

Noncanonical Parsing

Sylvain Schmitz

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JAVA Declarations

Gosling et al. [1996]

Example

```
public class Declarations {  
    public final static int FIELD = 10;  
    public static int method (int i) {  
        // ...  
    }  
}
```

JAVA Grammar

Gosling et al. [1996]

Example

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$\langle FDecl \rangle \rightarrow \langle FModS \rangle \langle Type \rangle \langle VDeclS \rangle ;$
 $\langle FModS \rangle \rightarrow \langle FModS \rangle \langle FMod \rangle | \epsilon$
 $\langle FMod \rangle \rightarrow public | final | static | transient | \dots$
 $\langle Type \rangle \rightarrow \langle NonVoidType \rangle$
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Gosling et al. [1996]

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Parsing JAVA Declarations

Example

```
public    final    static    int   FIELD = 10 ;  
  
$ || public final static int FIELD = 10;$
```

Parsing JAVA Declarations

Example

FModS

|
ε public final static int FIELD = 10 ;

\$ε || public final static int FIELD = 10;\$

≡_{reduce} \$<FModS> || public final static int FIELD = 10;\$

Parsing JAVA Declarations

Example

FModS

|
ε public final static int FIELD = 10 ;

\$ <FModS> || public final static int FIELD = 10;\$

⤻ shift \$ <FModS> public || final static int FIELD = 10;\$

Parsing JAVA Declarations

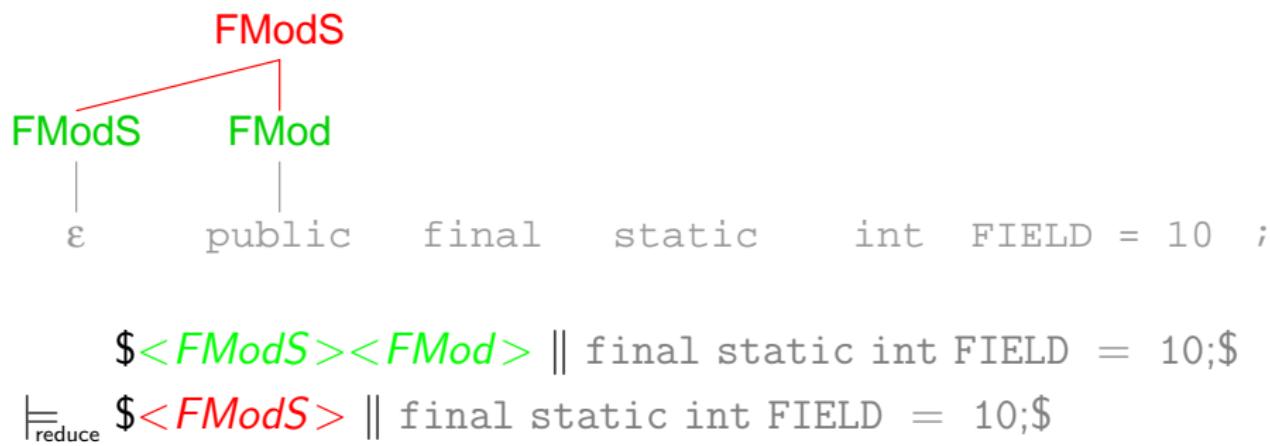
Example

$FModS$ $FMod$
| |
 ϵ public final static int FIELD = 10 ;

$\$ <FModS>$ public || final static int FIELD = 10;\$
 \models_{reduce} \$ $<FModS>$ $<FMod>$ || final static int FIELD = 10;\$

Parsing JAVA Declarations

Example



Parsing JAVA Declarations

Example



$\$ <FModS> \parallel \text{final static int FIELD} = 10; \$$

$\sqsubseteq_{\text{shift}} \$ <FModS> \text{ final} \parallel \text{static int FIELD} = 10; \$$

Parsing JAVA Declarations

Example

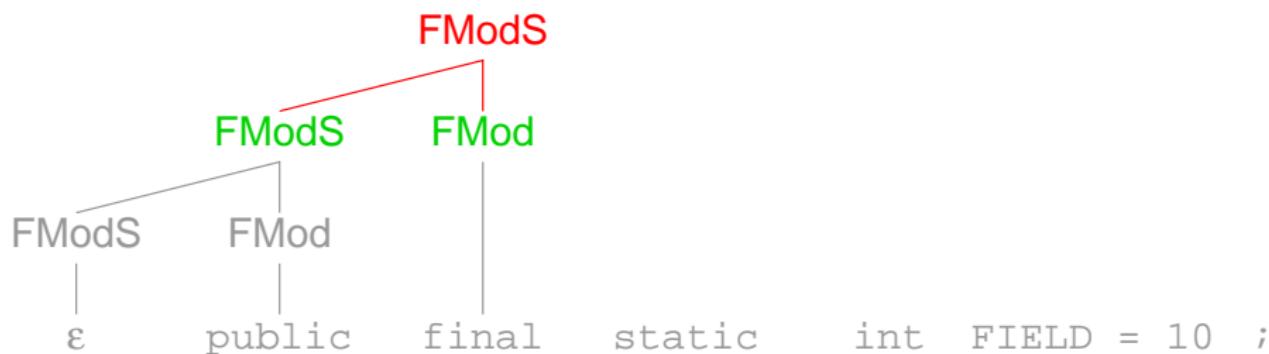


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Parsing JAVA Declarations

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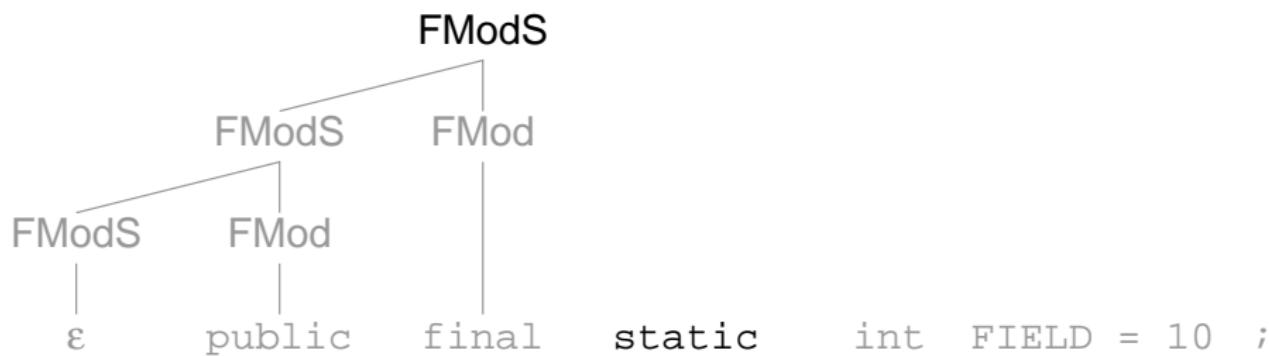


$\$ <FModS><FMod> \parallel \text{static int } \text{FIELD} = 10; \$$

$\models_{\text{reduce}} \$ <FModS> \parallel \text{static int } \text{FIELD} = 10; \$$

Parsing JAVA Declarations

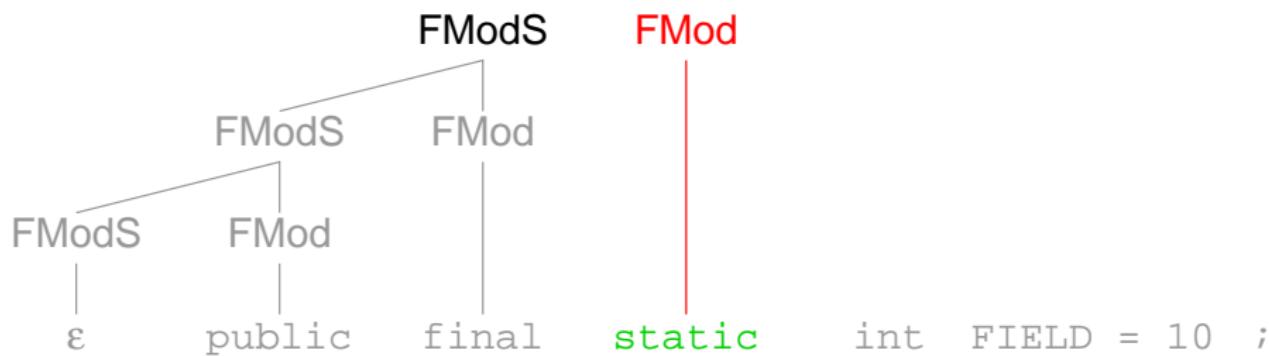
Example



$\$ <FModS> \parallel static int FIELD = 10; \$$
 $\sqsubseteq_{shift} \$ <FModS> static \parallel int FIELD = 10; \$$

Parsing JAVA Declarations

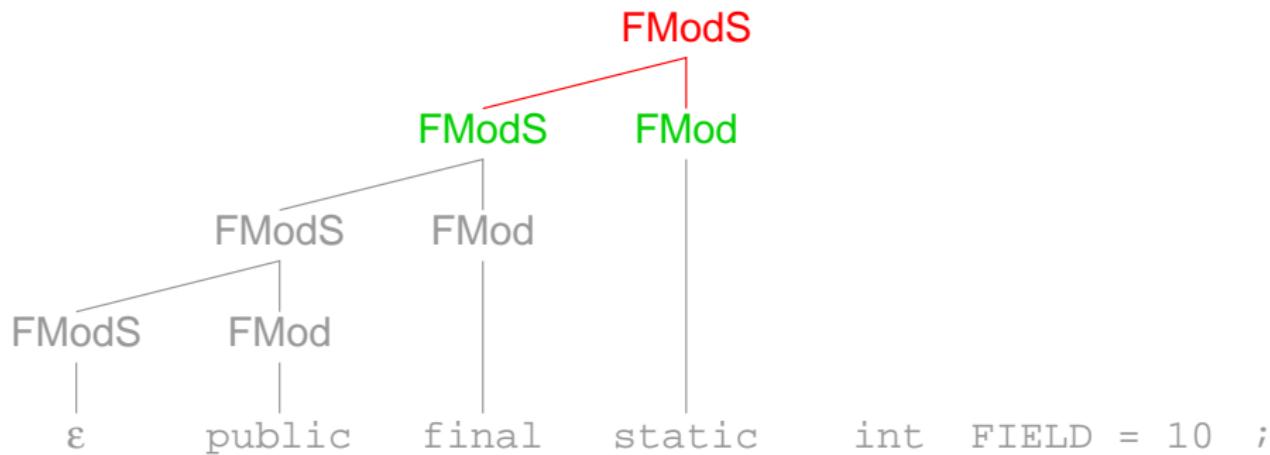
Example



$$\begin{aligned}
 & \$ <FModS> \text{ static } || \text{ int } \text{ FIELD } = 10; \$ \\
 \models_{\text{reduce}} & \$ <FModS> <\text{FMod}> || \text{ int } \text{ FIELD } = 10; \$
 \end{aligned}$$

Parsing JAVA Declarations

Example

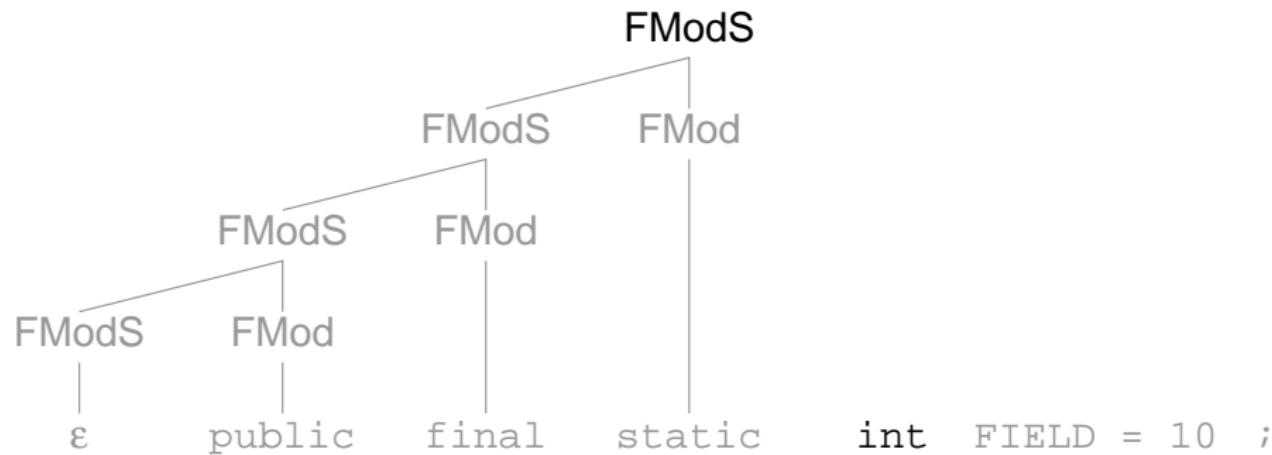


$\$ <FModS> <FMod> \parallel \text{int FIELD} = 10; \$$

$\models_{\text{reduce}} \$ <FModS> \parallel \text{int FIELD} = 10; \$$

Parsing JAVA Declarations

Example

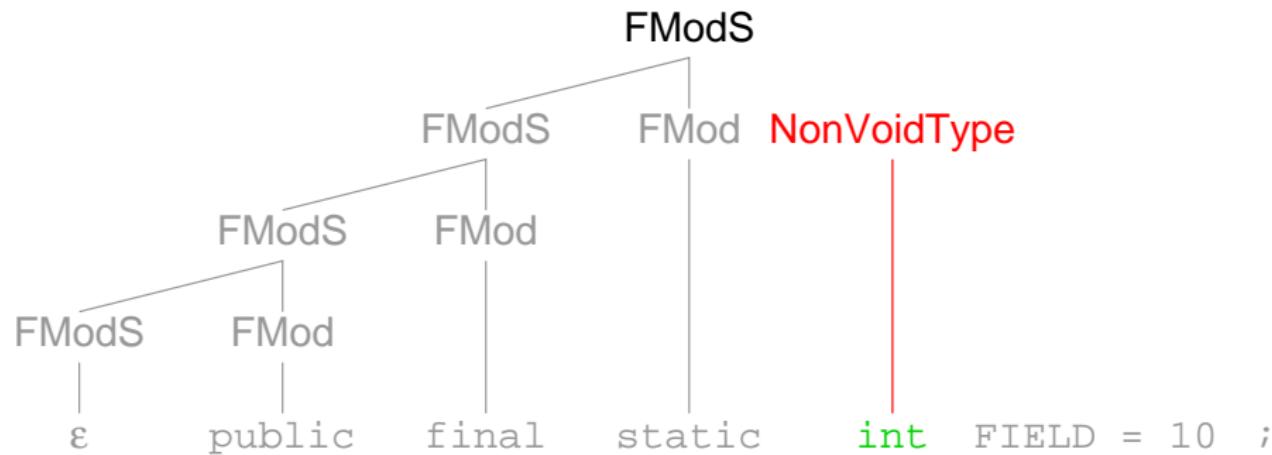


$\$ <FModS> \parallel \text{int } \text{FIELD} = 10; \$$

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Parsing JAVA Declarations

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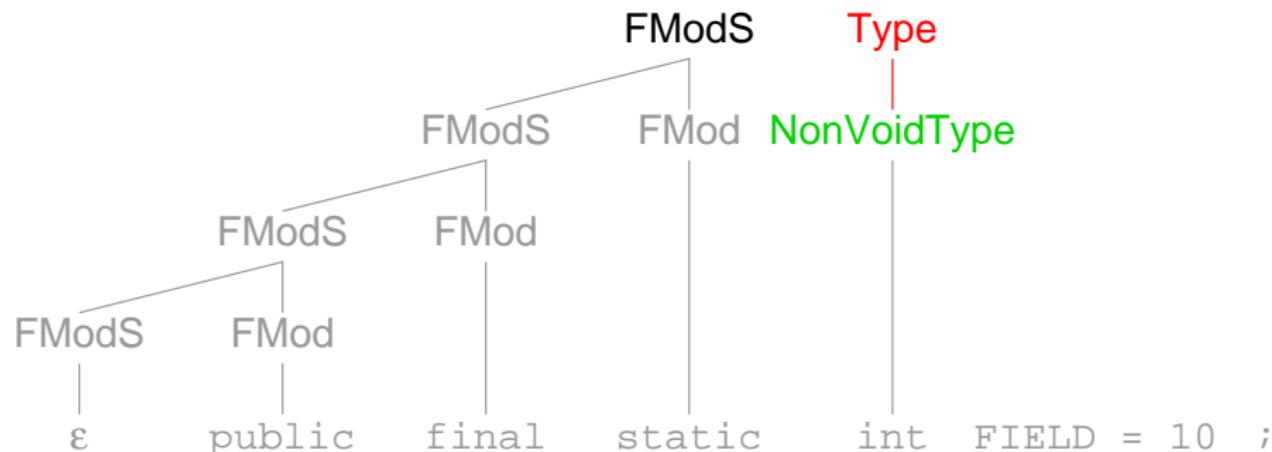


$$\$ <FModS> \text{int} \parallel \text{FIELD} = 10; \$$$

$$\models_{\text{reduce}} \$ <FModS> <\text{NonVoidType}> \parallel \text{FIELD} = 10; \$$$

Parsing JAVA Declarations

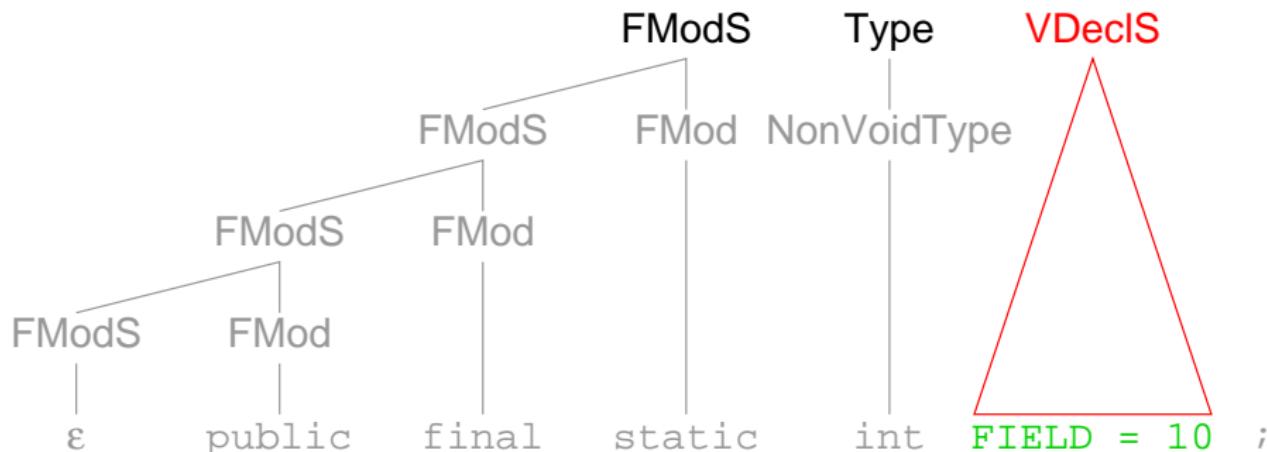
Example



$$\begin{aligned}
 & \$ <FModS> <\text{NonVoidType}> \parallel \text{FIELD} = 10; \$ \\
 \equiv_{\text{reduce}} & \$ <FModS> <\text{Type}> \parallel \text{FIELD} = 10; \$
 \end{aligned}$$

Parsing JAVA Declarations

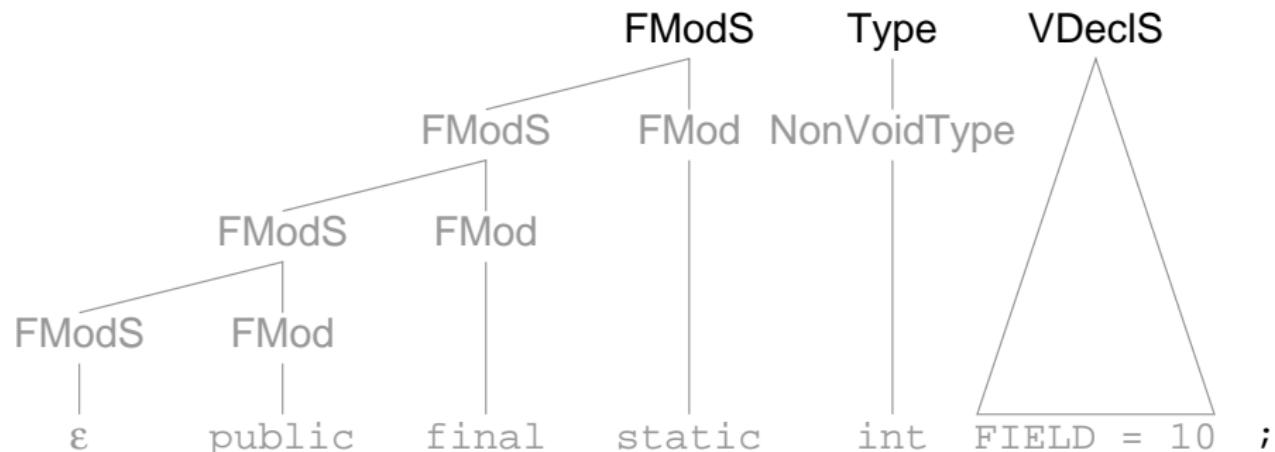
Example



$$\begin{aligned}
 & \$ <FModS><Type> \textcolor{red}{FIELD} \text{ } = \text{ } 10 \parallel ; \$ \\
 \equiv_{\text{reduce}} & \$ <FModS><Type> <\textcolor{red}{VDeclS}> \parallel ; \$
 \end{aligned}$$

Parsing JAVA Declarations

Example

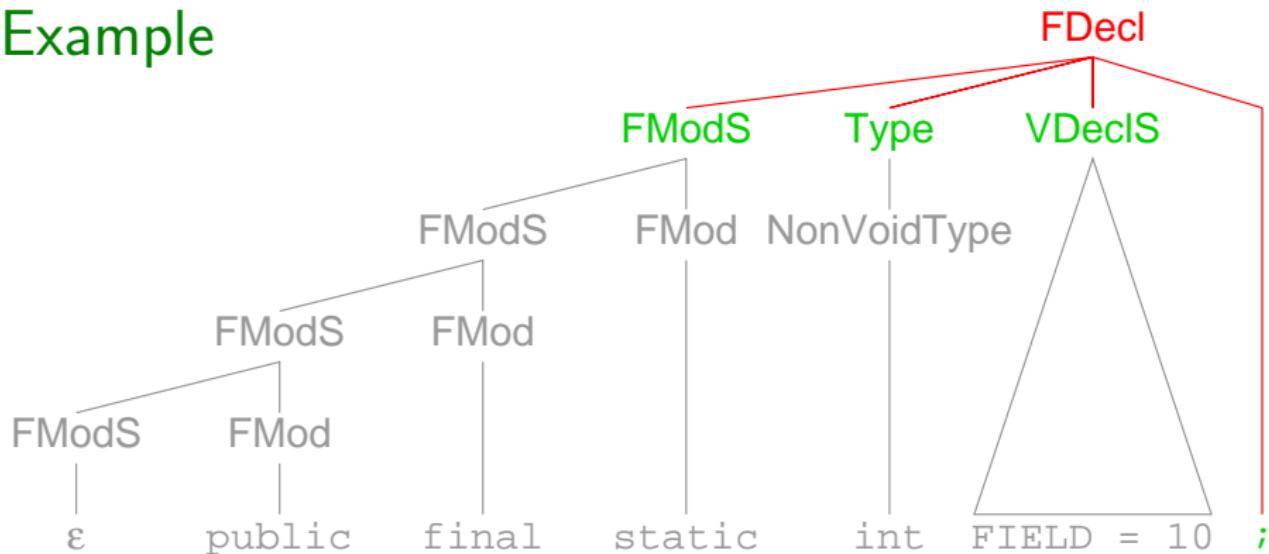


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$\models_{shift} \$ <FModS><Type><VDecIS> ; \parallel \$$

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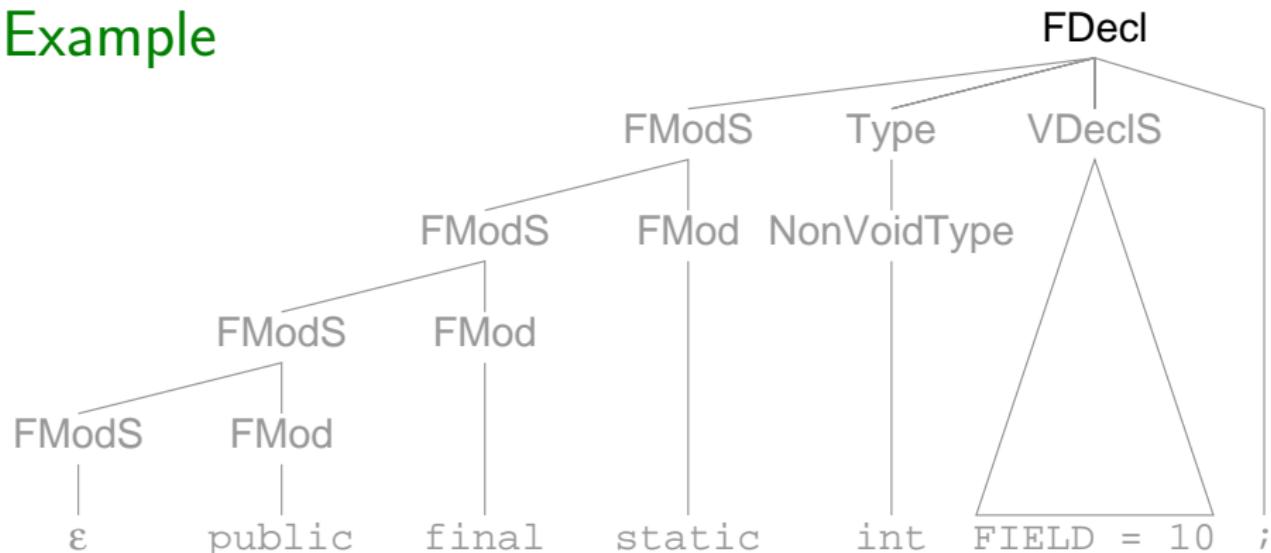


$\$ <FModS><Type><VDeclS> ; \parallel \$$

$\models_{\text{reduce}} \$ <FDecl> \parallel \$$

Parsing JAVA Declarations

Example



$\$ <FDecl> \parallel \$$

Nondeterminism

Example

```
public    final    static    int    FIELD = 10 ;  
  
$ || public final static int FIELD = 10;$
```

Nondeterminism

Example

MModS

|
 ϵ public final static int FIELD = 10 ;

$\$ \epsilon \parallel \text{public final static int FIELD} = 10; \$$

$\vdash_{\text{reduce}} \$ <\!MModS\!> \parallel \text{public final static int FIELD} = 10; \$$

Nondeterminism

Example

MModS

|
 ϵ public final static int FIELD = 10 ;

$\$ < MModS > \parallel \text{public final static int FIELD} = 10 ; \$$
 $\vdash_{\text{shift}} \$ < MModS > \text{public} \parallel \text{final static int FIELD} = 10 ; \$$

Nondeterminism

Example

MModS FMod
| |
 ϵ public final static int FIELD = 10 ;

$\$ <MModS> \text{public} \parallel \text{final static int FIELD} = 10; \$$
 $\vdash_{\text{reduce}} \$ <MModS> <\text{FMod}> \parallel \text{final static int FIELD} = 10; \$$

Nondeterminism

Example

error!



Nondeterminism

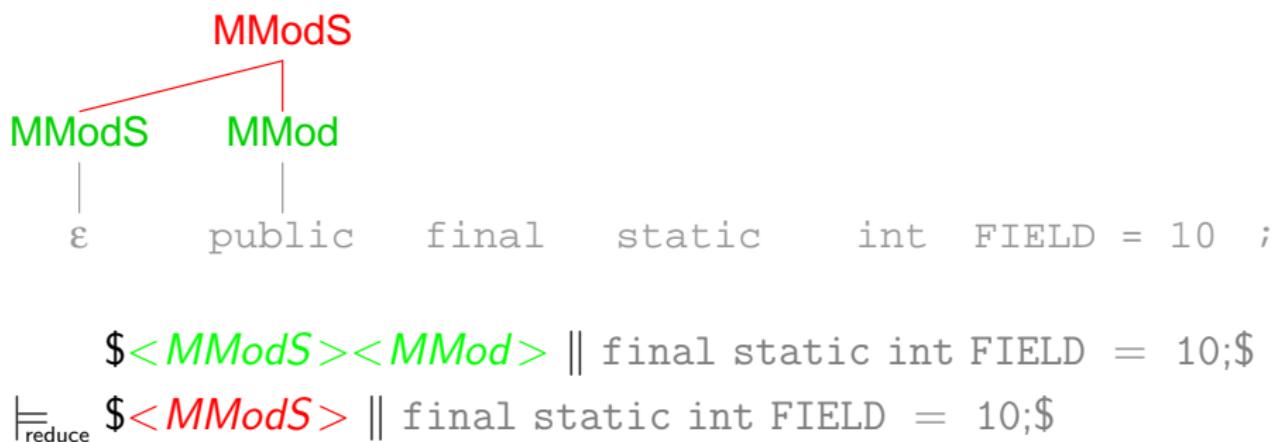
Example

MModS **MMod**
| |
 ϵ public final static int FIELD = 10 ;

$\$ <MModS> \text{public} \parallel \text{final static int FIELD} = 10; \$$
 $\vdash_{\text{reduce}} \$ <MModS> <\text{MMod}> \parallel \text{final static int FIELD} = 10; \$$

Nondeterminism

Example



Nondeterminism

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Nondeterminism

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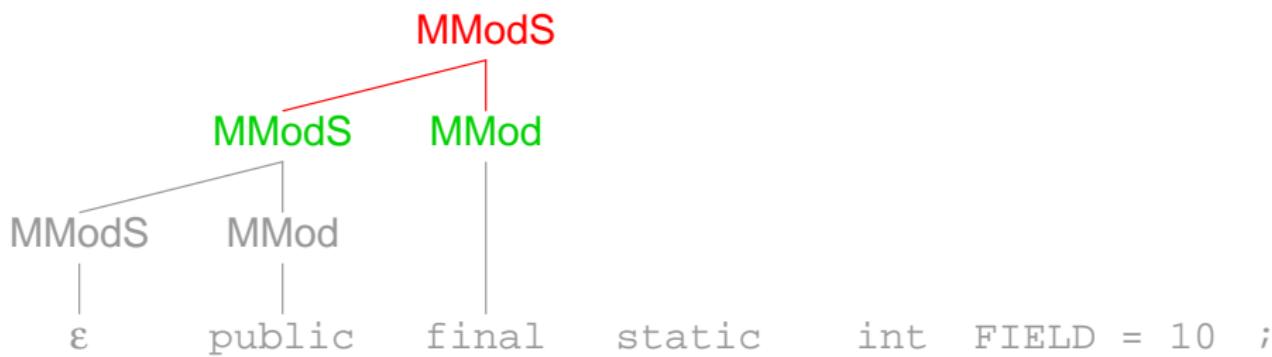


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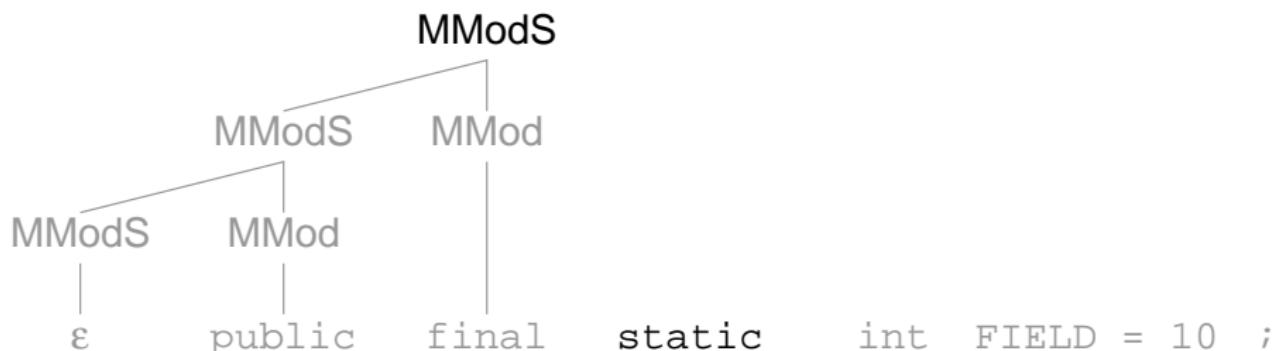


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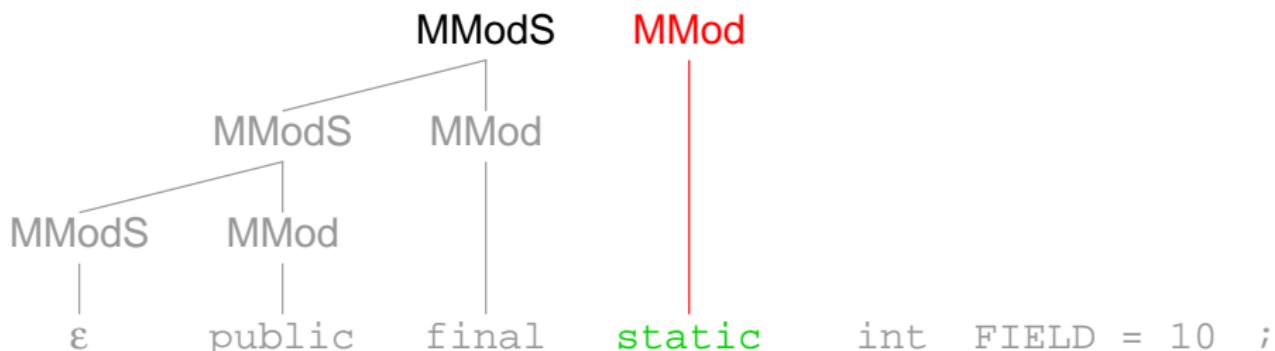


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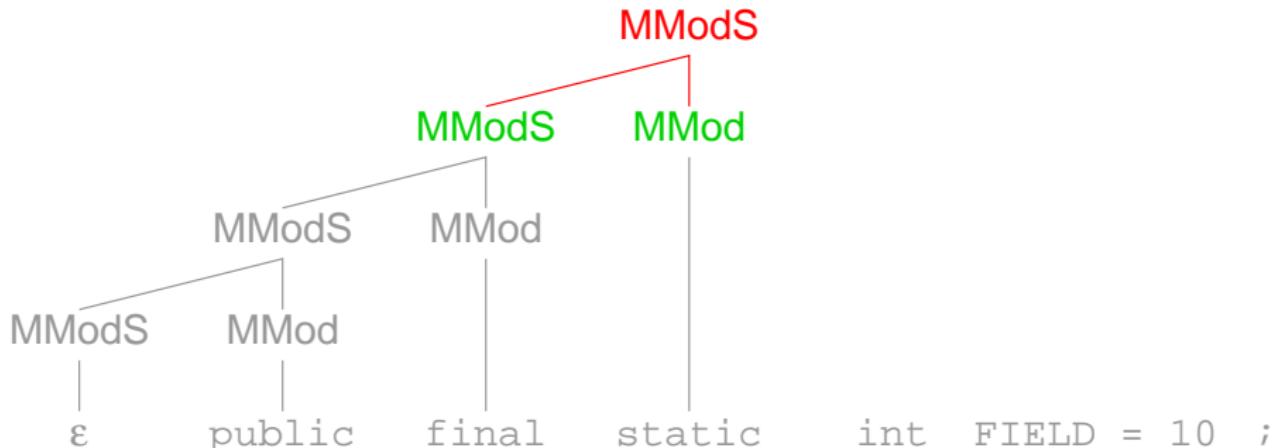
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Nondeterminism

Example

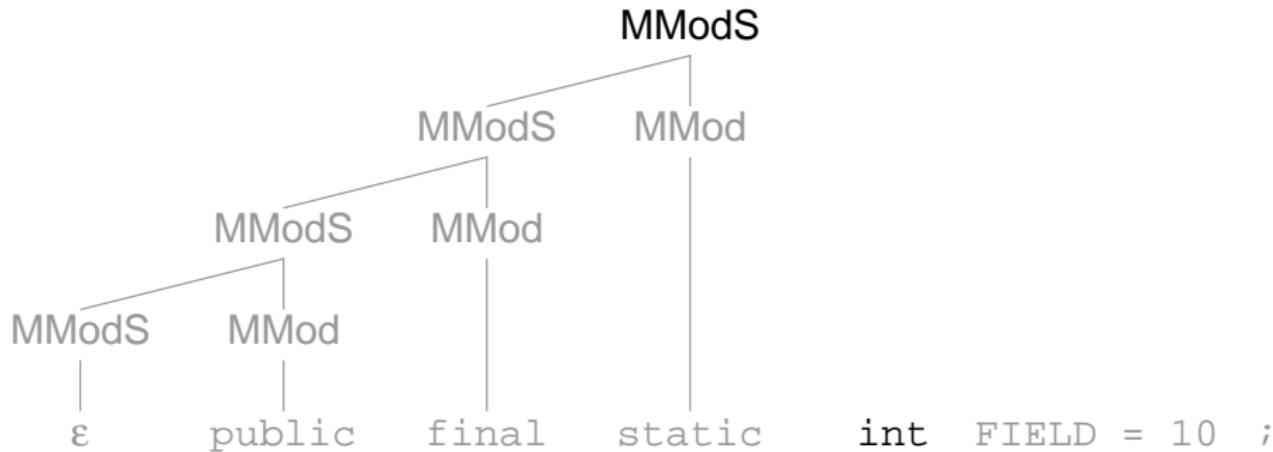


$\$ <MModS> <MMod> \parallel \text{int FIELD} = 10; \$$

$\vdash_{\text{reduce}} \$ <MModS> \parallel \text{int FIELD} = 10; \$$

Nondeterminism

Example

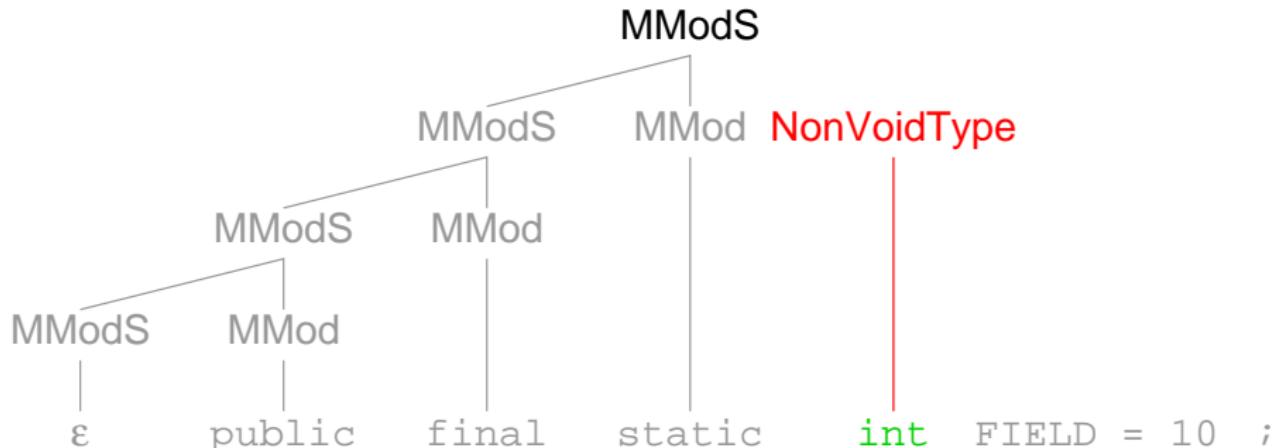


$\$ < MModS > \parallel \text{int FIELD} = 10; \$$

$\models_{\text{shift}} \$ < MModS > \text{int} \parallel \text{FIELD} = 10; \$$

Nondeterminism

Example

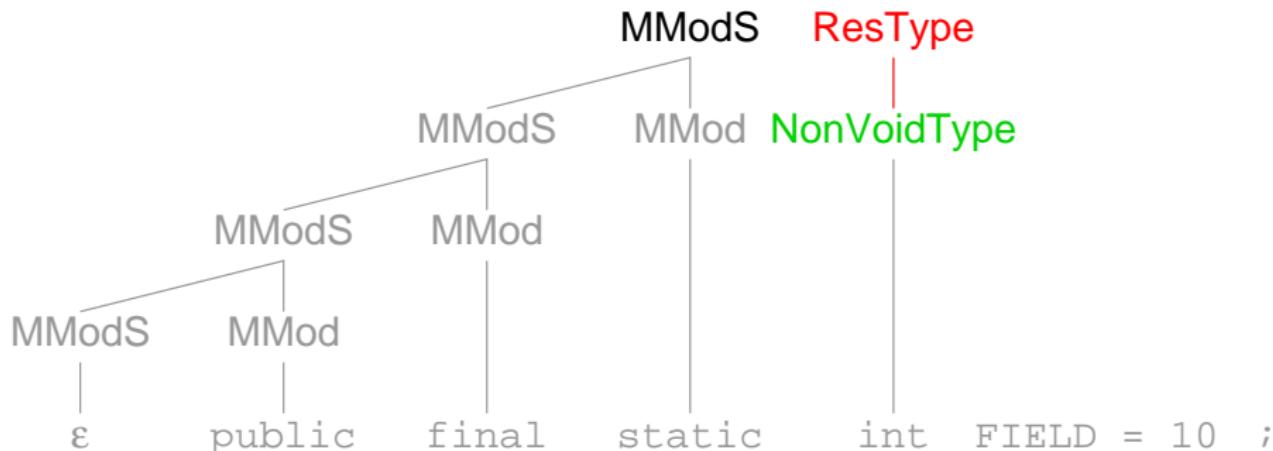


$\$ < MModS > \text{int} \parallel \text{FIELD} = 10; \$$

$\vdash_{\text{reduce}} \$ < MModS > < \text{NonVoidType} > \parallel \text{FIELD} = 10; \$$

Nondeterminism

Example

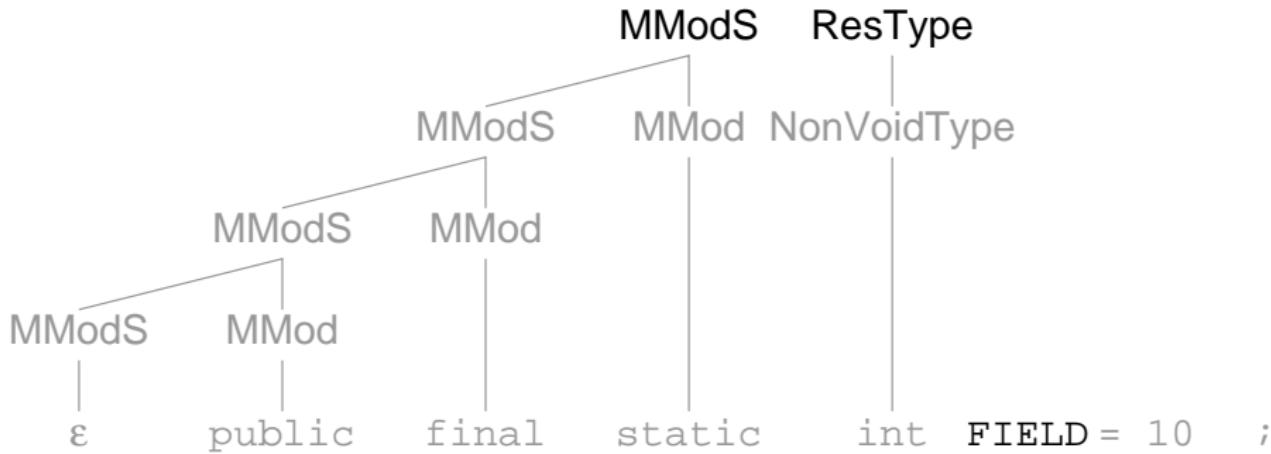


$\$ < MModS > < \text{NonVoidType} > \| \text{FIELD} = 10; \$$

$\vdash_{\text{reduce}} \$ < MModS > < \text{ResType} > \| \text{FIELD} = 10; \$$

Nondeterminism

Example

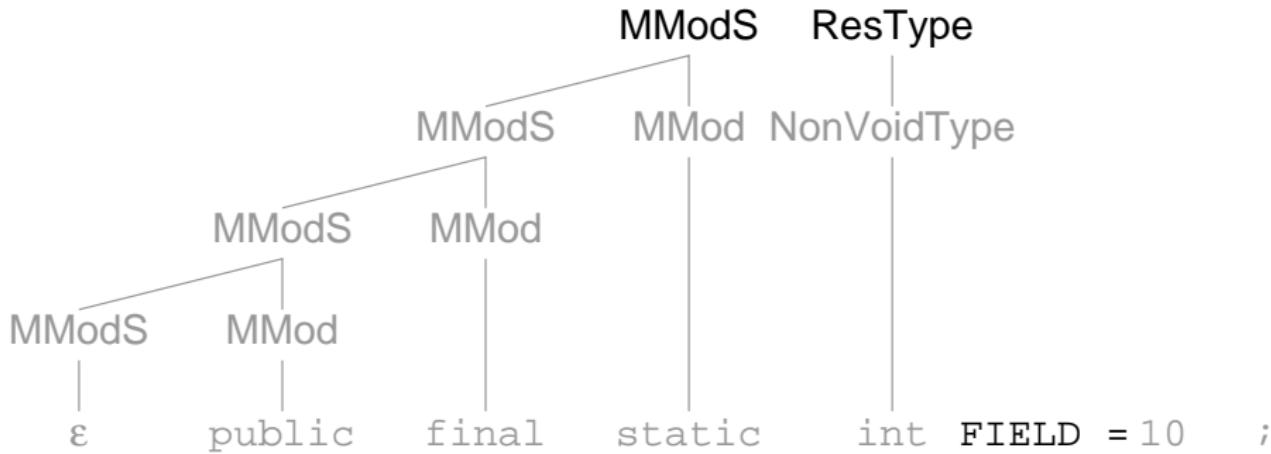


$\$ < MModS > < ResType > \parallel FIELD = 10; \$$

$\models_{shift} \$ < MModS > < ResType > FIELD \parallel = 10; \$$

Nondeterminism

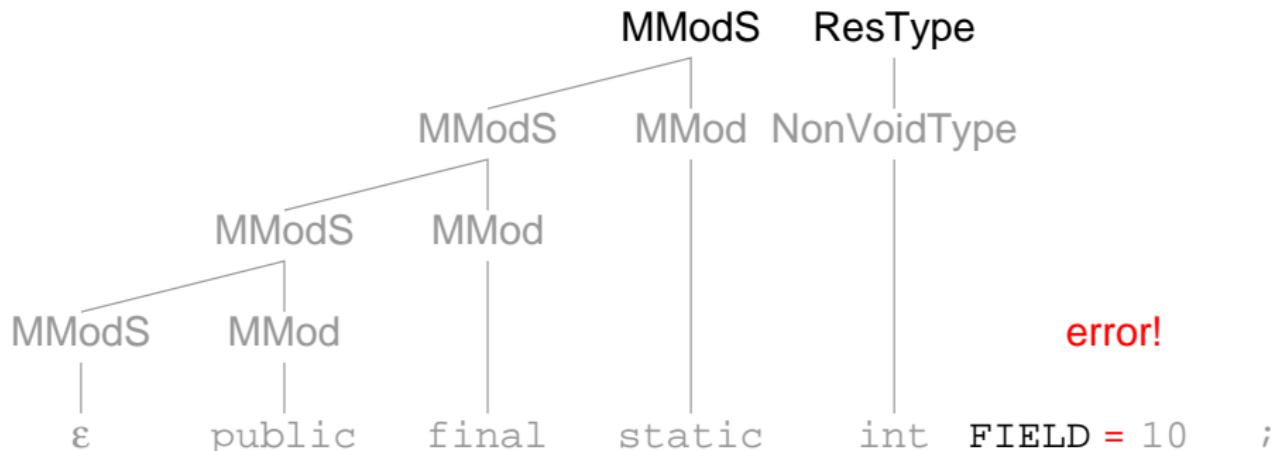
Example



$\$ < MModS > < ResType > FIELD = 10; \$$
 $\models_{shift} \$ < MModS > < ResType > FIELD = \$$

Nondeterminism

Example



$\$ <MModS><ResType> FIELD = || 10; \$$

Nondeterminism

Example

FModS

|
 ϵ public final static int FIELD = 10 ;

$\$ \epsilon \parallel \text{public final static int FIELD} = 10; \$$

$\models_{\text{reduce}} \$ <\!FModS\!> \parallel \text{public final static int FIELD} = 10; \$$

Why Determinism Matters

+ Performance

+ Safety

- Generality

LR(k) Parsing

Knuth [1965]

- ▶ complete stack information
- ▶ k symbols of lookahead

Example

Choice between reductions $\langle FModS \rangle \rightarrow \varepsilon$ and $\langle MModS \rangle \rightarrow \varepsilon$:

```
||public static final ... final static int l =  
||public static final ... final static int l (
```

- ▶ Infinite lookahead needed for better generality

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Example

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```
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```

- ▶ Infinite lookahead needed for better generality

Syntactic Predicates

Parr and Quong [1995]

- ▶ User defined lookahead pattern

Example

((MMod)* ResType MDecl)?

- ▶ Error-prone
- ▶ Exponential time complexity

Syntactic Predicates

Parr and Quong [1995]

- ▶ User defined lookahead pattern

Example

$$((MMod)^* \text{ ResType } MDecl)?$$

- ▶ Error-prone
- ▶ Exponential time complexity

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Parr and Quong [1995]

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Example

$$((MMod)^* \text{ ResType } MDecl)?$$

- ▶ Error-prone
- ▶ Exponential time complexity

LR-Regular Parsing

Baker [1981], Bermudez and Schimpf [1990], Farré and Fortes Gálvez [2001]

- ▶ Finite State lookahead discrimination

- ▶ $\mathcal{O}(n^2)$ time complexity

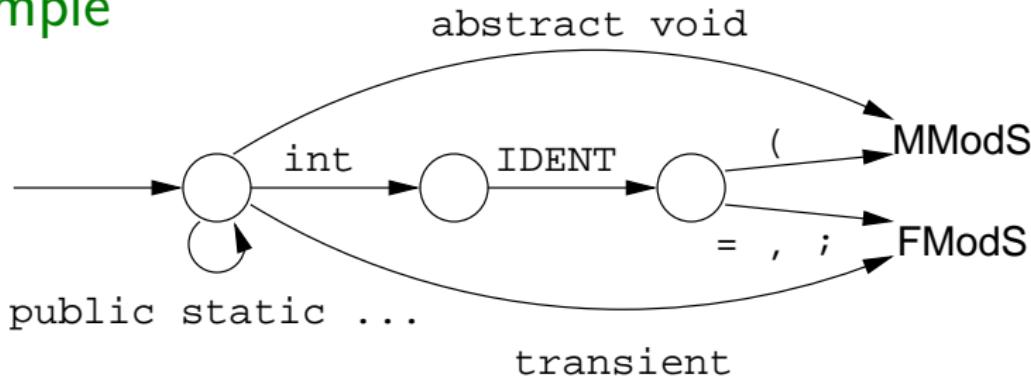
- ▶ Only considers terminal symbols

LR-Regular Parsing

Baker [1981], Bermudez and Schimpf [1990], Farré and Fortes Gálvez [2001]

- ▶ Finite State lookahead discrimination

Example



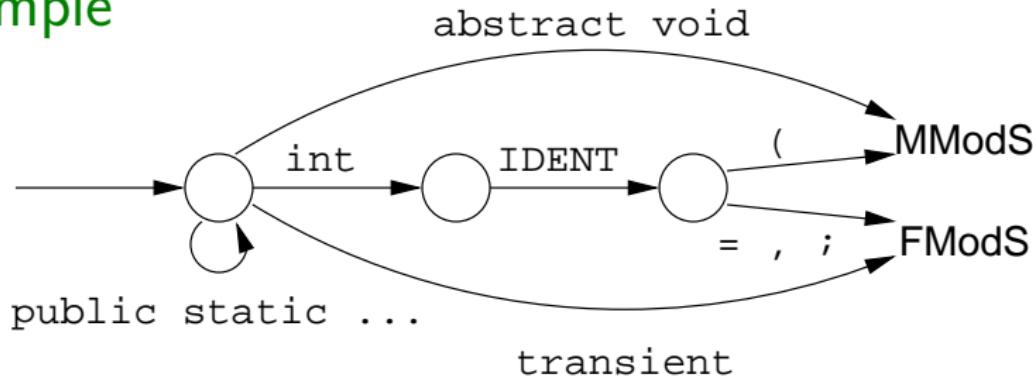
- ▶ $\mathcal{O}(n^2)$ time complexity
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Baker [1981], Bermudez and Schimpf [1990], Farré and Fortes Gálvez [2001]

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Example



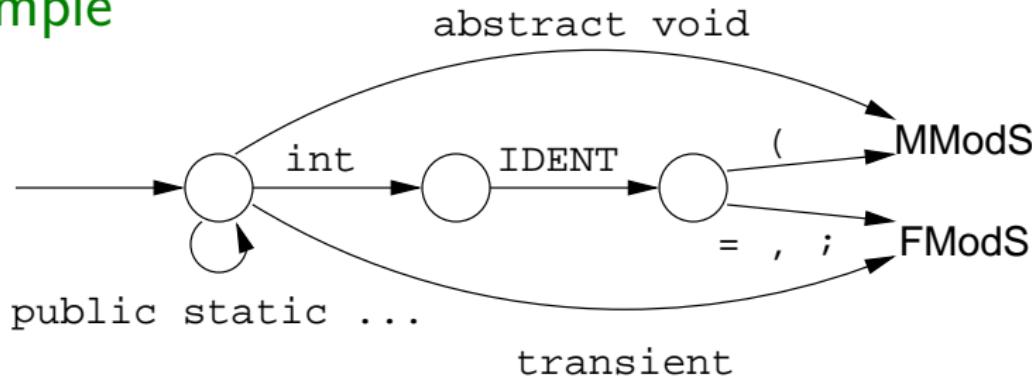
- ▶ $\mathcal{O}(n^2)$ time complexity
- ▶ Only considers terminal symbols

LR-Regular Parsing

Baker [1981], Bermudez and Schimpf [1990], Farré and Fortes Gálvez [2001]

- ▶ Finite State lookahead discrimination

Example



- ▶ $\mathcal{O}(n^2)$ time complexity
- ▶ Only considers terminal symbols

Parsing a Program Source

- ▶ Good generality
- ▶ Determinism
- ▶ $\mathcal{O}(n)$ time complexity

Parsing a Program Source

- ▶ Good generality
- ▶ Determinism
- ▶ $\mathcal{O}(n)$ time complexity

Noncanonical parsing

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example

```
public    final    static    int   FIELD = 10 ;
```

```
$ || public final static int FIELD = 10;$
```

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example

```
public    final    static    int   FIELD = 10 ;
```

```
$ || public final static int FIELD = 10;$  
|= $ public || final static int FIELD = 10;$
```

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example

```
public    final    static    int   FIELD = 10 ;
```

```
$public || final static int FIELD = 10;$  
|= $public final || static int FIELD = 10;$
```

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example

```
public    final    static    int   FIELD = 10 ;
```

```
$public final || static int FIELD = 10;$  
|= $public final static || int FIELD = 10;$
```

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example

```
public    final    static    int   FIELD = 10 ;
```

```
$public final static || int FIELD = 10;$  
|= $public final static int || FIELD = 10;$
```

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example

NonVoidType

```
public final static int FIELD = 10 ;
```

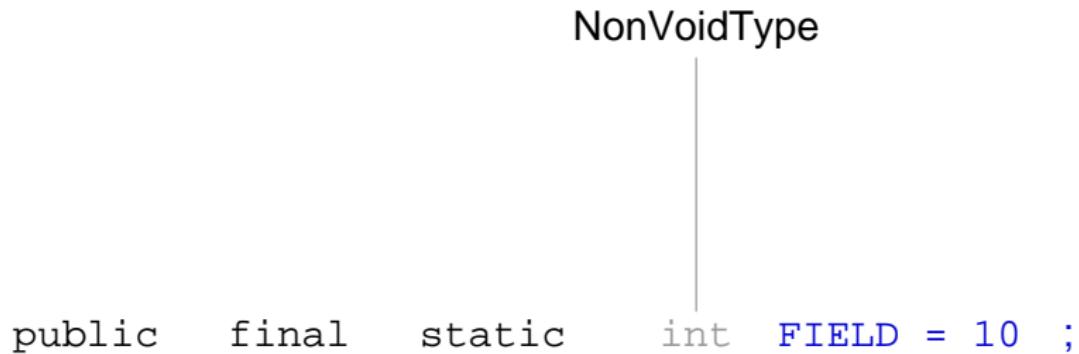
\$public final static int || FIELD = 10;\$

\models_{reduce} \$public final static || <NonVoidType> FIELD = 10;\$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example

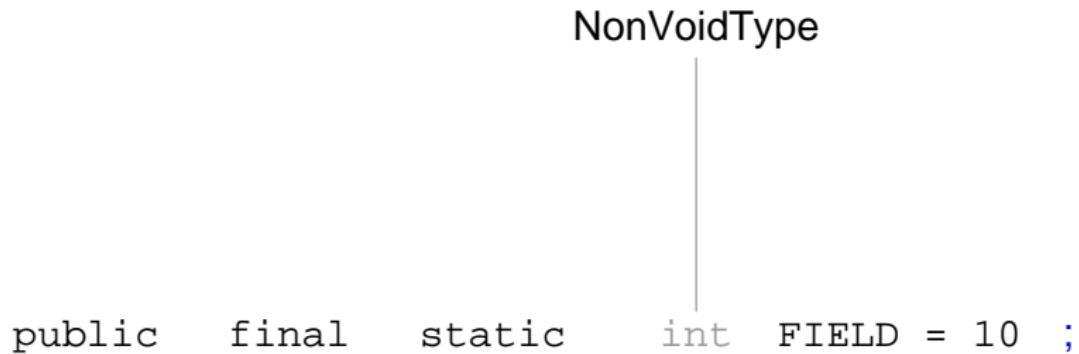


```
$public final static || <NonVoidType> FIELD = 10;$  
|= $public final static <NonVoidType> || FIELD = 10;$
```

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example

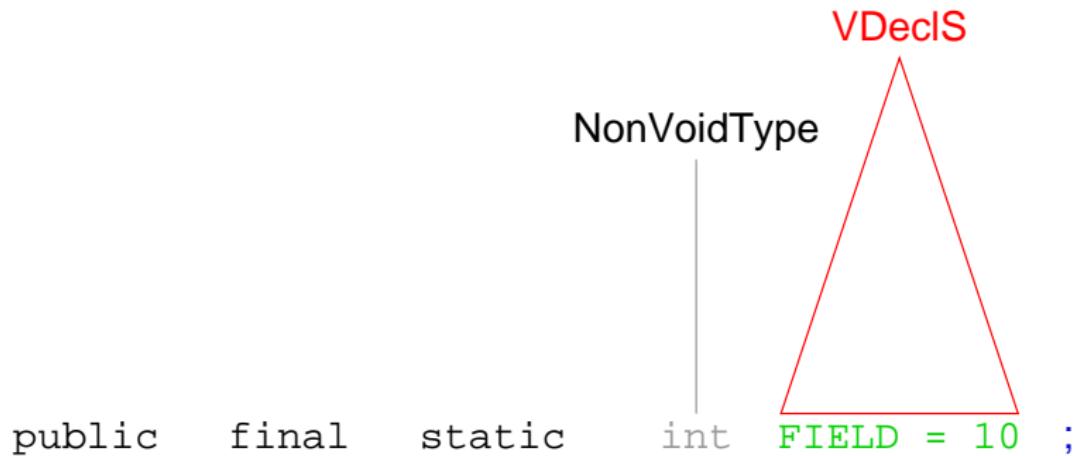


```
$public final static <NonVoidType> || FIELD = 10 ;$  
|= $public final static <NonVoidType> FIELD = 10 || ;$
```

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example

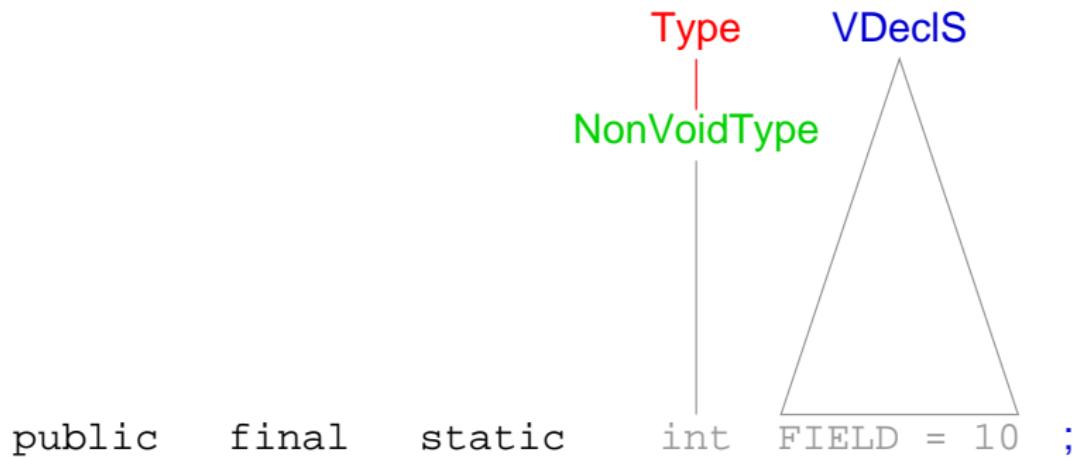


\$public final static <NonVoidType> FIELD = 10 ;\$
|= \$public final static <NonVoidType> || <VDeclS> ;\$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example



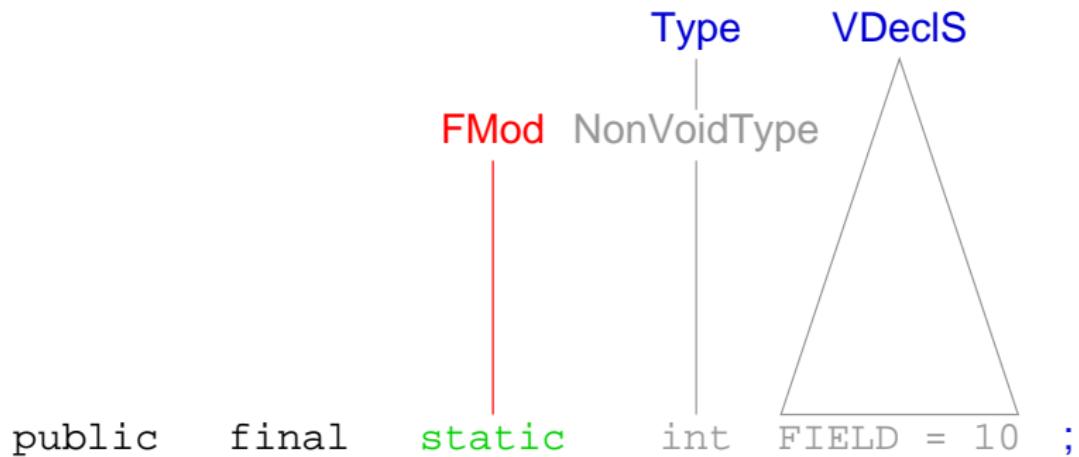
$\$public\ final\ static\ <NonVoidType>\ ||\ <VDeclS>\ ;\$$

$\models_{reduce} \$public\ final\ static\ ||\ <Type>\ <VDeclS>\ ;\$$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example

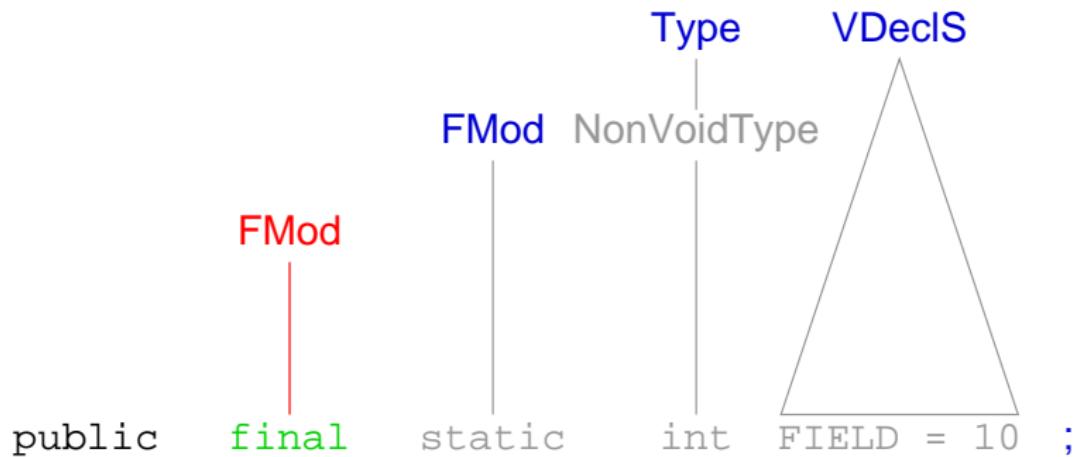


$\$public\ final\ static\ ||\ <Type><VDeclS>\ ;\$$
 $\models_{reduce} \$public\ final\ ||\ <FMod>\ <Type><VDeclS>\ ;\$$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example



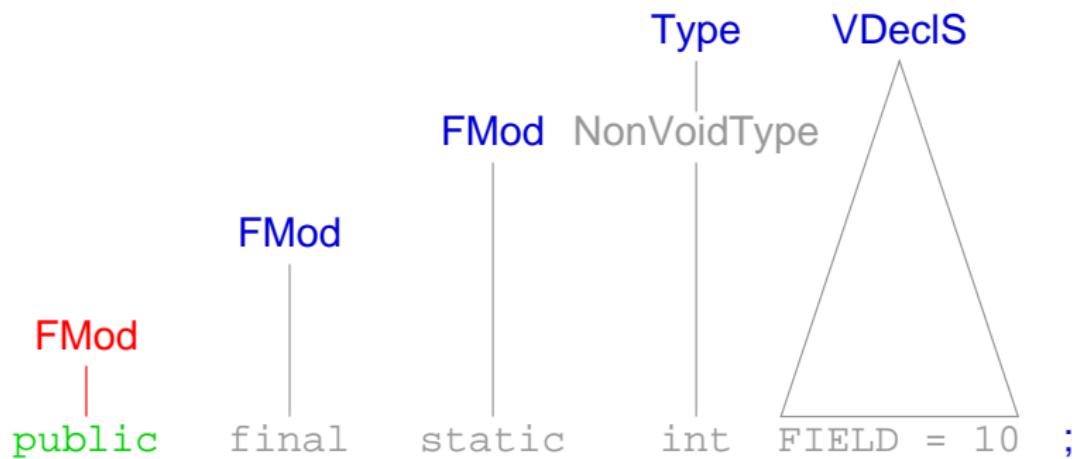
$\$public\ final\ ||\ <FMod><Type><VDecIS>\ ;\$$

$\models_{reduce} \$public\ ||\ <FMod>\ <FMod><Type><VDecIS>\ ;\$$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example



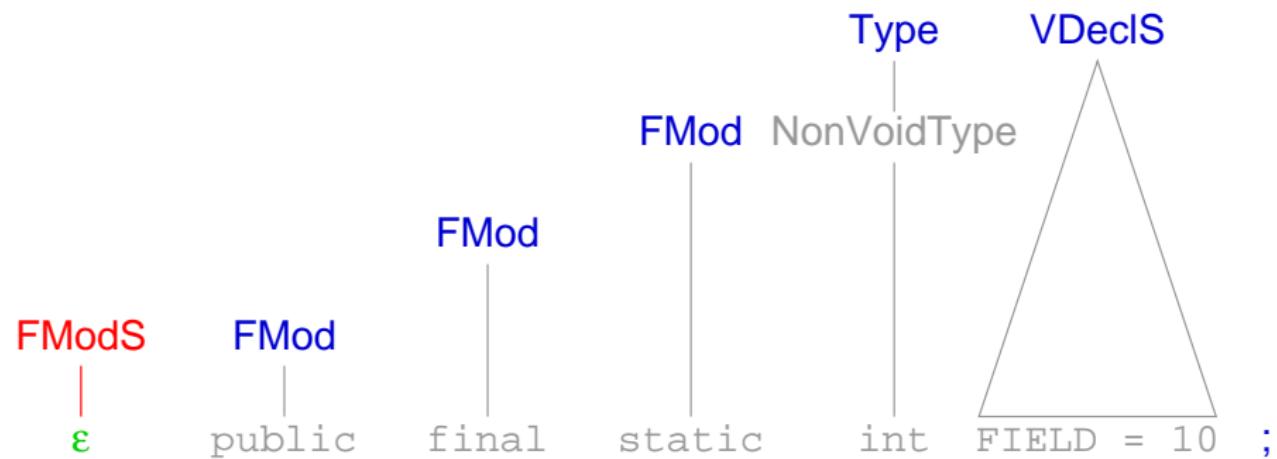
$\$ \text{public} \parallel <\text{FMod}><\text{FMod}><\text{Type}><\text{VDeclS}> ; \$$

$\vdash_{\text{reduce}} \$ \parallel <\text{FMod}> <\text{FMod}><\text{FMod}><\text{Type}><\text{VDeclS}> ; \$$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example



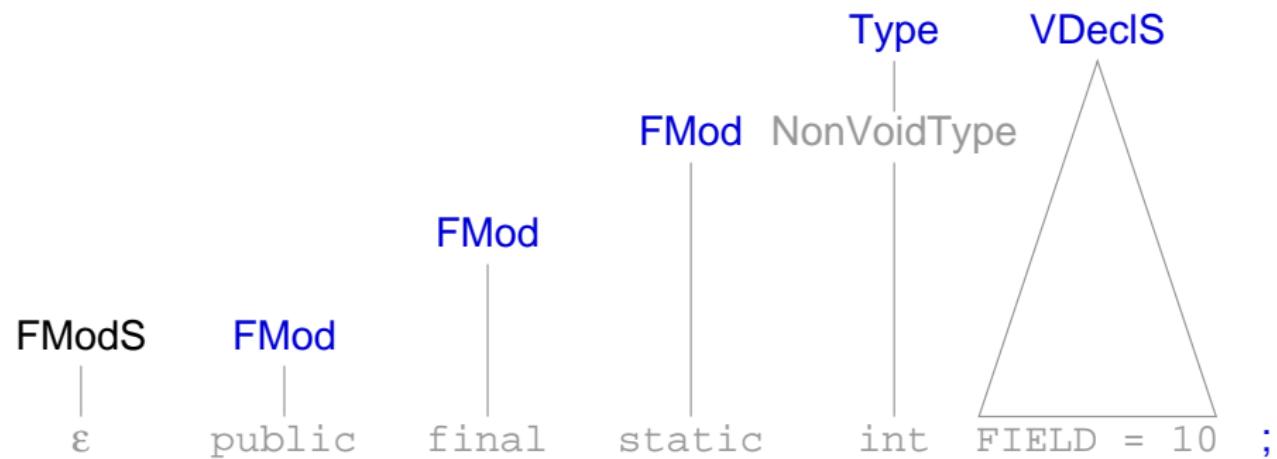
$\$ \epsilon \parallel < FMod > < FMod > < FMod > < Type > < VDeclS > ; \$$

$\vdash_{\text{reduce}} \$ \parallel < FModS > < FMod > < FMod > < FMod > < Type > < VDeclS >$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example



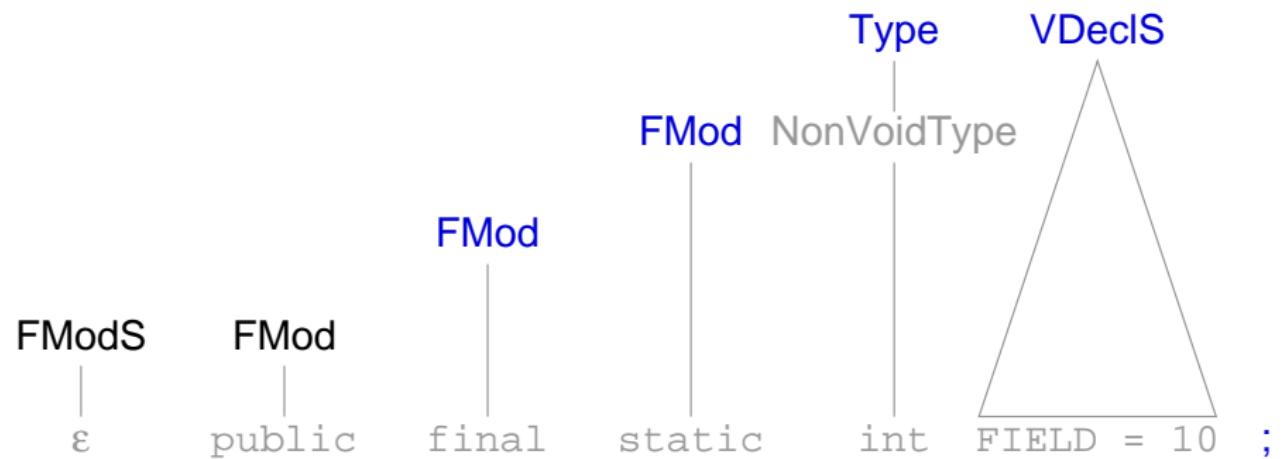
$\$ \parallel \langle FModS \rangle \langle FMod \rangle \langle FMod \rangle \langle FMod \rangle \langle Type \rangle \langle VDeclS \rangle$

$\Vdash_{shift} \$ \langle FModS \rangle \parallel \langle FMod \rangle \langle FMod \rangle \langle FMod \rangle \langle Type \rangle \langle VDeclS \rangle$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example

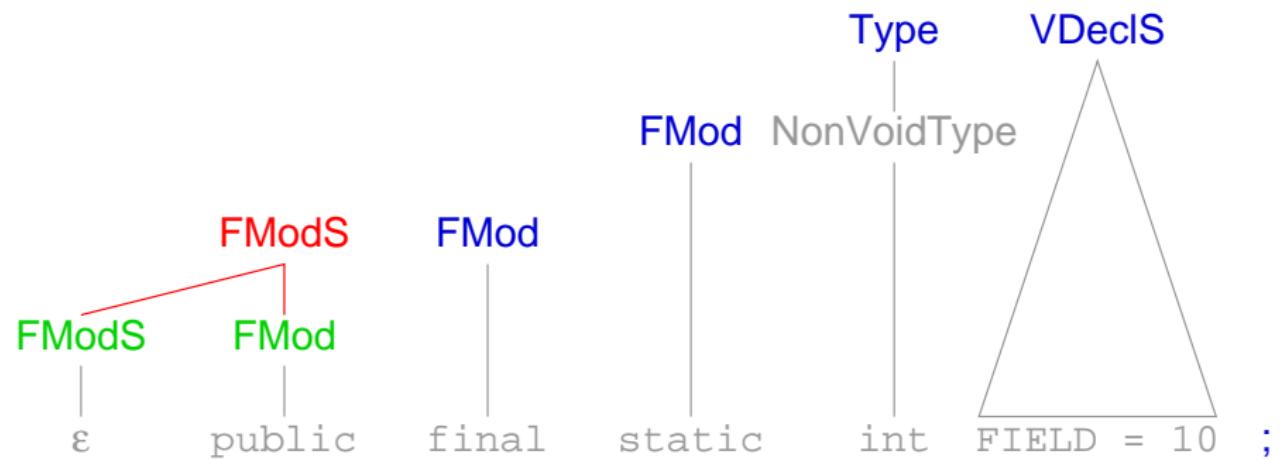


$\$ <FModS> \parallel <FMod> <FMod><FMod><Type><VDeclS>$
 $\vdash_{shift} \$ <FModS> <FMod> \parallel <FMod><FMod><Type><VDeclS>$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example

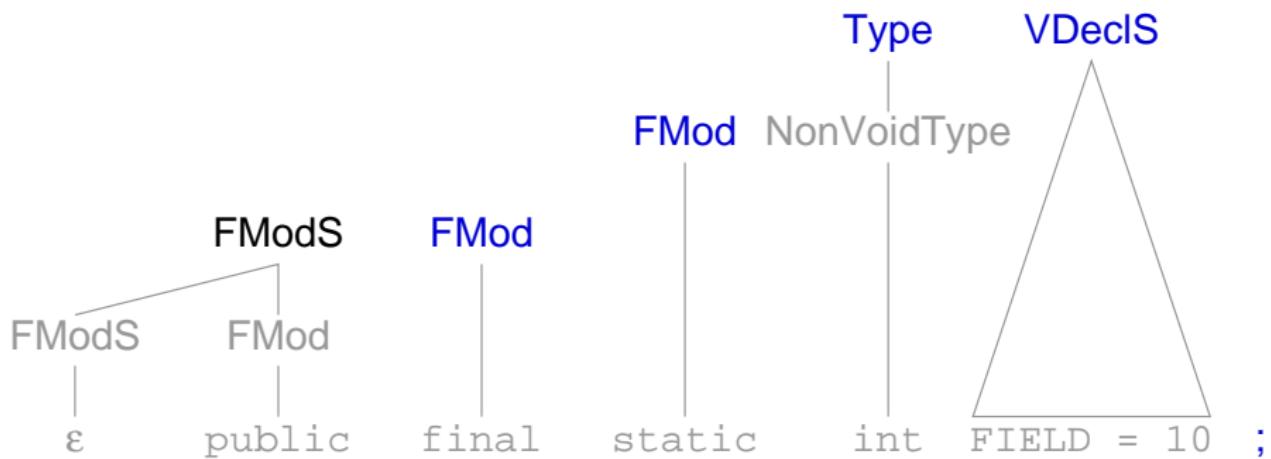


$\$ <FModS><FMod> \parallel <FMod><FMod><Type><VDeclS>$
 $\vdash_{\text{reduce}} \$ \parallel <FModS> <FMod><FMod><Type><VDeclS> ;\$$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example



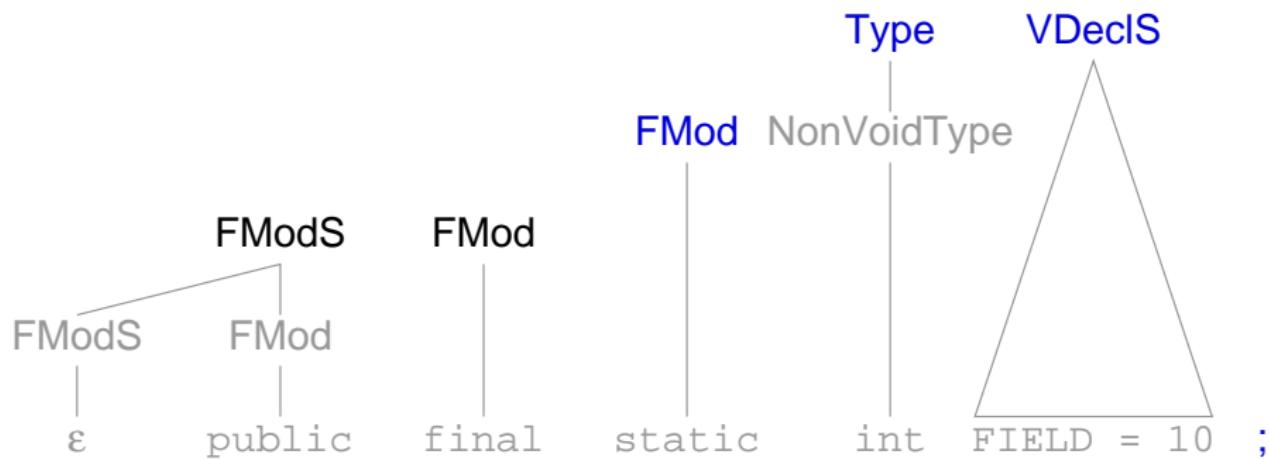
$\$ \parallel < FModS > < FMod > < FMod > < Type > < VDeclS > ; \$$

$\models_{shift} \$ < FModS > \parallel < FMod > < FMod > < Type > < VDeclS > ; \$$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example

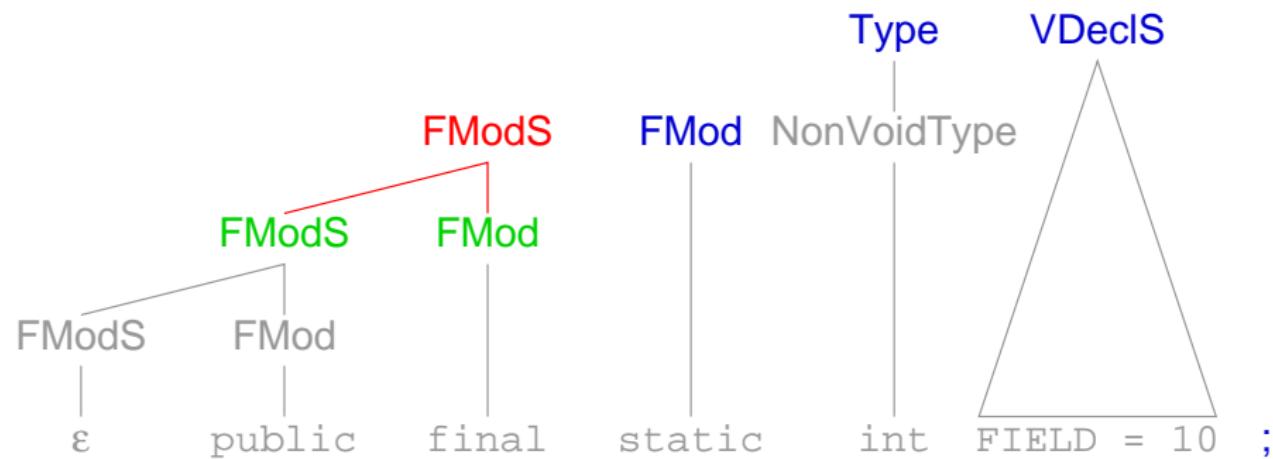


$\$ <FModS> \parallel <FMod> <FMod><Type><VDeclS> ; \$$
 $\models \$ <FModS> <FMod> \parallel <FMod><Type><VDeclS> ; \$$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example



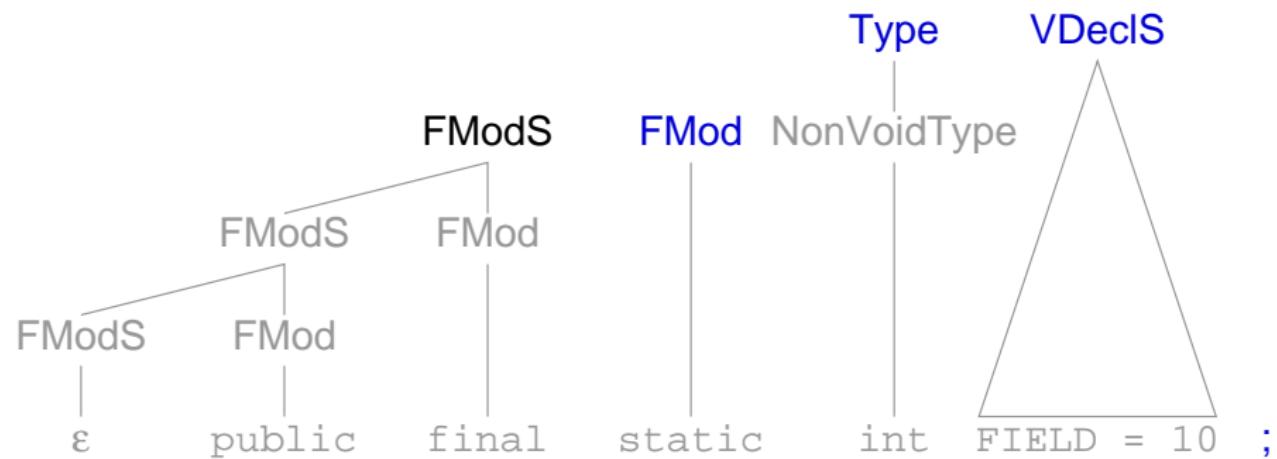
$\$ <FModS><FMod> \parallel <FMod><Type><VDeclS> ; \$$

$\vdash_{\text{reduce}} \$ \parallel <FModS> <FMod><Type><VDeclS> ; \$$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example

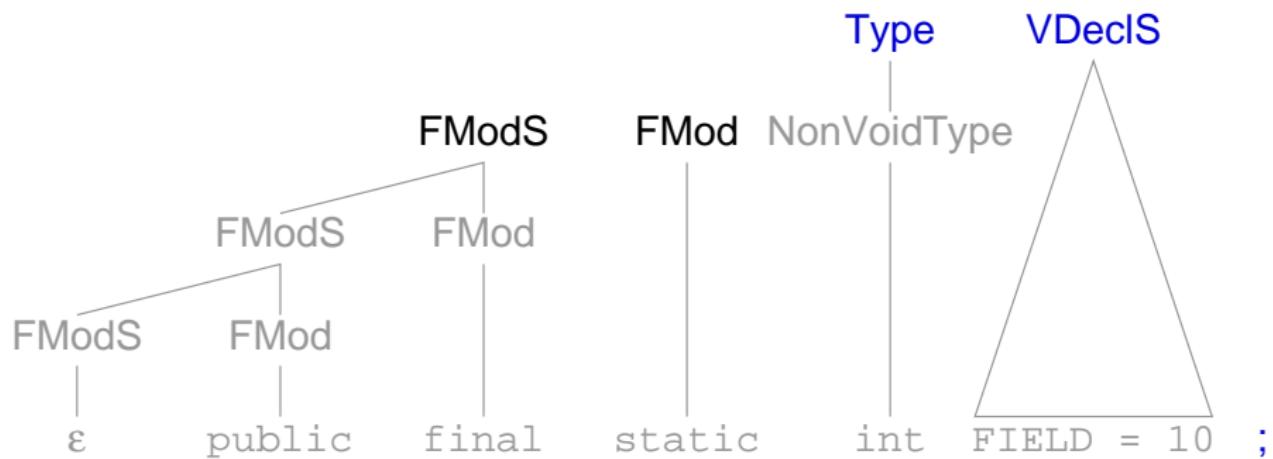


$\$ \parallel < FModS > < FMod > < Type > < VDeclS > ; \$$
 $\models \$ < FModS > \parallel < FMod > < Type > < VDeclS > ; \$$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example



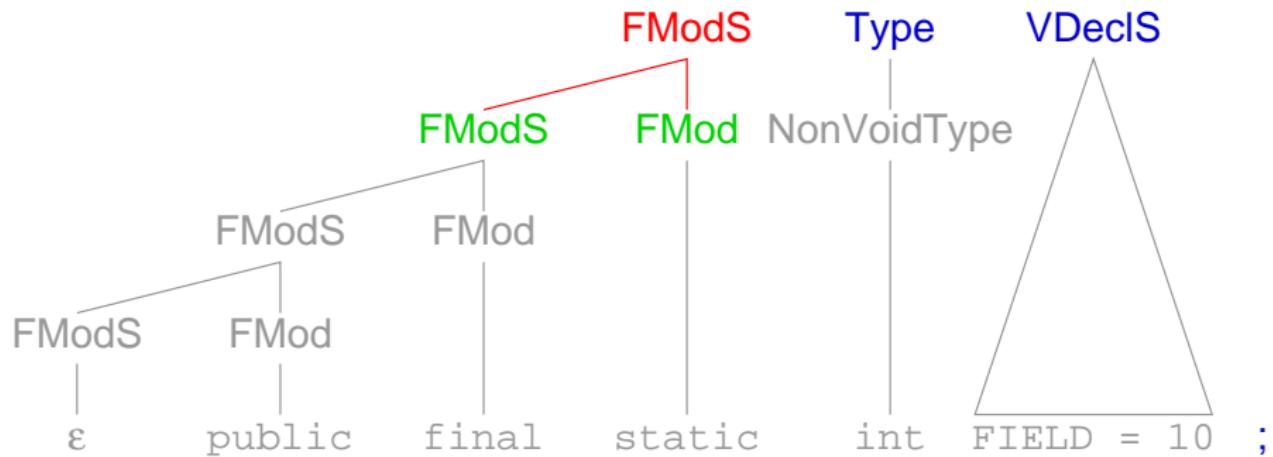
$\$ <FModS> \parallel <FMod> <Type><VDeclS> ; \$$

$\models_{shift} \$ <FModS> <FMod> \parallel <Type><VDeclS> ; \$$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example



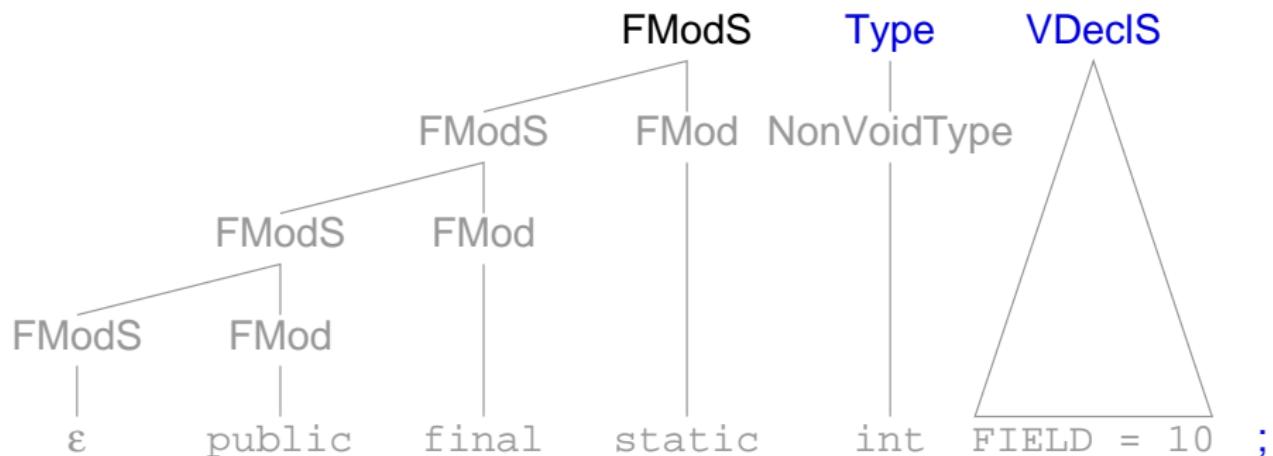
$\$ <FModS><FMod> \parallel <Type><VDeclS> ; \$$

$\models_{\text{reduce}} \$ \parallel <FModS> <Type><VDeclS> ; \$$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example

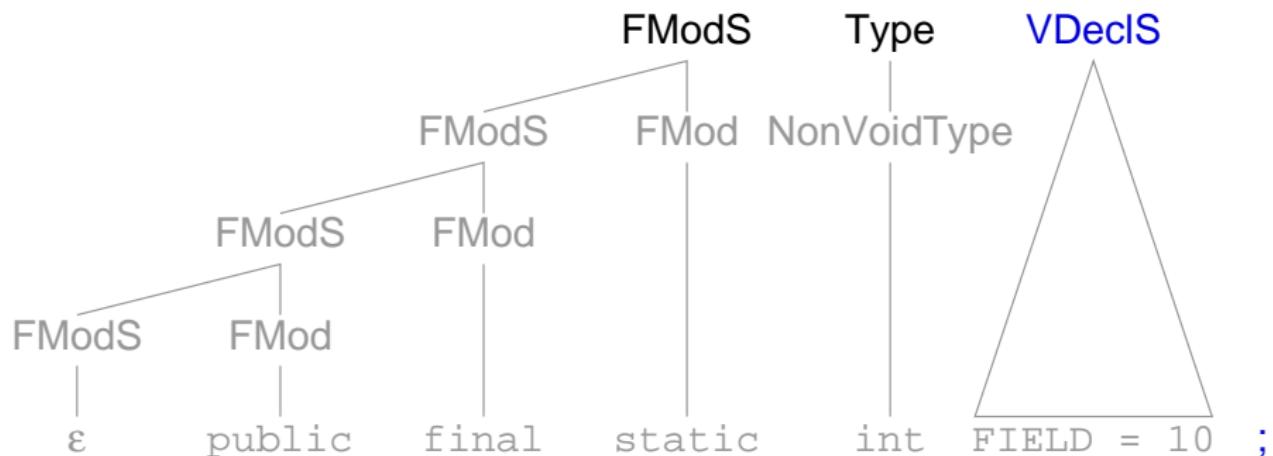


$\$ \parallel \langle FModS \rangle \langle Type \rangle \langle VDeclS \rangle ; \$$
 $\models_{shift} \$ \langle FModS \rangle \parallel \langle Type \rangle \langle VDeclS \rangle ; \$$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example

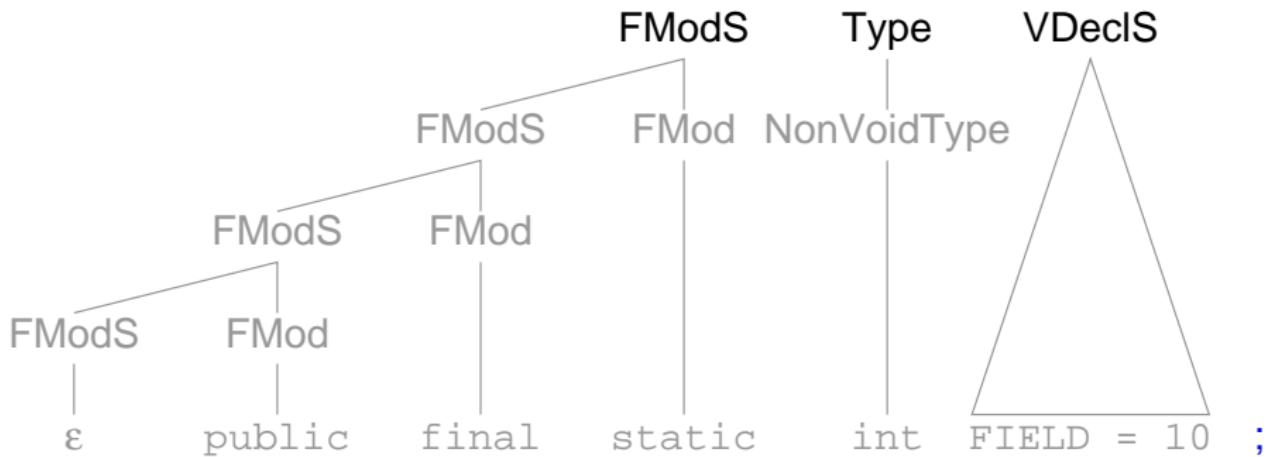


$$\begin{aligned}
 & \$ <FModS> \parallel <Type> <VDeclS> ; \\
 \models_{\text{shift}} & \$ <FModS> <Type> \parallel <VDeclS> ;
 \end{aligned}$$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example

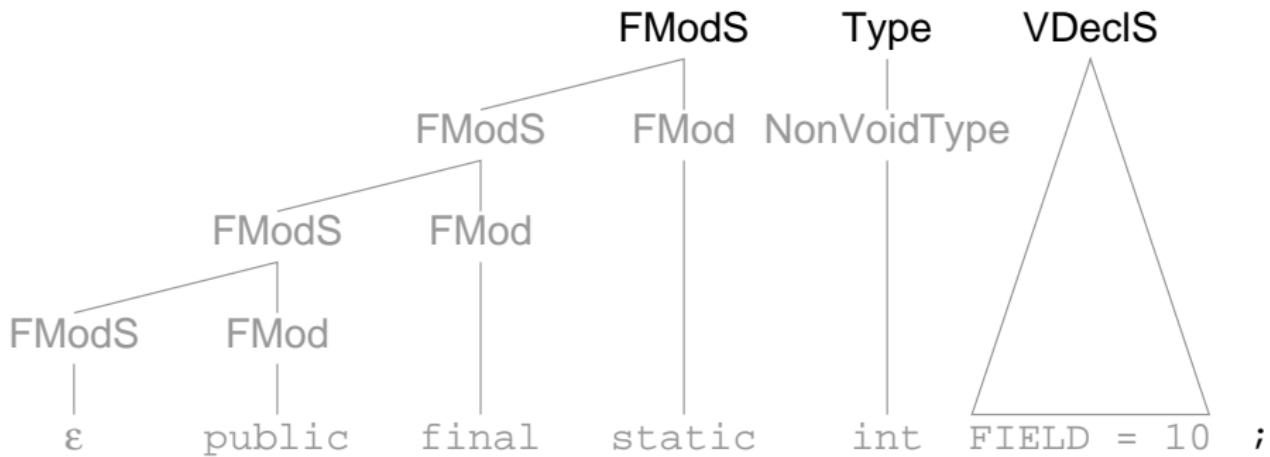


$\$ < FModS > < Type > \parallel < VDeclS > ; \$$
 $\models_{shift} \$ < FModS > < Type > < VDeclS > \parallel ; \$$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example



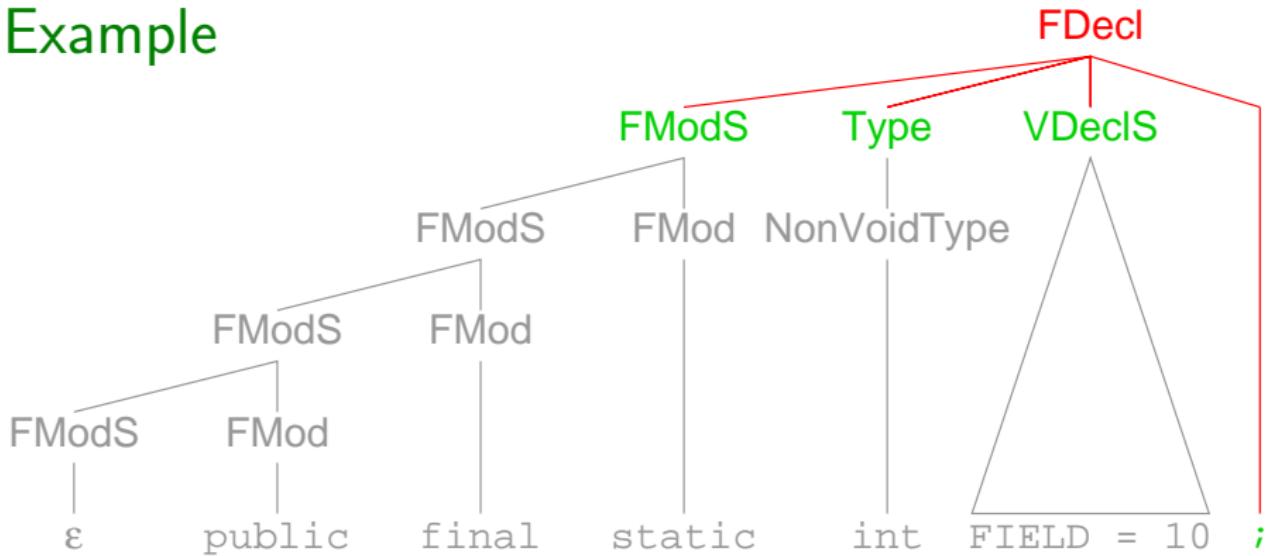
$\$ <FModS><Type><VDeclS> \parallel ; \$$

$\models_{shift} \$ <FModS><Type><VDeclS> ; \parallel \$$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example



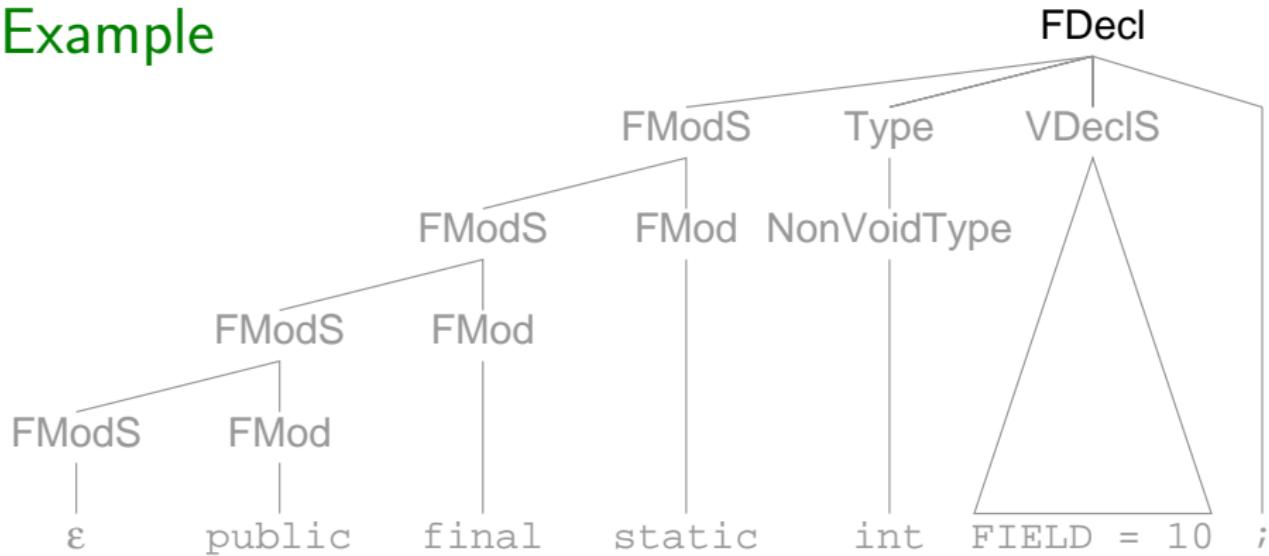
$\$ <FModS><Type><VDeclS> ; \parallel \$$

$\models_{\text{reduce}} \$ \parallel <FDecl> \$$

Noncanonical Parsing

Colmerauer [1970], Szymanski and Williams [1976], Tai [1979]

Example



$\$ \parallel \langle FDecl \rangle \$$
 $\models_{shift} \$ \langle FDecl \rangle \parallel \$$

Noncanonical Lookaheads

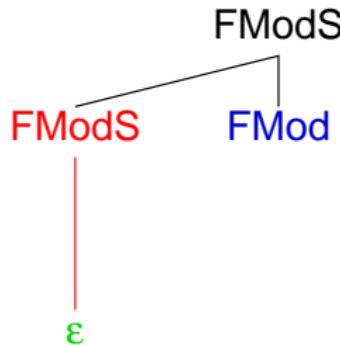
Example

FModS

ε

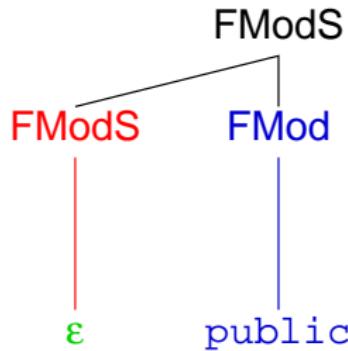
Noncanonical Lookaheads

Example



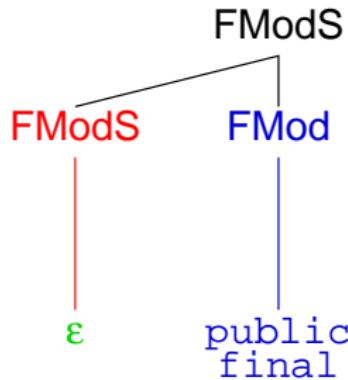
Noncanonical Lookaheads

Example



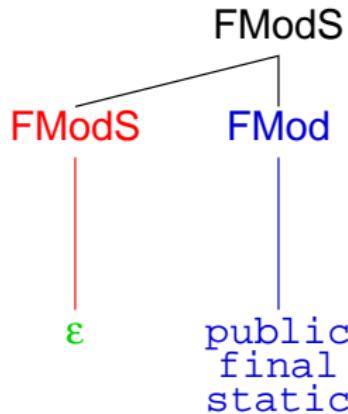
Noncanonical Lookaheads

Example



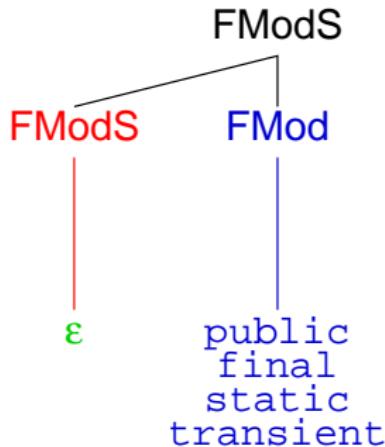
Noncanonical Lookaheads

Example



Noncanonical Lookaheads

Example



Noncanonical Lookaheads

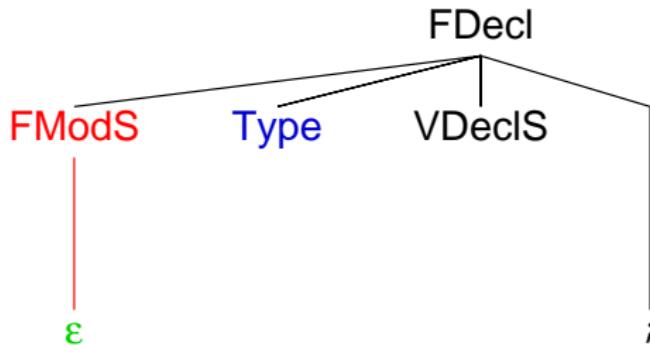
Example

FModS

ε

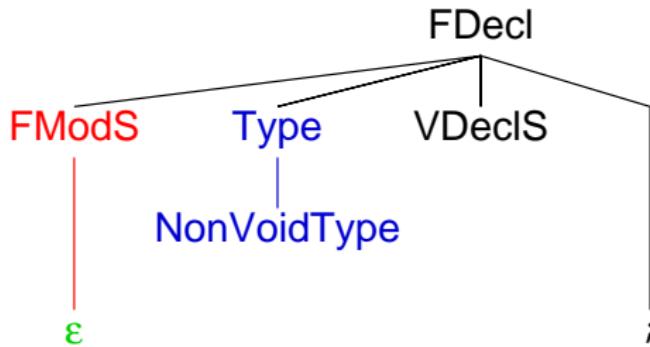
Noncanonical Lookaheads

Example



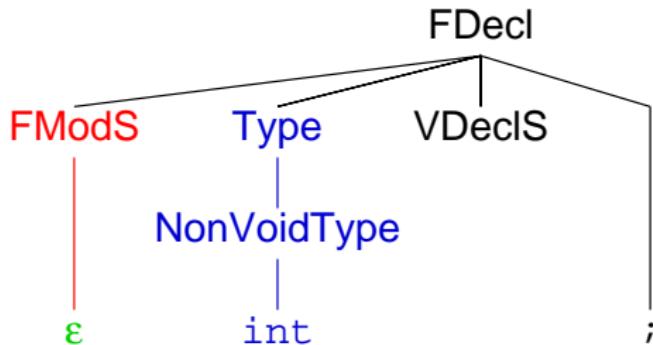
Noncanonical Lookaheads

Example



Noncanonical Lookaheads

Example



Noncanonical Lookaheads

Notation

$\langle FModS \rangle \rightarrow \varepsilon$ {public, final, static, int,
transient, $\langle FMod \rangle$, $\langle Type \rangle$,
 $\langle NonVoidType \rangle$ }

Noncanonical Lookaheads

Comparison

$\langle FModS \rangle \rightarrow \varepsilon$ {public, final, static, int,
transient, $\langle FMod \rangle$, $\langle Type \rangle$,
 $\langle NonVoidType \rangle$ }

$\langle MModS \rangle \rightarrow \varepsilon$ {public, final, static, int,
abstract, $\langle MMod \rangle$, $\langle ReturnType \rangle$,
 $\langle NonVoidType \rangle$ }

Noncanonical Lookaheads

Conflicts

$\langle FModS \rangle \rightarrow \varepsilon$ {public, final, static, int,
transient, $\langle FMod \rangle$, $\langle Type \rangle$,
 $\langle NonVoidType \rangle$ }

$\langle MModS \rangle \rightarrow \varepsilon$ {public, final, static, int,
abstract, $\langle MMod \rangle$, $\langle ReturnType \rangle$,
 $\langle NonVoidType \rangle$ }

Noncanonical Lookaheads

Decisions

$\langle FModS \rangle \rightarrow \varepsilon$ {public, final, static, int,
transient, $\langle FMod \rangle$, $\langle Type \rangle$,
 $\langle NonVoidType \rangle$ }

$\langle MModS \rangle \rightarrow \varepsilon$ {public, final, static, int,
abstract, $\langle MMod \rangle$, $\langle ReturnType \rangle$,
 $\langle NonVoidType \rangle$ }

Noncanonical LALR(1)

Schmitz [2006]

NLALR(1) Construction

- ▶ Easy: computations on the LR(0) automaton
- ▶ Fast: relational expressions

Closing Comments

Noncanonical Parsing

Good generality, Determinism, $\mathcal{O}(n)$ time complexity

Improvements

Better generality: no preset lookahead length

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