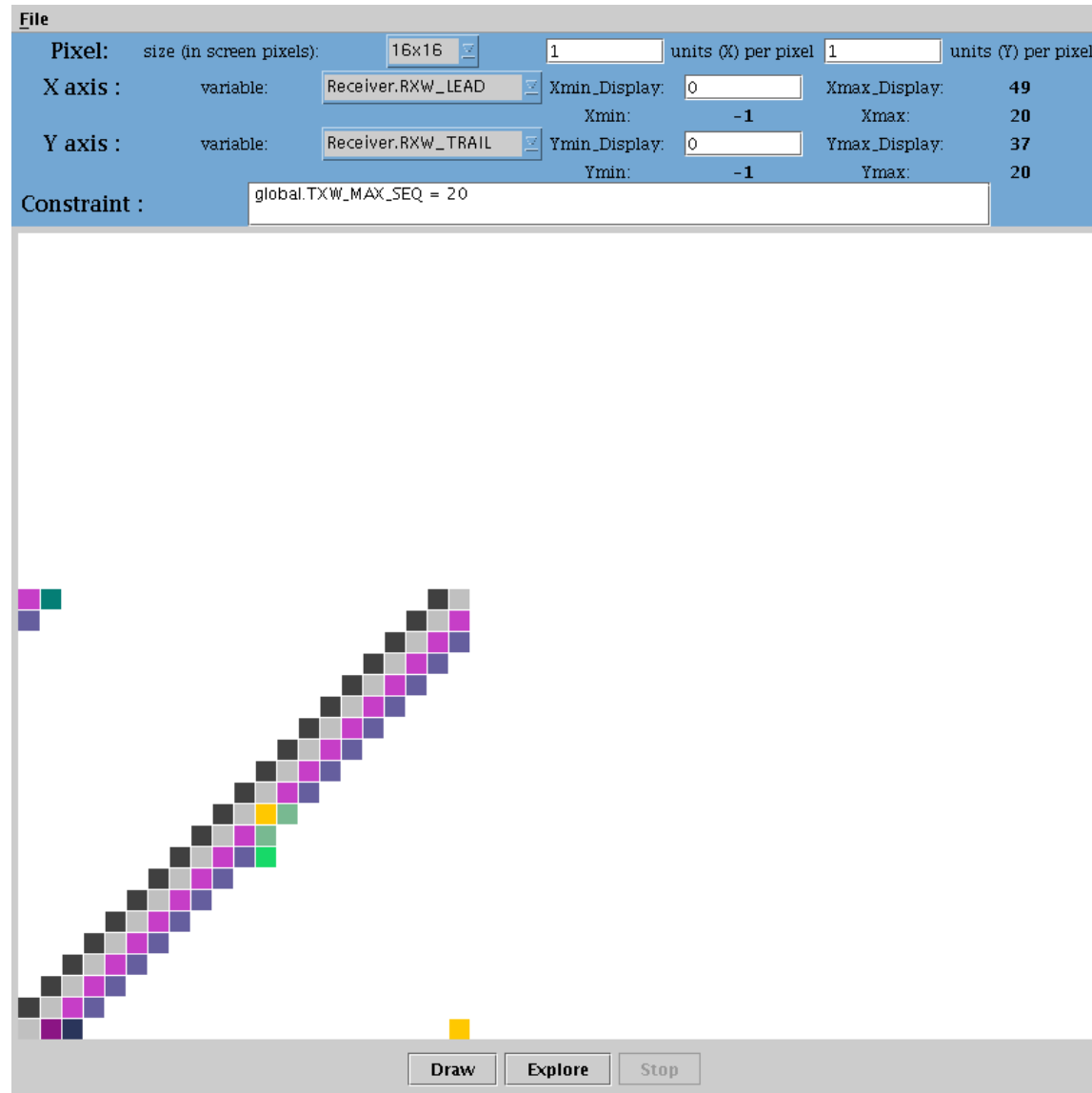
### 3. Verification Task

- Debugging the model
  - Impact of meta-transitions
  - Values of auxiliary variables
- Analysis Goals :
  - Relationships between variables
  - Is there a bound (mod `NO_MAX_SEQ`) on `LEAD - TRAIL` ?

# 4.a Analysis: SENDER (TRAIL vs LEAD) (**MAX\_SEQ = 20**)



## 4.b Analysis: RECEIVER (TRAIL vs LEAD) ( $\text{MAX\_SEQ} = 20$ )



## 4.c Analysis: SENDER (TRAIL vs LEAD) (**MAX\_SEQ = 20**)


**File**

Pixel: size (in screen pixels): 16x16 1 units (X) per pixel 1 units (Y) per pixel

X axis : variable: Sender.TXW\_LEAD Xmin\_Display: 0 Xmax\_Display: 49  
Xmin: 10 Xmax: 12

Y axis : variable: Sender.TXW\_TRAIL Ymin\_Display: 0 Ymax\_Display: 37  
Ymin: 10 Ymax: 13

Constraint : (global.TXW\_MAX\_SEQ = 20) and (Receiver.RXW\_LEAD = 11 and Receiver.RXW\_TRAIL = 8)



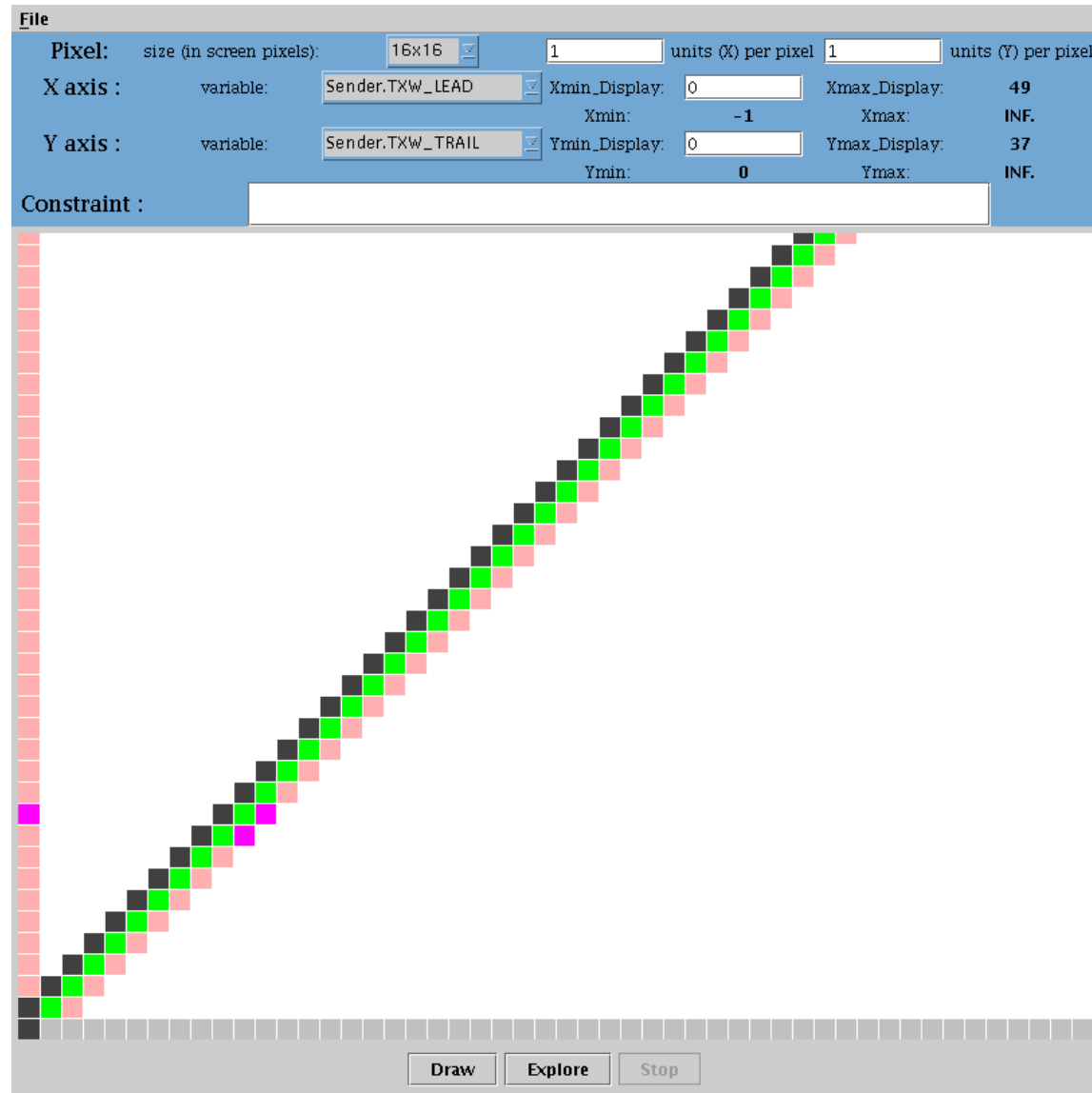
Draw Explore Stop

#### 4.d Analysis: Trace (manual)

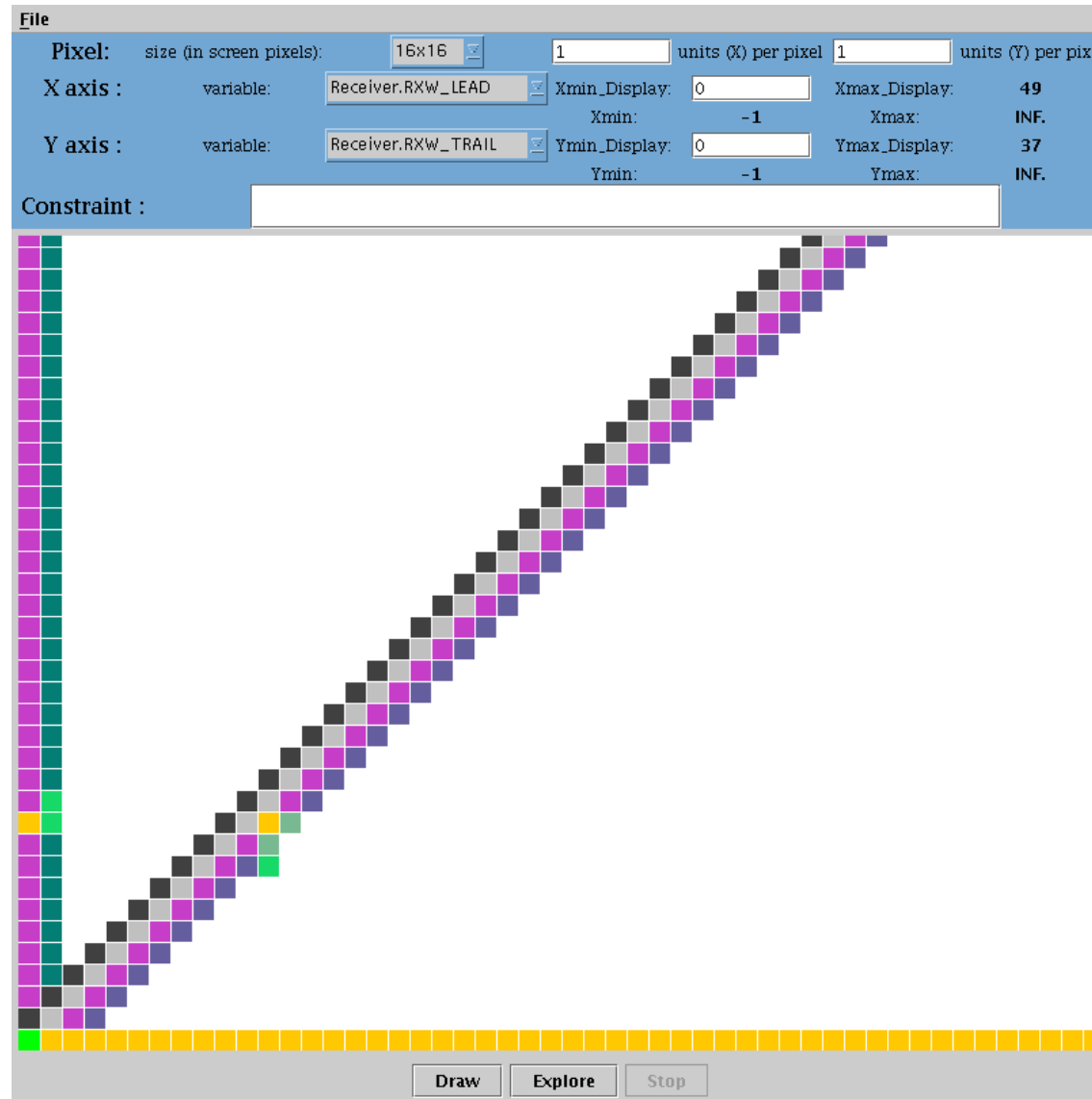
<b>ACTION</b>	<b>(Sender)</b> <b>(LEAD, TRAIL)</b>	<b>Network</b> <b>(lead, trail)</b>	<b>(Receiver)</b> <b>(LEAD, TRAIL)</b>
init	(7,8)	-	-
send	(7,8)	(8,8)	-
receive (a-b)	(7,8)	-	(8,8)
Sender.LEAD++	(8,8)	-	(8,8)
send	(8,8)	(9,8)	(8,8)
receive (a-b)	(8,8)	-	(9,8)
Sender.LEAD++	(9,8)	-	(9,8)
Sender.TRAIL++	(9,10)	-	(9,8)
loss	(9,10)	-	(9,8)
Sender.LEAD++	(10,10)	-	(9,8)
Sender.TRAIL++	(10,11)	-	(9,8)
send	(10,11)	(11,11)	(9,8)
receive (a)	(10,11)	-	(11,8)
Sender.LEAD++	(11,11)	-	(11,8)
Sender.TRAIL++	(11, 12)	-	(11,8)
send	(11, 12)	(12, 12)	(11,8)
Sender.LEAD++	(12, 12)	(12, 12)	(11,8)
Sender.TRAIL++	(12, 13)	(12, 12)	(11,8)
receive (b)	(12, 13)	(12, 12)	(11,11)



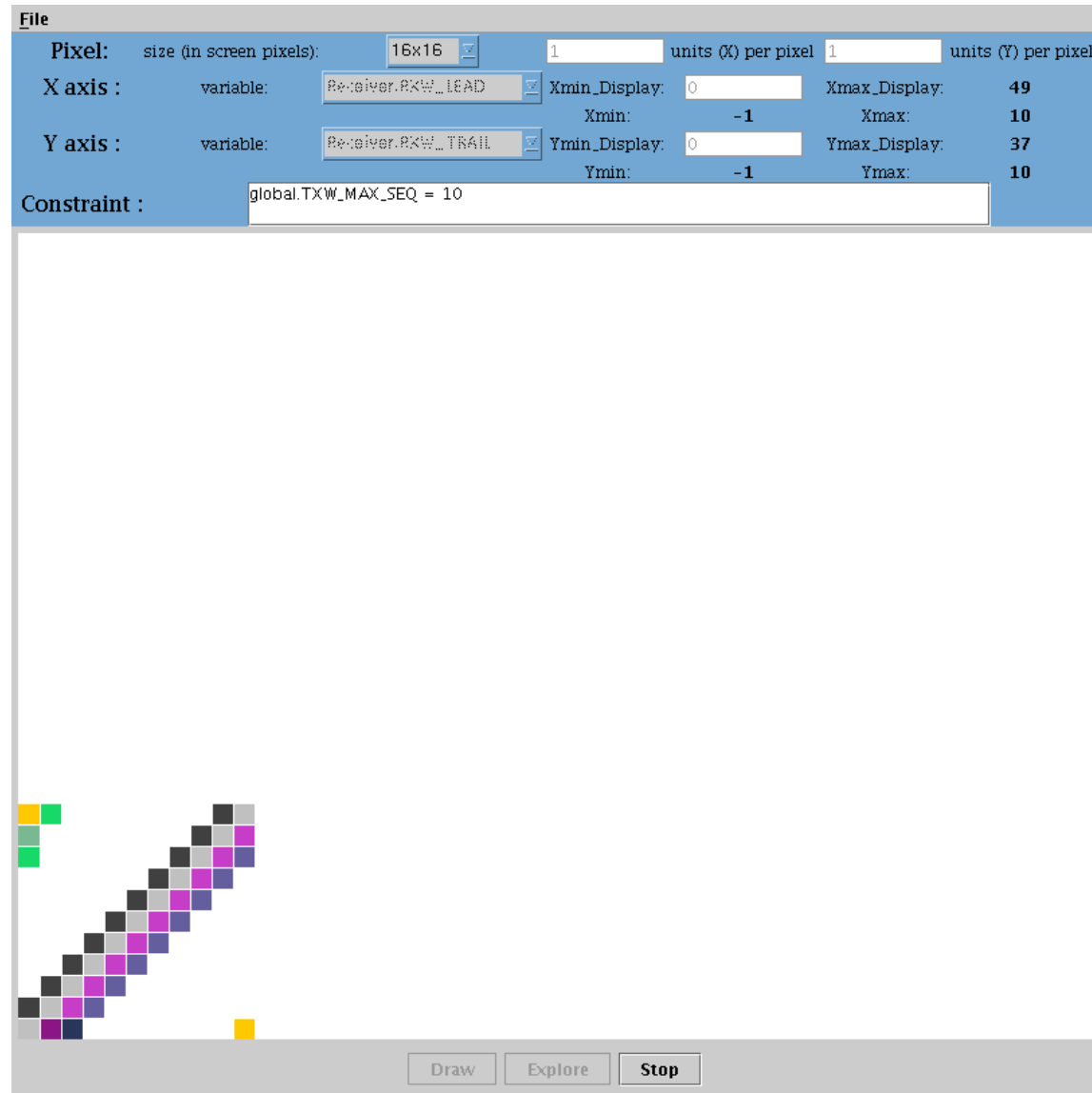
## 4.e Analysis: SENDER (TRAIL vs LEAD) (MAX\_SEQ = free )



#### 4.f Analysis: RECEIVER (TRAIL vs LEAD) (MAX\_SEQ = free )



## 4.g Analysis: RECEIVER (TRAIL vs LEAD) (**MAX\_SEQ = 10**)



## 5. Experimental Results (Window size = 2)

MAX_SEQ	Nb_steps	Max. Mem.	Nb. NDD States	Nb. States	Time
20	62	125 Mb	100 K	26 K	7h42
200	62	283 Mb	160 K	249 K	10h19
2000	62	467 Mb	219 K	2,479 K	17h09
20000	62	719 Mb	294 K	24,781 K	35h59
ND	76	279 Mb	225 K	INF.	23h52

## 6. Property

```
not (
  (Sender.LOST = 0 and
    ( ( Receiver.loop_LEAD = 0 and Receiver.loop_TRAIL = 0 and
        Receiver.RXW_LEAD - Receiver.RXW_TRAIL <= 2 and
        Receiver.RXW_LEAD - Receiver.RXW_TRAIL >= -1)
      or
      ( Receiver.loop_LEAD = 1 and
        Receiver.RXW_LEAD + global.TXW_MAX_SEQ - Receiver.RXW_TRAIL <= 2 and
        Receiver.RXW_LEAD + global.TXW_MAX_SEQ - Receiver.RXW_TRAIL >= -1)
      or
      ( Receiver.loop_TRAIL = 1 and
        Receiver.RXW_LEAD - global.TXW_MAX_SEQ - Receiver.RXW_TRAIL <= 2 and
        Receiver.RXW_LEAD - global.TXW_MAX_SEQ - Receiver.RXW_TRAIL >= -1)))
    or
    (Sender.LOST = 1 and
      ( ( Receiver.loop_LEAD = 0 and Receiver.loop_TRAIL = 0 and
          Receiver.RXW_LEAD - Receiver.RXW_TRAIL <= 3 and
          Receiver.RXW_LEAD - Receiver.RXW_TRAIL >= -1)
        or
        ( Receiver.loop_LEAD = 1 and
          Receiver.RXW_LEAD + global.TXW_MAX_SEQ - Receiver.RXW_TRAIL <= 3 and
          Receiver.RXW_LEAD + global.TXW_MAX_SEQ - Receiver.RXW_TRAIL >= -1)
        or
        ( Receiver.loop_TRAIL = 1 and
          Receiver.RXW_LEAD - global.TXW_MAX_SEQ - Receiver.RXW_TRAIL <= 3 and
          Receiver.RXW_LEAD - global.TXW_MAX_SEQ - Receiver.RXW_TRAIL >= -1))))
```

## 7. Conclusion

- **Exact reachability analysis of a PGM model with a parametric value of MAX\_SEQ.**
- Visualization tool gives essential feedback on the model behavior.
- **Slow . . .** but once !

## 8. Future Work

- Incorporate Reals.
- Increase efficiency (better representation, better algorithm, heuristics).
- Add tracing features.