Jerzy Trzeciak

Revised edition

Writing Mathematical Papers in English

a practical guide



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PREFACE

The booklet is intended to provide practical help for authors of mathematical papers. It is written mainly for non-English speaking writers but should prove useful even to native speakers of English who are beginning their mathematical writing and may not yet have developed a command of the structure of mathematical discourse.

The booklet is oriented mainly to research mathematics but applies to almost all mathematics writing, except more elementary texts where good teaching praxis typically favours substantial repetition and redundancy.

There is no intention whatsoever to impose any uniformity of mathematical style. Quite the contrary, the aim is to encourage prospective authors to write structurally correct manuscripts as expressively and flexibly as possible, but without compromising certain basic and universal rules.

The first part provides a collection of ready-made sentences and expressions that most commonly occur in mathematical papers. The examples are divided into sections according to their use (in introductions, definitions, theorems, proofs, comments, references to the literature, acknowledgements, editorial correspondence and referees' reports). Typical errors are also pointed out.

The second part concerns selected problems of English grammar and usage, most often encountered by mathematical writers. Just as in the first part, an abundance of examples are presented, all of them taken from actual mathematical texts.

The author is grateful to Edwin F. Beschler, Daniel Davies, Zofia Denkowska, Zbigniew Lipecki and Zdzisław Skupień for their helpful criticism. Thanks are also due to Adam Mysior and Marcin Adamski for suggesting several improvements, and to Henryka Walas for her painstaking job of typesetting the continuously varying manuscript.

Jerzy Trzeciak

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Part B: Selected Problems of English Grammar

Indefinite article (a, an, —)
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Number, quantity, size
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Word order
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ABSTRACT AND INTRODUCTION

We prove that in some families of compact there are no universal elements. It is also shown that

Some relevant counterexamples are indicated.

It is of interest to know whether	We wish to investigate
We are interested in finding	Our purpose is to
It is natural to try to relate to	

This work was intended as an attempt to motivate $\langle at motivating \rangle$ The aim of this paper is to bring together two areas in which

$\begin{array}{c c} In & Section \ 3 \\ the third section \\ [Note: paragraph \\ \neq section] \end{array}$		we	<pre>review some of the standard facts on have compiled some basic facts summarize without proofs the relevant material on give a brief exposition of briefly sketch set up notation and terminology. discuss (study/treat/examine) the case introduce the notion of develop the theory of</pre>
		we it is som r som our	 develop the theory of will look more closely at will be concerned with proceed with the study of indicate how these techniques may be used to extend the results of to derive an interesting formula for s shown that ne of the recent results are reviewed in a more general setting. ne applications are indicated. main results are stated and proved.
Section 4	contains a brief summary (a discussion) of deals with (discusses) the case is intended to motivate our investigation of is devoted to the study of provides a detailed exposition of establishes the relation between presents some preliminaries.		
We will touch only a few aspects of the theory. restrict our attention (the discussion/ourselves) to			

It is not our purpose to study

No attempt has been made here to develop It is possible that but we will not develop this point here. A more complete theory may be obtained by

However, this topic exceeds the scope of this paper. we will not use this fact in any essential way.

The basic $\langle \text{main} \rangle$ idea is to apply geometric ingredient is Our proof involves looking at The proof is based on the concept of adapted from This idea goes back at least as far as [7].

We emphasize that

It is worth pointing out that

The important point to note here is the form of

The advantage of using lies in the fact that

The estimate we obtain in the course of proof seems to be of independent interest.

Our theorem provides a natural and intrinsic characterization of

Our proof makes no appeal to

Our viewpoint sheds some new light on

Our example demonstrates rather strikingly that

The choice of seems to be the best adapted to our theory.

The problem is that

The main difficulty in carrying out this construction is that In this case the method of breaks down.

The this case the method of breaks dow

This class is not well adapted to

Pointwise convergence presents a more delicate problem.

The results of this paper were announced without proofs in [8].

The detailed proofs will appear in [8] $\langle elsewhere/in a forthcoming publication \rangle$.

For the proofs we refer the reader to [6].

It is to be expected that

One may conjecture that

One may ask whether this is still true if

One question still unanswered is whether

The affirmative solution would allow one to

It would be desirable to but we have not been able to do this.

These results are far from being conclusive.

This question is at present far from being solved.

Our method has the disadvantage of not being intrinsic. The solution falls short of providing an explicit formula. What is still lacking is an explicit description of

As for prerequisites, the reader is expected to be familiar with The first two chapters of constitute sufficient preparation.

- No preliminary knowledge of is required.
- To facilitate access to the individual topics, the chapters are rendered as self-contained as possible.
- For the convenience of the reader we repeat the relevant material from [7] without proofs, thus making our exposition self-contained.

DEFINITION

A set S is *dense* if

A set S is called (said to be) dense if \dots

We call a set *dense* (We say that a set is *dense*) if \dots

We call *m* the *product measure*. [Note the word order after "we call".]

The function f is given $\langle \text{defined} \rangle$ by $f = \dots$ Let f be given (defined) by $f = \dots$ We define T to be AB + CD.

The *length* of a sequence is, by definition, the number of The *length* of T, denoted by l(T), is defined to be By the *length* of T we mean

Define $\langle \text{Let/Set} \rangle E = Lf$, where $\begin{vmatrix} f & \text{is} \\ \text{we have set } f = \dots, \\ f & \text{being the solution of} \\ \text{with } f & \text{satisfying} \end{vmatrix}$

We will consider the behaviour of the family g defined as follows. the height of g (to be defined later) and

To measure the growth of q we make the following definition.

In this way we obtain what $\begin{vmatrix} \text{we shall call} \\ \text{will be referred to as} \\ \text{is known as} \end{vmatrix}$ the *P*-system.

Since, the norm of f is well defined. the definition of the norm is unambiguous (makes sense).

It is immaterial which M we choose to define F as long as M contains x. This product is independent of which member of g we choose to define it. It is Proposition 8 that makes this definition allowable.

Our definition agreeswith the one given in [7] if u isNote thatthis coincides with our previously introduced
terminology if K is convex.
this is in agreement with [7] for

NOTATION

We will denote by ZLet us denote by Z the set Write $\langle \text{Let/Set} \rangle f =$ [Not: "Denote f ="] The closure of A will be denoted by clA. We will use the symbol (letter) k to denote We write H for the value of We will write the negation of p as $\neg p$. The notation aRb means that Such cycles are called homologous (written $c \sim c'$). Here Here and subsequently, Throughout the proof, In what follows, $K \begin{vmatrix} \text{denotes} \\ \text{stands for} \end{vmatrix}$ the map From now on, We follow the notation of [8] (used in [8]). Our notation differs (is slightly different) from that of [8]. Let us introduce the temporary notation Ff for qfq. With the notation $f = \dots$, With this notation, In the notation of [8, Ch. 7] we have \dots . If f is real, it is customary to write rather than we write f instead of use the same letter f for continue to write f for let f stand for For simplicity of notation, To $\langle \text{simplify/shorten} \rangle$ notation, By abuse of notation, For abbreviation, We abbreviate Faub to b'. We denote it briefly by *F*. [*Not*: "shortly"] We write it F for short (for brevity). [Not: "in short"] The Radon–Nikodym property (RNP for short) implies that We will write it simply x when no confusion can arise.

It will cause no confusion if we use the same letter to designate a member of A and its restriction to K.

We shall write the above expression as The above expression may be written as $t = \dots$. We can write (4) in the form

The Greek indices label components of sections of E.

Print terminology:

The expression in italics (in italic type), in large type, in bold print; in parentheses () (= round brackets), in brackets [] (= square brackets), in brackets [] (= square brackets),

in braces { } (= curly brackets), in angular brackets $\langle \rangle$; within the norm signs

- Capital letters = upper case letters; small letters = lower case letters; Gothic $\langle German \rangle$ letters; script $\langle calligraphic \rangle$ letters (e.g. \mathcal{F}, \mathcal{G}); special Roman $\langle blackboard \ bold \rangle$ letters (e.g. \mathbb{R}, \mathbb{N})
- Dot , prime ', asterisk = star *, tilde ~, bar [over a symbol], hat ^, vertical stroke (vertical bar) |, slash (diagonal stroke/slant) /, dash —, sharp #

Dotted line, dashed line ____, wavy line _____

PROPERTY

The $\langle An \rangle$ element	such that (with the property that) [Not: "such an element that"] with the following properties: satisfying $Lf =$ with $Nf = 1$ (with coordinates x, y, z) of norm 1 (of the form) whose norm is all of whose subsets are by means of which g can be computed for which this is true at which g has a local maximum described by the equations given by $Lf =$ depending only on (independent of not in A so small that (small enough that) as above (as in the previous theorem) so obtained occurring in the cone condition [Note the double "r".] guaranteed by the assumption	>
----------------------------------	--	---

The $\langle An \rangle$ eleme	we have just defined we wish to study (we used in Chapter 7) to be defined later $[=$ which will be defined] in question under study (consideration)			
, the constant C being independent of [= where C is] , the supremum being taken over all cubes , the limit being taken in L .				
, where $C \begin{vmatrix} i \\ i \\ i \\ i \\ r \\ r \\ r \\ r \end{vmatrix}$	s so chosen that s to be chosen later. s a suitable constant. s a conveniently chosen element of nvolves the derivatives of ranges over all subsets of nay be made arbitrarily small by			
The operators A_i are	⟨share⟩ many of the properties of still better smoothness properties. ⟨fail to have⟩ the smoothness properties of have norm 1. not merely symmetric but actually self-adjoint. not necessarily monotone. both symmetric and positive-definite. not continuous, nor do they satisfy (2). [Note the inverse word order after "nor".] neither symmetric nor positive-definite. only nonnegative rather than strictly positive, as one may have expected. any self-adjoint operators, possibly even unbounded. still ⟨no longer⟩ self-adjoint. not too far from being self-adjoint.			
The preceding theorem indicated set [But adjectival clauses with above-mentioned group prepositions come <i>after</i> a noun, resulting region e.g. "the group defined in Section 1".]				
Both X and Y are finit Neither X nor Y is finit Both X and Y are cour Neither of them is finite None of the functions F	e. te. ntable, but neither is finite. e. [<i>Note</i> : "Neither" refers to <i>two</i> alternatives.] F_i is finite.			

The set X is not finite; nor $\langle \text{neither} \rangle$ is Y.

Note that X is not finite, nor is Y countable. [Note the inversion.]

We conclude that X is empty $\begin{vmatrix} \text{; so also is } Y \\ \text{, but } Y \text{ is not.} \end{vmatrix}$

Hence X belongs to $Y \mid$, and so does Z. , but Z does not.

ASSUMPTION, CONDITION, CONVENTION

We will make $\langle need \rangle$ the following assumptions: From now on we make the assumption: The following assumption will be needed throughout the paper. Our basic assumption is the following. Unless otherwise stated $\langle Until further notice \rangle$ we assume that In the remainder of this section we assume $\langle require \rangle g$ to be In order to get asymptotic results, it is necessary to put some restrictions on f. We shall make two standing assumptions on the maps under consideration.

It is required (assumed) that

The requirement on g is that

, where g is subject to the condition $Lg = 0$. satisfies the condition $Lg = 0$. is merely required to be positive.				
Let us orient M	thy the re	The requirement that g be positive. [Note the infinitive.] quiring g to be aposing the condition:		
Now, (4) holds $\begin{bmatrix} \text{for } \langle \mathbf{j} \\ \text{unles} \end{bmatrix}$		$\begin{array}{l} \mbox{rovided/whenever/only in case} \ p \neq 1.\\ p = 1.\\ \mbox{the condition (hypothesis) that}\\ \mbox{the more general assumption that}\\ \mbox{some further restrictions on}\\ \mbox{additional (weaker) assumptions.} \end{array}$		
satisfies (fai has the desi provides the still satisfies meets this of does not ne satisfies all	satisfies $\langle \text{fails to satisfy} \rangle$ the assumptions of has the desired $\langle \text{asserted} \rangle$ properties. provides the desired diffeomorphism. still satisfies $\langle \text{need not satisfy} \rangle$ the requirement that meets this condition. does not necessarily have this property. satisfies all the other conditions for membership of X.			

There is no loss of generality in assuming Without loss (restriction) of generality we can assume This involves no loss of generality.

We can certainly assume that	, since otherwise, for[= because], for if not, we replace Indeed,
------------------------------	---

Neither the hypothesis nor the conclusion is affected if we replace By choosing b = a we may actually assume that

If f = 1, which we may assume, then

For simplicity (convenience) we ignore the dependence of F on g.

[E.g. in notation]

It is convenient to choose

We can assume, by decreasing k if necessary, that

Thus F meets S transversally, say at F(0). There exists a minimal element, say n, of F. Hence G acts on H as a multiple (say n) of V. For definiteness $\langle To \text{ be specific} \rangle$, consider

This condition	is not particularly restrictive. is surprisingly mild. admits (rules out/excludes) elements of is essential to the proof. cannot be weakened (relaxed/improved/omitted/ dropped).
----------------	--

The theorem is true if "open" is deleted from the hypotheses. The assumption is superfluous (redundant/unnecessarily restrictive). We will now show how to dispense with the assumption on Our lemma does not involve any assumptions about curvature.

We have been working under the assumption that

Now suppose that this is no longer so.

To study the general case, take

For the general case, set

The map f will be viewed (regarded/thought of) as a functor realizing

From now on we think of L as being constant. regard f as a map from tacitly assume that

It is understood that $r \neq 1$.

We adopt (adhere to) the convention that 0/0=0.

THEOREM: GENERAL REMARKS

an extension (a fairly straightforward generalization/a sharpened version/ a refinement) of \ldots an analogue of is a reformulation (restatement) of in terms of analogous to This theorem a partial converse of an answer to a question raised by deals with ensures the existence of expresses the equivalence of provides a criterion for yields information about makes it legitimate to apply The theorem states $\langle asserts/shows \rangle$ that Roughly (Loosely) speaking, the formula says that When f is open, (3.7) just amounts to the fact that to the fact that Here is another way of stating (c): Another way of stating (c) is to say: An equivalent formulation of (c) is: Theorems 2 and 3 may be summarized by saying that Assertion (ii) is nothing but the statement that Geometrically speaking, the hypothesis is that; part of the conclusion is that The interest The interest The principal significance of the lemma is in the assertion The point The point The theorem gains in interest if we realize that The theorem is still true still holds if we drop the assumption it is just assumed that If we take $f = \dots$. Replacing f by -f, we recover the standard lemma \dots . This specializes to the result of [7] if f = q. This result will be needed in prove extremely useful in Section 8. not be needed until

THEOREM: INTRODUCTORY PHRASE

We have thus proved Summarizing, we have We can now rephrase Theorem 8 as follows. state the analogue of formulate our main results.

> We are thus led to the following strengthening of Theorem 6: The remainder of this section will be devoted to the proof of

The continuity of A is established by our next theorem.

The following result may be proved in much the same way as Theorem 6. Here are some elementary properties of these concepts.

Let us mention two important consequences of the theorem.

We begin with a general result on such operators.

[*Note*: Sentences of the type "We now have the following lemma", carrying no information, can in general be cancelled.]

THEOREM: FORMULATION

If and if, then Let M be Suppose that Assume that Then, Then, provided $m \neq 1$. unless m = 1. with g a constant satisfying Furthermore (Moreover), In fact, \dots [= To be more precise] Accordingly, \dots [= Thus] Given any $f \neq 1$ suppose that Then Let P satisfy the hypotheses of the above assumptions. Then N(P) = 1.Let assumptions 1–5 hold. Then Under the above assumptions, Under the same hypotheses, Under the conditions stated above, Under the assumptions of Theorem 2 with "convergent" replaced by "weakly convergent", Under the hypotheses of Theorem 5, if moreover Equality holds in (8) if and only if The following conditions are equivalent:

[*Note*: Expressions like "the following inequality holds" can in general be dropped.]

PROOF: BEGINNING

We first first // fir				
Let us outline (give the main ideas of) the proof. examine Bf .				
But $A = B$. To see $\langle \text{prove} \rangle$ this, let $f = \dots$. We prove this as follows. This is proved by writing $g = \dots$.				
We first compute If . To this end, consider [= For this purpose; <i>not</i> : "To this aim"] To do this, take For this purpose, we set				
To deduce (3) from (2), take We claim that Indeed, We begin by proving $\langle by$ recalling the notion of \rangle				
Our proof starts with the observation that The procedure is to find The proof consists in the construction of				
The proof is $\begin{vmatrix} \text{straightforward } \langle \text{quite involved} \rangle \\ \text{by induction on } n. \\ \text{left to the reader.} \\ \text{based on the following observation.} \end{vmatrix}$				
The main $\langle basic \rangle$ idea of the proof is to take				
The proof falls naturally into three parts. will be divided into three steps.				
We have divided the proof into a sequence of lemmas.				
Suppose the assertion of the lemma is false.				
Conversely $\langle To obtain a contradiction \rangle$, suppose that				
Suppose the lemma were false. Then we could find				

If	there existed an x , x were not in B , it were true that,	we would have there would be
----	---	---------------------------------

Assume the formula holds for degree k; we will prove it for k + 1. Assuming (5) to hold for k, we will prove it for k + 1.

We give the proof only for the case n = 3; the other cases are left to the reader.

We give only the main ideas of the proof.

PROOF: ARGUMENTS

Bv	definition, the definition of assumption, the compactness of Taylor's formula	But $f = f$	$g \left \begin{array}{c} , \mbox{ which follows from} \\ \mbox{ as was described} \\ \mbox{ (shown/mentioned/ noted) in} \end{array} \right.$	
23	a similar argument, the above, the lemma below, continuity,	Theorem 4 nov	$ \begin{cases} \text{shows that} \\ \text{yields } \langle \text{gives} / \\ \text{implies} \rangle f = \\ \text{leads to } f = \end{cases} $	
	Since f is compact,	Lf = 0. [Not: we have $Lf = 0$ it follows that we see $\langle \text{conclust} \rangle$	"Since, then"] D. Lf = 0. Lf = 0. Lf = 0.	
But $Lf = 0$ since f is compact. We have $Lf = 0$, because [+ a longer explanation] We must have $Lf = 0$, for otherwise we can replace As f is compact we have $Lf = 0$. Therefore $Lf = 0$ by Theorem 6. That $Lf = 0$ follows from Theorem 6.				
	From $\begin{cases} \text{this} \\ (5) \\ \text{what has alress been proven} \end{cases}$	ady ed, we conclu we have ([<i>Note</i> : it follows it may be	de $\langle \text{deduce/see} \rangle$ that obtain $\rangle M = N$. without "that"] that concluded that	
Acco	ording to $\langle On account of \rangle$	\rangle the above rem	hark, we have $M = N$.	
It follows that Hence $\langle \text{Thus/Consequently,/Therefore} \rangle M = N.$				
[hence = from this; thus = in this way; therefore = for this reason; it follows that = from the above it follows that]				
This We f The Now This	gives $M=N$. thus get $M=N$. result is $M=N$. (3) becomes $M=N$. clearly forces $M=N$.	t is compact,	and so $M = N$. and consequently $M = N$. and, in consequence, $M = N$. and hence bounded. which gives $\langle \text{implies} / \\ \text{yields} \rangle M = N$. [Not: "what gives"]	
Now $F = G = H$, the last equality being a consequence of Theorem 7. which is due to the fact that				

Since, (2) shows that, by (4). We conclude from (5) that, hence that, and finally that The equality f = g, which is part of the conclusion of Theorem 7, implies that

As in the proof of Theorem 8, equation (4) gives

Analysis similar to that in the proof of Theorem 5 shows that [Not: "similar as in"]

A passage to the limit similar to the above implies that Similarly $\langle Likewise \rangle$,

Similar arguments apply The same reasoning applies to the case

The same conclusion can be drawn for

This follows by the same method as in

The term Tf can be handled in much the same way, the only difference being in the analysis of

In the same manner we can see that

The rest of the proof runs as before.

We now apply this argument again, with I replaced by J, to obtain

PROOF: CONSECUTIVE STEPS

				evaluate
Consider	Define			compute
Choose	Let	$f = \dots$	Let us	apply the formula to
Fix	Set	°		suppose for the moment
				regard s as fixed and

[*Note*: The imperative mood is used when you *order* the reader to do something, so you should not write e.g. "Give an example of" if you mean "*We* give an example of"]

Adding g to the left-hand side	
Subtracting (3) from (5)	
Writing $\langle \text{Taking} \rangle h = Hf$ Substituting (4) into (6) Combining (3) with (6)	yields $\langle \text{gives} \rangle h = \dots$ we obtain $\langle \text{get/have} \rangle f = g$
Combining these [E.g. these inequalities]	we conclude (deduce/see) that
Replacing (2) by (3)	we can assert that \dots
Letting $n \to \infty$	we can rewrite (J) as
Applying (5)	
Interchanging f and g	

[*Note*: The ing-form is either the subject of a sentence ("Adding gives"), or requires the subject "we" ("Adding we obtain"); so do *not* write e.g. "Adding the proof is complete."]

We continue in this fashion obtaining $\langle \text{to obtain} \rangle f = \dots$. We may now integrate k times to conclude that Repeated application of Lemma 6 enables us to write We now proceed by induction.

We can now proceed analogously to the proof of

We next $\begin{vmatrix} \text{claim } \langle \text{show/prove that} \rangle \dots \\ \text{sharpen these results and prove that } \dots \end{vmatrix}$

Our next $\begin{cases} \text{claim is that} \\ \text{goal is to determine the number of} \\ \text{objective is to evaluate the integral } I. \\ \text{concern will be the behaviour of} \end{cases}$

We now turn to the case $f \neq 1$.

We are now in a position to show \dots [= We are able to]

We proceed to show that

The task is now to find

Having disposed of this preliminary step, we can now return to

We wish to arrange that f be as smooth as possible. [Note the infinitive.] We are thus looking for the family We have to construct

In order to get this inequality, it will be necessary to is convenient to

To deal with If, To estimate the other term, we note that For the general case,

PROOF: "IT IS SUFFICIENT TO"

It suffices $|_{\text{is sufficient}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{to}}|_{\text{$

We need only consider three cases: We only need to show that

It remains to prove that $\langle \text{to exclude the case when} \rangle$ What is left is to show that We are reduced to proving (4) for We are left with the task of determining The only point remaining concerns the behaviour of The proof is completed by showing that We shall have established the lemma if we prove the following: If we prove that, the assertion follows. The statement O(g)=1 will be proved once we prove the lemma below.

PROOF: "IT IS EASILY SEEN THAT"

It is $\begin{vmatrix} \text{clear} & \langle \text{evident/immediate/obvious} \rangle \text{ that } \dots \\ \text{easily seen that } \dots \\ \text{easy to check that } \dots \\ \text{a simple matter to } \dots \end{vmatrix}$

We see $\langle check \rangle$ at once that They are easily seen to be smooth., which is clear from (3)., as is easy to check.

It follows easily (immediately) that Of course (Clearly/Obviously), The proof is straightforward (standard/immediate).

An easy computation $\langle A \text{ trivial verification} \rangle$ shows that

(2) makes it obvious that \dots [= By (2) it is obvious that]

The factor Gf poses no problem because G is

PROOF: CONCLUSION AND REMARKS

, which [<i>Not</i> : "what"] This	proves the theorem. completes the proof. establishes the formula. is the desired conclusion. is our claim $\langle assertion \rangle$. [Not: "thesis"] gives (4) when substituted in (5) $\langle combined with (5) \rangle$.
, an	the proof is complete. this is precisely the assertion of the lemma. the lemma follows. (3) is proved. f = g as claimed (required).
This controdict	a our assumption /the fact that

This contradicts our assumption \langle the fact that \rangle, contrary to (3).

...., which is impossible. [Not: "what is"]

...., which contradicts the maximality of

...., a contradiction.

The proof for G is similar. The map G may be handled in much the same way. Similar considerations apply to G.

The same proof | works $\langle \text{remains valid} \rangle$ for obtains $\langle \text{fails} \rangle$ when we drop the assumption

The method of proof carries over to domains

The proof above gives more, namely f is A slight change in the proof actually shows that Note that we have actually proved that

[= We have proved more, namely that]

We have used only the fact that the existence of only the right-hand derivative.

For f=1 it is no longer true that the argument breaks down.

The proof strongly depended on the assumption that

Note that we did not really have to use; we could have applied

For more details we refer the reader to [7].

The details are left to the reader.

We leave it to the reader to verify that [Note: the "it" is necessary] This finishes the proof, the detailed verification of (4) being left to the reader.

REFERENCES TO THE LITERATURE

(see for instance [7, Th. 1]) (see [7] and the references given there) (see [Ka2] for more details) the definition of) the complete bibliography) The best general reference here The standard work on Is This was proved by Lax [8]. The classical work here Lax [7, Ch. 2].

This construction	is due to Strang [8]. goes back to the work of as far as [8]. was motivated by [7]. generalizes that of [7]. follows [7]. is adapted from [7] (appears in [7]).
	has previously been used by Lax [7].

For	a recent account of the theory a treatment of a more general case a fuller (thorough) treatment a deeper discussion of direct constructions along more classical lines yet another method	we refer the reader to [7].
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We introduce the notion of, following Kato [7]. We follow [Ka] in assuming that

The main results of this paper were announced in [7].

Similar results have been obtained independently by Lax and are to be published in [7].

ACKNOWLEDGMENTS

The author wishes to express his thanks $\langle \text{gratitude} \rangle$ to is greatly indebted to

his active interest in the publication of this paper. suggesting the problem and for many stimulating conversations. for drawing the author's attraction in the surface of the surface of

- drawing the author's attention to pointing out a mistake in his collaboration in proving Lemma 4.
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- The author wishes to thank the University of, where the paper was written, for financial support \langle for the invitation and hospitality \rangle .

HOW TO SHORTEN THE PAPER

General rules:

- 1. Remember: you are writing for an expert. Cross out all that is trivial or routine.
- 2. Avoid repetition: do not repeat the assumptions of a theorem at the beginning of its proof, or a complicated conclusion at the end of the proof. Do not repeat the assumptions of a previous theorem in the statement of a next one (instead, write e.g. "Under the hypotheses of Theorem 1 with f replaced by g, \dots ."). Do not repeat the same formula—use a label instead.

3. Check all formulas: is each of them necessary?

Phrases you can cross out:

We denote by ℝ the set of all real numbers. We have the following lemma. The following lemma will be useful. the following inequality is satisfied:

Phrases you can shorten (see also p. 38):

Let ε be an arbitrary but fixed positive number \rightsquigarrow Fix $\varepsilon > 0$ Let us fix arbitrarily $x \in X \rightsquigarrow$ Fix $x \in X$ Let us first observe that \rightsquigarrow First observe that We will first compute \rightsquigarrow We first compute

Hence we have $x = 1 \rightsquigarrow$ Hence x = 1Hence it follows that $x = 1 \rightsquigarrow$ Hence x = 1

Taking into account (4) \rightarrow By (4) By virtue of (4) \rightarrow By (4) By relation (4) \rightarrow By (4) In the interval $[0,1] \rightsquigarrow \text{In } [0,1]$ There exists a function $f \in C(X) \rightsquigarrow$ There exists $f \in C(X)$ For every point $p \in M \rightsquigarrow$ For every $p \in M$ It is defined by the formula $F(x) = \dots$ \rightarrow It is defined by $F(x) = \dots$ Theorem 2 and Theorem $5 \rightsquigarrow$ Theorems 2 and 5 This follows from (4), (5), (6) and (7) \sim This follows from (4)–(7) For details see [3], [4] and [5] \rightarrow For details see [3]–[5] The derivative with respect to $t \rightsquigarrow$ The t-derivative A function of class $C^2 \xrightarrow{} A C^2$ function For arbitrary $x \rightsquigarrow$ For all x (For every x) In the case $n = 5 \rightsquigarrow$ For n = 5This leads to a contradiction with the maximality of f \rightarrow , contrary to the maximality of f Applying Lemma 1 we conclude that \rightarrow Lemma 1 shows that, which completes the proof \rightsquigarrow

EDITORIAL CORRESPONDENCE

I would like to submit the enclosed manuscript "....." I am submitting for publication in Studia Mathematica.

I have also included a reprint of my article for the convenience of the referee.

I wish to withdraw my paper as I intend to make a major revision of it.

I regret any inconvenience this may have caused you.

I am very pleased that the paper will appear in Fundamenta. Thank you very much for accepting my paper for publication in

Please find enclosed two copies of the revised version.

As the referee suggested, I inserted a reference to the theorem of

We have followed the referee's suggestions.

I have complied with almost all suggestions of the referee.

REFEREE'S REPORT

The author proves the interesting result that The proof is short and simple, and the article well written. The results presented are original. The paper is a good piece of work on a subject that attracts considerable attention.

I am pleased to It is a pleasure to I strongly recommend it for publication in Studia Mathematica.

The only remark I wish to make is that condition B should be formulated more carefully.

A few minor typographical errors are listed below.

I have indicated various corrections on the manuscript.

The results obtained are not particularly surprising and will be of limited interest.

The results are correct but only moderately interesting. rather easy modifications of known facts.

The example is worthwhile but not of sufficient interest for a research article.

The English of the paper needs a thorough revision.

The paper does not meet the standards of your journal.

Theorem 2 is false as stated. in this generality.

Lemma 2 is known (see)

Accordingly, I recommend that the paper be rejected.

PART B: SELECTED PROBLEMS OF ENGLISH GRAMMAR

INDEFINITE ARTICLE (a, an, —)

- Note: Use "a" or "an" depending on *pronunciation* and not spelling, e.g. a unit, an x.
- 1. Instead of the number "one":

The four centres lie in a plane.

A chapter will be devoted to the study of expanding maps. For this, we introduce **an** auxiliary variable z.

2. Meaning "member of a class of objects", "some", "one of":

Then D becomes a locally convex space with dual space D'. The right-hand side of (4) is then a bounded function. This is easily seen to be **an** equivalence relation. Theorem 7 has been extended to **a** class of boundary value problems. This property is **a** consequence of the fact that Let us now state **a** corollary of Lebesgue's theorem for After **a** change of variable in the integral we get We thus obtain the estimate with **a** constant C.

in the plural:

The existence of partitions of unity may be proved by The definition of distributions implies that, with suitable constants.

 \dots , where G and F are differential operators.

3. In definitions of classes of objects

(i.e. when there are many objects with the given property):

A fundamental solution is a function satisfying

We call C **a** module of ellipticity.

A classical example of **a** constant C such that

We wish to find a solution of (6) which is of the form

in the plural:

The elements of D are often called test functions.

the set of $\begin{vmatrix} \mathbf{p} & \text{oints with distance 1 from } K \\ \text{all functions with compact support} \end{vmatrix}$

The integral may be approximated by sums of the form Taking in (4) functions v which vanish in U we obtain Let f and g be functions such that

4. In the plural—when you are referring to each element of a class:

Direct sums exist in the category of abelian groups.

In particular, closed sets are Borel sets.

Borel measurable functions are often called Borel mappings.

This makes it possible to apply H_2 -results to functions in any H_p .

If you are referring to all elements of a class, use "the":

The real measures form a subclass of the complex ones.

5. In front of an adjective which is intended to mean "having this particular quality":

This map extends to all of M in **an** obvious fashion. **A** remarkable feature of the solution should be stressed.

Section 1 gives a condensed exposition of \dots describes in a unified manner the recent results \dots .

A simple computation gives

Combining (2) and (3) we obtain, with \mathbf{a} new constant C,

A more general theory must be sought to account for these irregularities.

The equation (3) has a unique solution g for every f. But: (3) has the unique solution g = ABf.

DEFINITE ARTICLE (the)

1. Meaning "mentioned earlier", "that":

Let $A \subset X$. If aB = 0 for every B intersecting the set A, then Define $\exp x = \sum x^i/i!$. The series can easily be shown to converge.

2. In front of a noun (possibly preceded by an adjective) referring to a single, uniquely determined object (e.g. in definitions):

Let f be **the** linear form $\begin{vmatrix} g \mapsto (g, F) \\ \text{defined by (2).} \end{vmatrix}$ [If there is only one.]

So u = 1 in the compact set K of all points at distance 1 from L. We denote by B(X) the Banach space of all linear operators in X., under the usual boundary conditions.

...., with the natural definitions of addition and multiplication. Using the standard inner product we may identify

3. In the construction: the + property (or another characteristic) + of + object:

The continuity of f follows from

The existence of test functions is not evident.

There is a fixed compact set containing the supports of all the f^j . Then x is the centre of an open ball U.

The intersection of a decreasing family of such sets is convex.

- But: Every nonempty open set in \mathbb{R}^k is a union of disjoint boxes. [If you wish to stress that it is some union of not too well specified objects.]
- 4. In front of a cardinal number if it embraces all objects considered:

The two groups have been shown to have the same number of generators. [Two groups only were mentioned.]Each of the three products on the right of (4) satisfies[There are exactly three products there.]

5. In front of an ordinal number:

The first Poisson integral in (4) converges to g. The second statement follows immediately from the first.

6. In front of surnames used attributively:

the Dirichlet problem		Taylor's formula
the Taylor expansion	But:	[without "the"]
the Gauss theorem		a Banach space

7. In front of a noun in the plural if you are referring to a class of objects as a whole, and not to particular members of the class:

The real measures form a subclass of **the** complex ones. This class includes **the** Helson sets.

ARTICLE OMISSION

1. In front of nouns referring to activities:

Application of Definition 5.9 gives (45).
Repeated application (use) of (4.8) shows that
The last formula can be derived by direct consideration of
Thus A is the smallest possible extension in which differentiation is always possible.
Using integration by parts we obtain
If we apply induction to (4), we get
Addition of (3) and (4) gives
This reduces the solution to division by Px.
Comparison of (5) and (6) shows that

2. In front of nouns referring to properties if you mention no particular object:

In questions of uniqueness one usually has to consider By continuity, (2) also holds when f = 1. By duality we easily obtain the following theorem. Here we do not require translation invariance. 3. After certain expressions with "of":

a type of c onvergence	the hypothesis of p ositivity
a problem of u niqueness	the method of p roof
the condition of e llipticity	the point of i ncrease

4. In front of numbered objects:

It follows from **Theorem 7** that **Section 4** gives a concise presentation of **Property (iii)** is called the triangle inequality. This has been proved in **part (a)** of the proof.

But: the set of solutions of the form (4.7)To prove the estimate (5.3) we first extend We thus obtain the inequality (3). [Or: inequality (3)] The asymptotic formula (3.6) follows from Since the region (2.9) is in U, we have

5. To avoid repetition:

the order and symbol of a distribution the associativity and commutativity of Athe direct sum and direct product the inner and outer factors of f [Note the plural.]

But: a deficit or an excess

6. In front of surnames in the possessive:

Minkowski's inequality, *but*: **the** Minkowski inequality Fefferman and Stein's famous theorem, *more usual*: the famous Fefferman–Stein theorem

- 7. In some expressions describing a noun, especially after "with" and "of":
 - an algebra with unit e; an operator with domain H^2 ; a solution with vanishing Cauchy data; a cube with sides parallel to the axes; a domain with smooth boundary; an equation with constant coefficients; a function with compact support; random variables with zero expectation

the equation of motion; the velocity of propagation; an element of finite order; a solution of polynomial growth;

a ball of radius 1; a function of norm p

But: elements of **the** form $f = \dots$ a Banach space with **a** weak symplectic form wtwo random variables with **a** common distribution

8. After forms of "have":

It has finite norm. But: It has **a** finite norm not exceeding 1. **a** compact support. But: It has **b** a compact support contained in I.

9. In front of the name of a mathematical discipline:

This idea comes from game theory (homological algebra).

But: in the theory of distributions

10. Other examples:

We can assume that G is in diagonal form.

Then A is deformed into B by pushing it at constant speed along the integral curves of X.

G is now viewed as a set, without group structure.

INFINITIVE

1. Indicating aim or intention:

To prove the theorem, we first let

We now apply (5) to study the group of to derive the following theorem. to obtain an x with norm not exceeding 1.

Here are some examples to show how

2. In constructions with "too" and "enough":

This method is **too** complicated **to** be used here.

This case is important **enough to** be stated separately.

3. Indicating that one action leads to another:

We now apply Theorem 7 to get Nf = 0. $[= \dots$ and we get Nf = 0]Insert (2) into (3) to find that

4. In constructions like "we may assume M to be":

We may assume M to be compact. We define K to be the section of H over S. If we take the contour G to lie in U, then We extend f to be homogeneous of degree 1. The class A is defined by requiring all the functions f to satisfy Partially order P by declaring X < Y to mean that 5. In constructions like "M is assumed to be":

is assumed $\langle expected/found/considered/taken/claimed \rangle$ to be open.

The map M will be chosen to satisfy (2). can be taken to be constant. can easily be shown to have is also found to be of class S.

This investigation is **likely to produce** good results. [= It is very probable it will]

The close agreement of the six elements is **unlikely to be** a coincidence. [= is probably not]

6. In the structure "for this to happen":

For this to happen, F must be compact. [= In order that this happens]

For the last estimate to hold, it is enough to assume Then for such a map to exist, we must have

7. As the subject of a sentence:

To see that this is not a symbol is fairly easy.

[Or: It is fairly easy to see that]

To choose a point at random in the interval [0,1] is a conceptual experiment with an obvious intuitive meaning.

To say that u is maximal means simply that

After expressions with "it":

It is necessary (useful/very important) to consider

- It makes sense to speak of
- It is therefore of interest to look at
- 8. After forms of "be":

Our goal $\langle method/approach/procedure/objective/aim \rangle$ is to find The problem $\langle difficulty \rangle$ here is to construct

9. With nouns and with superlatives, in the place of a relative clause:

The theorem to be proved is the following. [= which will be proved] This will be proved by the method to be described in Section 6. For other reasons, to be discussed in Chapter 4, we have to He was the first to propose a complete theory of They appear to be the first to have suggested the now accepted

interpretation of

10. After certain verbs:

These properties led him to suggest that

Lax claims to have obtained a formula for

This map turns out to satisfy

At first glance M appears to differ from N in two major ways:

A more sophisticated argument **enables** one **to prove** that

[Note: "enable" requires "one", "us" etc.]

He **proposed to study** that problem. [Or: He proposed studying] We **make** G **act** trivially on V.

Let f satisfy (2). [Not: "Let f satisfies"]

We need to consider the following three cases.

We need not consider this case separately.

["need to" in affirmative clauses, without "to" in negative clauses; also note: "we only need to consider", but: "we need only consider"]

ING-FORM

1. As the subject of a sentence (note the absence of "the"):

Repeating the previous argument and using (3) leads to Since taking symbols commutes with lifting, A is Combining Proposition 5 and Theorem 7 gives

2. After prepositions:

After making a linear transformation, we may assume that

In passing from (2) to (3) we have ignored the factor n.

In deriving (4) we have made use of

On substituting (2) into (3) we obtain

Before making some other estimates, we prove

The trajectory Z enters X without meeting x = 0.

Instead of using the Fourier method we can multiply

In addition to illustrating how our formulas work, it provides

Besides being very involved, this proof gives no information on This set is obtained by letting $n \to \infty$.

It is important to pay attention to domains of definition when trying to

The following theorem is the key to constructing

The reason for preferring (1) to (2) is simply that

3. In certain expressions with "of":

The idea of combining (2) and (3) came from The problem considered there was that of determining WF(u) for We use the technique of extending

This method has the **disadvantage of** $\begin{bmatrix} being very involved. \\ requiring that f be positive. \\ [Note the infinitive.] \end{bmatrix}$

Actually, S has the much stronger **property of being** convex.

4. After certain verbs, especially with prepositions:

We begin by analyzing (3). We succeeded (were successful) in proving (4). [*Not*: "succeeded to prove"] We next turn to estimating They **persisted in investigating** the case We are **interested in finding** a solution of We were surprised at finding out that [Or: surprised to find out] Their study resulted in proving the conjecture for The success of our method will **depend on proving** that To compute the norm of amounts to finding We should **avoid using** (2) here, since [Not: "avoid to use"] We put off discussing this problem to Section 5. It is worth noting that [Not: "worth to note"] It is worth while discussing here this phenomenon. [Or: worth while to discuss; "worth while" with ing-forms is best avoided as it often leads to errors.] It is an idea worth carrying out. [Not: "worth while carrying out", nor: "worth to carry out"] After having finished proving (2), we will turn to [*Not*: "finished to prove"] However, (2) **needs handling** with greater care. One more case **merits mentioning** here. In [7] he mentions having proved this for f not in S. 5. Present Participle in a separate clause (note that the subjects of the main clause and the subordinate clause must be the same): We show that f satisfies (2), thus completing the analogy with \dots **Restricting** this to R, we can define [Not: "Restricting, the lemma follows". The lemma does not restrict!] The set A, being the union of two intersecting continua, is connected. 6. Present Participle describing a noun: We need only consider paths starting at 0. We interpret f as a function with image **having** support in We regard f as **being** defined on 7. In expressions which can be rephrased using "where" or "since": Now J is defined to equal Af, the function f being as in (3). [= where f is] This is a special case of (4), the space X here **being** B(K). We construct three maps of the form (5), each of them **satisfying** (8). Then $\lim_{t} a(x,t) < 1$, the limit **being assumed** to exist for every x.

The ideal is defined by $m = \ldots$, it **being understood** that Now, F **being** convex, we can assume that [= since F is] Hence $F = \emptyset$ (it **being** impossible to make A and B intersect). [= since it is impossible]

[Do not write "a function being an element of X" if you mean "a function which is an element of X".]

8. In expressions which can be rephrased as "the fact that X is":

Note that M being cyclic implies F is cyclic. The probability of X being rational equals 1/2. In addition to f being convex, we require that

PASSIVE VOICE

1. Usual passive voice:

This theorem was proved by Milnor in 1976.

In items 2–6, passive voice structures replace sentences with subject "we" or impersonal constructions of other languages.

2. Replacing the structure "we do something":

This identity is established by observing that

This difficulty is avoided above.

When this is substituted in (3), an analogous description of K is obtained.

Nothing is assumed concerning the expectation of X.

3. Replacing the structure "we prove that X is":

The function M is easily shown to have may be said to be regular if

This equation is known to hold for

4. Replacing the construction "we give an object X a structure Y":

Note that E can be given a complex structure by The letter A is here given a bar to indicate that

5. Replacing the structure "we act on something":

This order behaves well when g is acted upon by an operator. Hence F can be thought of as

So all the terms of (5) are accounted for.

The preceding observation, when **looked at** from a more general point of view, leads to

In the physical context already referred to, K is

6. Meaning "which will be (proved etc.)":

Before stating the result **to be proved**, we give This is a special case of convolutions **to be introduced** in Chapter 8. We conclude with two simple lemmas **to be used** mainly in

QUANTIFIERS

This implies that A contains $\begin{vmatrix} all \text{ open subsets of } U.\\ all y \text{ with } Gy = 1. \end{vmatrix}$ Let B be the collection of $\begin{vmatrix} all \text{ transforms } F \text{ of the form }\\ all A \text{ such that } \end{vmatrix}$

In this way F is defined at **all** points of X.

This holds for all $n \neq 0$ (for all *m* which have/for all other *m*/ for all but a finite number of indices *i*)

The domain X contains **all the** boundary except the origin. The integral is taken over **all of** X.

Hence E, F and G	all extend to a neighbourhood of U . all have their supports in U .
	are all zero at x . are all equal.

There exist functions R, all of whose poles are in U, with Each of the following nine conditions implies all the others. Such an x exists iff all the intervals A_x have

> For every g in X (not in X) there exists an N [But: for all f and g, for any two maps f and g; "every" is followed by a singular noun.] To every f there corresponds a unique g such that Every invariant subspace of X is of the form" [Do not write: "Every subspace is not of the form" if you mean: "No subspace is of the form"; "every" must be followed by an affirmative statement.] Thus $f \neq 0$ at almost every point of X. = 0 for each n [Each = every considered separate]

Since $A_n = 0$ for each n, \dots [Each = every, considered separately] Each term in this series is either 0 or 1.

Consequently, F is bounded on **each** bounded set.

Each of these four integrals is finite.

These curves arise from, and **each** consists of There remain four intervals of length 1/16 **each**. Thus X assumes values $0, 1, \ldots, 9$, **each** with probability 1/10. The functions F_1, \ldots, F_n are **each** defined in the interval [0, 1].

Those n disjoint boxes are translates of each other.

If K is now **any** compact subset of H, there exists

[Any = whatever you like; write "for all x", "for every x" if you just mean a quantifier.]

Every measure can be completed, so whenever it is convenient, we may assume that **any** given measure is complete.

There is a subsequence such that There exists an x with [Or: there exists x, but: there is an x]There are sets satisfying (2) but not (3). There is only one such f. There is a unique function f such that Each f lies in zA for some A (at least one A/exactly one A/at most one A). Note that some of the X_n may be repeated.

Thus F has **no** pole in U (hence **none** in K). [Or: no poles]

Call a set dense if its complement contains no nonempty open subset.

If no two members of A have an element in common, then

No two of the spaces X, Y, and Z are isomorphic.

It can be seen that **no** x has more than one inverse.

In other words, for **no** real x does $\lim F_n(x)$ exist.

[Note the inversion after the negative clause.]

If there is **no** bounded functional such that

..... provided **none of** the sums is of the form

Let A_n be a sequence of positive integers **none of which** is 1 less than a power of two.

If there is an f such that, set If there are $\langle is \rangle$ none, define None of these are $\langle is \rangle$ possible.

Both f and g are obtained by

[Or: f and g are both obtained]

For **both** C^{∞} and analytical categories,

It behaves covariantly with respect to maps of **both** X and G. We now apply (3) to **both** sides of (4).

Both $\langle \text{these}/\text{the} \rangle$ conditions are restrictions only on

[*Note*: "the" and "these" after "both"]

It lies on no segment **both of whose** endpoints are in K.

Two consecutive elements do not belong both to A or both to B.

Both its sides are convex. [Or: Its sides are both convex.] Let B and C be nonnegative numbers, not both 0.

Choose points x in M and y in N, both close to z, and We show how this method works in two cases.

In **both** \langle In each \rangle , C is

In either case, it is clear that [= In both cases]

Each f can be expressed in either of the forms (1) and (2).

[= in any of the two forms]

The density of X + Y is given by **either of** the two integrals.

The two classes coincide if X is compact. In that case we write C(X) for either of them.

Either f or g must be bounded.

Let u and v be two distributions **neither of** which is

[Use "neither" when there are *two* alternatives.]

This is true for **neither of** the two functions.

Neither statement is true.

In **neither** case can f be smooth.

[Note the inversion after the negative clause.]

He proposes two conditions, but neither is satisfactory.

NUMBER, QUANTITY, SIZE

1. Cardinal numbers:

Hence A and B are also F-functions, any two of A, B, and C being independent.

the multi-index with all entries **zero** except the kth which is **one** the last k entries **zero**

This shows that there are no **two** points a and b such that There are **three** that the reader must remember. [= three of them] We have defined A, B, and C, and **the three** sets satisfy For **the two** maps defined in Section 3,

["The" if only two maps are defined there.]

Clearly, R is concentrated at the n points x_1, \ldots, x_n defined above.

for at least $\langle at most \rangle$ one k; with norm at least equal to 2

There are at most 2 such r in (0, 1). There is a unique map satisfying (4). Equation (4) has a unique solution g for each f. But: it has the unique solution g = ABf. Problem (4) has one and only one solution. Precisely r of the intervals are closed. In Example 3 only one of the x_j is positive. If p = 0 then there are an additional m arcs.

2. Ordinal numbers:

The first two are simpler than the third. Let S_i be the first of the remaining S_j . The *n*th trial is the last. It follows that X_1 appears at the (k + 1)th place. The gain up to and including the nth trial is The elements of the third and fourth rows are in I. [Note the plural.]

Therefore F has a zero of **at least third** order at x.

3. Fractions:

Two-thirds of its diameter is covered by

But: Two-thirds of the gamblers are ruined.

Obviously, G is half the sum of the positive roots.

[*Note*: Only "half" can be used with or without "of".] On the average, about half the list will be tested. But J contains an interval of half its length in which

> Note that F is greater by a half (a third). The other player is half (one third) as fast. We divide J in half. All sides were increased by the same proportion. About 40 percent of the energy is dissipated. A positive percentage of summands occurs in all k partitions.

4. Smaller (greater) than:

Observe that n is $\begin{array}{l}
\textbf{greater \langle \text{less} \rangle \textbf{than } k.}\\
\textbf{much \langle \text{substantially} \rangle \textbf{greater } \text{than } k.}\\
\textbf{no greater } \langle \text{less} \rangle \textbf{than or equal to } k.\\
\textbf{greater } \langle \text{less} \rangle \textbf{than or equal to } k.\\
\textbf{[Not: "greater or equal to"]}\\
\textbf{strictly less than } k.
\end{array}$

All points at a distance less than K from A satisfy (2). We thus obtain a graph of no more than k edges.

This set has $\begin{vmatrix} \mathbf{fewer} & \text{elements than } K \\ \mathbf{no fewer than twenty elements.} \end{vmatrix}$

Therefore F can have no jumps exceeding 1/4. The degree of P exceeds that of Q. Find the density of the smaller of X and Y. The smaller of the two satisfies It is dominated (bounded/estimated/majorized) by

5. How much smaller $\langle \text{greater} \rangle$:

25 is **3 greater** than 22; 22 is **3 less** than 25.

Let a_n be a sequence of positive integers none of which is **1** less than a power of two.

The degree of P exceeds that of Q by at least 2.

Consequently, f is greater by a half $\langle a \text{ third} \rangle$.

It follows that C is less than a third of the distance between

Within I, the function f varies (oscillates)
by less than l.
The upper and lower limits of f differ by at most 1.
We thus have in A one element too many.
On applying this argument k more times, we obtain
This method is recently less and less used.
A succession of more and more refined discrete models.

6. How many times as great:

twice $\langle \text{ten times}/\text{one third} \rangle$ as long as; half as big as The longest edge is at most 10 times as long as the shortest one. Now A has twice as many elements as B has. Clearly, J contains a subinterval of half its length in which Observe that A has four times the radius of B.

The diameter of L is 1/k times $\langle \mathbf{twice} \rangle$ that of M.

7. Multiples:

The k-fold integration by parts shows that We have shown that F covers M twofold.

> It is bounded by a multiple of $t \langle a \text{ constant times } t \rangle$. This distance is less than a constant multiple of d. Note that G acts on H as a multiple, say n, of V.

8. Most, least, greatest, smallest:

Evidently, F has the most $\langle the fewest \rangle$ points when In most cases it turns out that

Most of the theorems presented here are original.

The proofs are, for the most part, only sketched. Most probably, his method will prove useful in What most interests us is whether

The **least** such constant is called the norm of f.

This is **the least** useful of the four theorems.

The method described above seems to be the least complex.

That is **the least** one can expect.

The elements of A are comparatively big, but **least** in number. None of those proofs is easy, and John's **least of all**.

The best estimator is a linear combination U such that $\operatorname{var} U$ is $\langle \operatorname{the} \rangle$ smallest possible.

The expected waiting time is **smallest** if

Let L be the smallest number such that

Now, F has the smallest norm among all f such that

It is the largest of the functions which occur in (3).

There exists a smallest algebra with this property.

Find the second largest element in the list L.

9. Many, few, a number of:

	a large number of illustrations.
There are	only a finite number of f with $Lf = 1$.
Note the	a small number of exceptions.
plural.	an infinite number of sets
	a negligible number of points with

Ind c is **the number of times** that c winds around 0. We give **a number of** results concerning [= some] This may happen in **a number of** cases.

They correspond to the values of a countable number of invariants. for all n except a finite number (for all but finitely many n). Thus Q contains all but a countable number of the f^i .

There are only **countably many** elements q of Q with dom q = S.

The theorem is fairly general. There are, however, **numerous** exceptions.

A variety of other characteristic functions can be constructed in this way.

> There are **few** exceptions to this rule. [= not many] **Few** of various existing proofs are constructive.

He accounts for all the major achievements in topology over **the last few** years.

The generally accepted point of view in this domain of science seems to be changing **every few** years.

There are **a few** exceptions to this rule. [= some]Many interesting examples are known. We now describe

a few of these.

Only a few of those results have been published before. Quite a few of them are now widely used.

[= A considerable number]

10. Equality, difference:

```
A equals B or A is equal to B [Not: "A is equal B"]
```

The Laplacian	of g is $4r > 0$.	Then r is about kn .

The inverse of FG is GF.

The norms of f and g coincide.

Therefore F has the same number of zeros and poles in U.

They differ by a linear term $\langle by a scale factor \rangle$. The differential of f is different from 0. Each member of G other than g is Lemma 2 shows that F is not identically 0. Let a, b and c be distinct complex numbers. Each w is Pz for precisely m distinct values of z. Functions which are equal a.e. are indistinguishable as far as integration is concerned.

11. Numbering:

Exercises 2 to 5 furnish other applications of this technique. [Amer.: Exercises 2 through 5]

in the third and fourth rows the derivatives up to order kfrom row k onwards the odd-numbered terms in lines 16–19 the next-to-last column the last paragraph but one of the previous proof

> The matrix with $\begin{vmatrix} 1 & \text{in the } (i, j) \text{ entry and zero elsewhere} \\ \text{all entries zero except for } N - j \text{ at } (N, j) \end{vmatrix}$ This is $\begin{vmatrix} \text{hinted at in Sections 1 and 2.} \\ \text{quoted on page 36 of } [4]. \end{vmatrix}$

HOW TO AVOID REPETITION

1. Repetition of nouns:

Note that the continuity of f implies that of g.

The passage from Riemann's theory to that of Lebesgue is

The diameter of F is about twice **that** of G.

His method is similar to **that** used in our previous paper.

The nature of this singularity is the same as **that**

which f has at x = 0.

Our results do not follow from those obtained by Lax.

One can check that the metric on T is **the one** we have just described.

It follows that S is the union of two disks. Let D be the one that contains

The cases p = 1 and p = 2 will be **the ones** of interest to us.

We prove a uniqueness result, similar to those of the preceding section.

Each of the functions on the right of (2) is **one** to which

Now, F has many points of continuity. Suppose x is **one**.

In addition to a contribution to W_1 , there may be one to W_2 .

We now prove that the constant pq cannot be replaced by a smaller **one**.

Consider the differences between these integrals and

the corresponding ones with f in place of g.

The geodesics (4) are **the** only **ones** that realize the distance between their endpoints.

On account of the estimate (2) and similar ones which can be

- We may replace A and B by whichever is the larger of **the two**. [*Not*: "the two ones"]
- This inequality applies to conditional expectations as well as to ordinary **ones**.
- One has to examine the equations (4). If **these** have no solutions, then
- Thus D yields operators D^+ and D^- . These are formal adjoints of each other.
- This gives rise to the maps F_i . All the other maps are suspensions of **these**.
- So F is the sum of A, B, C and D. The last two of **these** are zero.
- Both f and g are connected, but **the latter** is in addition compact. [The latter = the second of *two* objects]
- Both AF and BF were first considered by Banach, but only the former is referred to as the Banach map, the latter being called the Hausdorff map.
- We have thus proved Theorems 1 and 2, the latter without using

Since the vectors G_i are orthogonal to **this last** space,

As a consequence of this last result,

Let us consider sets of the type (1), (2), (3) and (4). These last two are called

We shall now describe a general situation in which **the last-mentioned** functionals occur naturally.

- 2. Repetition of adjectives, adverbs or phrases like "x is":
 - If f and g are measurable functions, then so are f + g and $f \cdot g$.

The union of measurable sets is a measurable set; **so is** the complement of every measurable set.

- The group G is compact and so is its image under f.
- It is of the same fundamental importance in analysis \mathbf{as} is the construction of

Note that F is bounded but is not necessarily so after division by G.

Show that there are many such Y. There is only one such series for each y. Such an h is obtained by

3. Repetition of verbs:

A geodesic which meets bM does so either transversally or

This will hold for x > 0 if it **does** for x = 0.

Note that we have not required that, and we shall not **do so** except when explicitly stated.

The integral might not converge, but it **does so** after

We will show below that the wave equation can be put in this form, as can many other systems of equations.

The elements of L are not in S, as they are in the proof of

4. Repetition of whole sentences:

The same is true for f in place of g.

The same being true for \bar{f} , we can [= Since the same] The same holds for (applies to) the adjoint map.

We shall assume that this is the case.

Such was the case in (2).

The L^2 theory has more symmetry than is the case in L^1 .

Then either or In the latter $\langle \text{former} \rangle$ case,

For k this is no longer true. This is not true of (2).

This is not so in other queuing processes.

If this is so, we may add

If $f_i \in L$ and if $F = f_1 + \cdots + f_n$ then $F \in H$, and every F is so obtained.

We would like to If U is open, this can be done.

On S, this gives the ordinary topology of the plane.

Note that **this** is not equivalent to

[Note the difference between "this" and "it": you say "*it* is not equivalent to" if you are referring to some object explicitly mentioned in the preceding sentence.]

Consequently, F has the stated (desired/claimed) properties.

WORD ORDER

- $General \ remarks$: The normal order is: subject + verb + direct object + adverbs in the order manner-place-time.
- Adverbial clauses can also be placed at the beginning of a sentence, and some adverbs always come between subject and verb. Subject almost always precedes verb, except in questions and some negative clauses.

1. ADVERBS

- 1a. Between subject and verb, but after forms of "be"; in compound tenses after first auxiliary
- Frequency adverbs:

This has **already** been proved in Section 8. This result will **now** be derived computationally. Every measurable subset of X is **again** a measure space. We **first** prove a reduced form of the theorem. There has since been little systematic work on It has recently been pointed out by Fix that It is sometimes difficult to This usually implies further conclusions about f. It often does not matter whether

• Adverbs like "also", "therefore", "thus":

Our presentation is **therefore** organized in such a way that The sum in (2), though formally infinite, is **therefore** actually finite. One must **therefore** also introduce the class of

But C is connected and is **therefore** not the union of

These properties, with the exception of (1), also hold for t.

We will **also** leave to the reader the verification that It will **thus** be sufficient to prove that

So (2) implies (3), since one would **otherwise** obtain

The order of several topics has **accordingly** been changed.

• *Emphatic adverbs* (*clearly*, *obviously*, *etc.*):

It would **clearly** have been sufficient to assume that

But F is clearly not an I-set.

Its restriction to N is **obviously** just f.

This case must **of course** be excluded.

The theorem **evidently** also holds if x = 0.

The crucial assumption is that the past history

in no way influences

We did not really have to use the existence of T.

The problem is to decide whether (2) really follows from (1).

The proof is now **easily** completed.

The maximum is **actually** attained at some point of M.

We then **actually** have [= We have even more]

At present we will **merely** show that

A stronger result is **in fact** true.

Throughout integration theory, one **inevitably** encounters ∞ . But *H* itself can **equally well** be a member of *S*.

1b. After verb-most adverbs of manner:

We conclude **similarly** that One sees **immediately** that Much relevant information can be obtained **directly** from (3). This difficulty disappears **entirely** if This method was used **implicitly** in random walks. 1c. After an object if it is short:

We will prove the theorem **directly** without using the lemma. But: We will prove **directly** a theorem stating that This is true for every sequence that shrinks to x **nicely**. Define Fg **analogously** as the limit of Formula (2) defines g **unambiguously** for every g'.

1d. At the beginning-adverbs referring to the whole sentence:

Incidentally, we have now constructed **Actually**, Theorem 3 gives more, namely **Finally**, (2) shows that f = g. [Not: "At last"] **Nevertheless**, it turns out that **Next**, let V be the vector space of

More precisely, Q consists of
Explicitly (Intuitively), this means that
Needless to say, the boundedness of f was assumed only for simplicity.
Accordingly, either f is asymptotically dense or

1e. In front of adjectives-adverbs describing them:

a **slowly varying** function **probabilistically significant** problems a method **better suited** for dealing with

> The maps F and G are similarly obtained from H. The function F has a rectangularly shaped graph. Three-quarters of this area is covered by subsequently chosen cubes. [Note the singular.]

1f. "only"

We need the openness **only** to prove the following.

It reduces to the statement that **only** for the distribution F do the maps F_i satisfy (2). [Note the inversion.]

In this chapter we will be concerned **only** with

In (3) the X_j assume the values 0 and 1 only.

If (iii) is required for finite unions only, then

We need **only** require (5) to hold for bounded sets. The proof of (2) is similar, and will **only** be indicated briefly. To prove (3), it **only** remains to verify

2. ADVERBIAL CLAUSES

2a. At the beginning:

In testing the character of, it is sometimes difficult to For n = 1, 2, ..., consider a family of 2b. At the end (normal position):

The averages of F_n become small in small neighbourhoods of x.

2c. Between subject and verb, but after first auxiliary-only short clauses:

The observed values of X will on average cluster around This could in principle imply an advantage. For simplicity, we will for the time being accept as F only C^2 maps.

> Accordingly we are in effect dealing with The knowledge of f is at best equivalent to The stronger result is in fact true. It is in all respects similar to matrix multiplication.

2d. Between verb and object if the latter is long:

It suffices for our purposes to assume To a given density on the line there corresponds on the circle the density given by

3. INVERSION AND OTHER PECULIARITIES

3a. Adjective or past participle after a noun:

Let Y be the complex X with the origin removed.
Theorems 1 and 2 combined give a theorem
We now show that G is in the symbol class indicated.
We conclude by the part of the theorem already proved that
The bilinear form so defined extends to
Then for A sufficiently small we have
By queue length we mean the number of customers present including the customer being served.
The description is the same with the roles of A and B reversed.

3b. Direct object or adjectival clause placed farther than usual—when they are long:

We must add to the right-hand side of (3) the probability that This is equivalent to defining in the z-plane a density with Let F be the restriction to D of the unique linear map The probability at birth of a lifetime exceeding t is at most

3c. Inversion in some negative clauses:

We do not assume that, **nor do** we assume a priori that **Neither is** the problem simplified by assuming f = g. The "if" part now follows from (3), since **at no point can** S exceed the larger of X and Y.

The fact that for no x does Fx contain y implies that

In no case does the absence of a reference imply any claim to originality on my part.

3d. Inversion—other examples:

But F is compact and so is G. If f, g are measurable, then so are f + g and $f \cdot g$.

Only for f = 1 **can** one expect to obtain **does** that limit exist.

3e. Adjective in front of forms of "be"-for emphasis:

By far the most important is the case where Much more subtle are the following results of John. Essential to the proof are certain topological properties of M.

3f. Subject coming sooner than in some other languages:

Equality occurs in (1) iff f is constant. The natural **question** arises whether it is possible to In the following applications **use** will be made of Recently **proofs** have been constructed which use

- 3g. Incomplete clause at the beginning or end of a sentence:
 - **Put differently**, the moments of arrival of the lucky customers constitute a renewal process.
 - Rather than discuss this in full generality, let us look at
 - It is important that the tails of F and G are of comparable magnitude, a statement made more precise by the following inequalities.

WHERE TO INSERT A COMMA

- General rules: Do not over-use commas—English usage requires them less often than in many other languages. Do not use commas around a clause that defines (limits, makes more precise) some part of a sentence. Put commas before and after non-defining clauses (i.e. ones which can be left out without damage to the sense). Put a comma where its lack may lead to ambiguity, e.g. between two symbols.
- 1. Comma not required:

We shall now prove that f is proper. The fact that f has radial limits was proved in [4]. It is reasonable to ask whether this holds for g = 1. Let M denote the set of all paths that satisfy (2). There is a polynomial P such that Pf = g. The element given by (3) is of the form (5). Let M be the manifold to whose boundary f maps K. Take an element all of whose powers are in S.

> We call F proper if G is dense. There exists a D such that $D \sim H$ whenever $H \sim G$. Therefore F(x) = G(x) for all $x \in X$. Let F be a nontrivial continuous linear operator in V.

2. Comma required:

The proof of (3) depends on the notion of M-space, which has already been used in [4].

We will use the map H, which has all the properties required.

There is only one such f, and (4) defines a map from

In fact, we can do even better. In this section, however, we will not use it explicitly. Moreover, F is countably additive. Finally, (d) and (e) are consequences of (4). Nevertheless, he succeeded in proving that Conversely, suppose that Consequently, (2) takes the form In particular, f also satisfies (1).

- Guidance is also given, whenever necessary or helpful, on further reading.
- This observation, when looked at from a more general point of view, leads to
- It follows that f, being convex, cannot satisfy (3).
- If e = 1, which we may assume, then

We can assume, by decreasing k if necessary, that

Then (5) shows, by Fubini's theorem, that

Put this way, the question is not precise enough. Being open, V is a union of disjoint boxes.

This is a special case of (4), the space X here being B(K).

In [2], X is assumed to be compact.

For all x, G(x) is convex.

[Comma between two symbols.]

In the context already referred to, K is the complex field. [Comma to avoid ambiguity.]

3. Comma optional:

By Theorem 2, there exists an h such that

For z near 0, we have

If h is smooth, then M is compact.

Since h is smooth, M is compact.

It is possible to use (4) here, but it seems preferable to

This gives (3), because $\langle \text{since} \rangle$ we may assume

Integrating by parts, we obtain The maps X, Y, and Z are all compact. We have X = FG, where F is defined by Thus $\langle \text{Hence/Therefore} \rangle$, we have

1. Non(-):

Write consistently either

nontrivial, nonempty, nondecreasing, nonnegative, or non-trivial, non-empty, non-decreasing, non-negative.

[But: non-locally convex, non-Euclidean]

2. Hyphen required:

one-parameter group two-stage computation *n*-fold integration out-degree global-in-time solution [But: solution global in time]

3. Hyphen optional:

right hand side or right-hand side second order equation or second-order equation selfadjoint or self-adjoint halfplane or half-plane seminorm or semi-norm a blow-up, a blow up, or a blowup [But: to blow up]the *n*th element or the *n*-th element

SOME TYPICAL ERRORS

1. Spelling errors:

Spelling should be either British or American throughout:

Br.: colour, neighbourhood, centre, fibre, labelled, modelling *Amer.*: color, neighborhood, center, fiber, labeled, modeling

"an unified approach" \leadsto a unified approach

```
"a M such that" \leadsto an M such that
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[Use a or an according to pronunciation.]

"preceeding" → preceding "occuring" → occurring "developped" → developed "loosing" → losing "it's norm" → its norm

2. Grammatical errors:

"Let f denotes" \rightsquigarrow Let f denote "Most of them is" \rightsquigarrow Most of them are "There is a finite number of" \rightsquigarrow There are a finite number of

"In 1964 Lax has shown" \rightarrow In 1964 Lax showed [Use the past tense if a date is given.] "the Taylor's formula" \rightarrow Taylor's formula [Or: the Taylor formula] "the section 1" \rightarrow Section 1 "Such map exists" \rightarrow Such a map exists [But: for every such map] "in case of smooth norms" \rightarrow in the case of smooth norms "We are in the position to prove" \rightarrow We are in a position to prove "We now give few examples" [= not many] \rightarrow We now give a few examples [= some] "F is equal G" \rightsquigarrow F is equal to G [Or: F equals G] "F is greater or equal to G" \rightarrow F is greater than or equal to G "This is precised by" \rightsquigarrow This is made more precise by "This allows to prove" \rightsquigarrow This allows us to prove "This makes clear that" \rightarrow This makes it clear that "The first two ones are" \rightsquigarrow The first two are "a not dense set" \rightsquigarrow a non-dense set [But: This set is not dense] "Since f = 0, then M is closed" \rightarrow Since f = 0, it follows that M is closed "....., as it is shown in Sec. 2" \sim , as is shown in Sec. 2 "Every function being an element of X is convex" \rightsquigarrow Every function which is an element of X is convex "Every f is not convex" \rightsquigarrow No f is convex "Setting n = p, the equation can be solved by \rightarrow Setting n = p, we can solve the equation by [Because we set.] "We have $\langle \text{get/obtain} \rangle$ that B is empty" \sim We see $\langle \text{know/conclude/deduce/find/infer} \rangle$ that B is empty 3. Wrong word used: "Summing (2) and (3) by sides" \rightarrow Summing (2) and (3) "In the first paragraph" \rightarrow In the first section "which proves our thesis" \rightsquigarrow which proves our assertion (conclusion/statement) [thesis = dissertation]"to this aim" \sim to this end "At first, note that" ~> First, note that "At last, C is dense because" \rightarrow Finally, C is dense because "for every two elements" \rightsquigarrow for any two elements "...., what completes the proof" \rightarrow , which completes the proof "...., what is impossible" \rightsquigarrow , which is impossible

"We denote it shortly by c" \rightsquigarrow We denote it briefly by c"This map verifies (2)" \rightsquigarrow This map satisfies (2)

> "continuous in the point x" \rightarrow continuous at x"disjoint with B" \rightarrow disjoint from B"equivalent with B" \rightarrow equivalent to B"independent on B" \rightarrow independent of B[But: depending on B, independence from B] "similar as B" \rightarrow similar to Bsimilarly as in Sec. 2 \rightarrow similarly to Sec. 2 as (just as) in Sec. 2 as is the case in Sec. 2 in much the same way as in Sec. 2 "on Fig. 3" \rightarrow in Fig. 3 "in the end of Sec. 2" \rightarrow at the end of Sec. 2

4. Wrong word order:

"a bounded by 1 function" \rightsquigarrow a function bounded by 1 "the described above condition" \rightsquigarrow the condition described above "the obtained solution" \rightsquigarrow the solution obtained "the mentioned map" \rightsquigarrow the map mentioned

[But: the above-mentioned map]

"the both conditions" \leadsto both conditions, both the conditions "its both sides" \leadsto both its sides

"the three first rows" \rightsquigarrow the first three rows "the two following sets" \rightsquigarrow the following two sets

"This map we denote by f" \rightsquigarrow We denote this map by f"Only for x = 1 the limit exists" \rightsquigarrow Only for x = 1 does the limit exist "For no x the limit exists" \rightsquigarrow For no x does the limit exist

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