

L^AT_EX for Beginners

This short document should help you get started with L^AT_EX. You can also find a lot of documentation on the web, for instance <http://en.wikibooks.org/wiki/LaTeX>, and of course the full documentation of packages on CTAN <http://ctan.org/>.

1 Installing a L^AT_EX Distribution

The T_EX “environment” is a pretty large one, including processing programs, libraries, fonts, and many extensions.

1.1 Installing a Distribution

The most comprehensive distribution is T_EX Live <http://tug.org/texlive/>, and can be installed on your favorite operating system:

GNU/Linux preferably use the package manager of your GNU/Linux distribution to install T_EX Live,

MacOS X use MacT_EX <http://tug.org/mactex/> or your package manager (for instance MacPorts <http://macports.org>),

Microsoft Windows use the T_EX Live distribution for Windows or MiK_TE_X <http://miktex.org/>.

Unless you are short on disk space, you can start right away with a full installation (which might use several GiBs!).

1.2 Updating a Distribution

If you installed your T_EX distribution through a general-purpose package manager, use that. If you installed T_EX Live directly, then you can maintain your T_EX installation through the *T_EX Live package manager tlmgr*: see <http://www.tug.org/texlive/tlmgr.html>. If you installed MiK_TE_X, there is a *MiK_TE_X update wizard* tool to maintain your installation: see <http://docs.miktex.org/2.9/manual/updating.html>.

2 Running L^AT_EX

A L^AT_EX document is a plain text document. It is interpreted by a T_EX processor that outputs a formatted document (here a PDF file).

2.1 The Basics

Example 1 (A Minimal Document). A minimal L^AT_EX document looks like the following:

```

1 \documentclass{article}
2 \begin{document}
3   Hello, world!
4 \end{document}

```

The “`\documentclass{article}`” instruction selects the type of document we want to generate (here an “article”), while the “document” environment delimits the main contents of our document.

If this is the content of a file named `example1.tex`, then running

```
# pdflatex example1.tex
```

on the command line will result in a PDF file `example1.pdf` (among others).

2.1.1 Basic Typesetting

Paragraphs are simply separated by blank lines:

```

1 Lorem ipsum dolor sit amet, consectetur adipiscing elit. Ut molestie
2 nunc ac erat consectetur scelerisque. Lorem ipsum dolor sit amet,
3 consectetur adipiscing elit. Sed ante velit, aliquam at faucibus
4 sed, varius in metus. Curabitur ut libero et ligula mollis fermentum
5 a sit amet urna. Etiam eu sapien leo, ac lobortis odio. Donec
6 tempor, magna vel lobortis blandit, quam mi fringilla neque, nec
7 sagittis nisi leo eu tortor. Nunc rhoncus urna a lectus auctor eu
8 fringilla nulla accumsan.
9
10 Aliquam erat volutpat. Vivamus euismod consectetur
11 ultricies. Maecenas vel sem sed lectus consequat vulputate. Etiam in
12 orci massa. Sed eros nisl, aliquam vitae pulvinar nec, lobortis sit
13 amet nisl. Donec metus leo, accumsan et ultricies vel, elementum id
14 leo. Donec tempus nibh sed est interdum cursus.

```

will result in two paragraphs:

Lorem ipsum dolor sit amet, consectetur adipiscing elit. Ut molestie nunc ac erat consectetur scelerisque. Lorem ipsum dolor sit amet, consectetur adipiscing elit. Sed ante velit, aliquam at faucibus sed, varius in metus. Curabitur ut libero et ligula mollis fermentum a sit amet urna. Etiam eu sapien leo, ac lobortis odio. Donec tempor, magna vel lobortis blandit, quam mi fringilla neque, nec sagittis nisi leo eu tortor. Nunc rhoncus urna a lectus auctor eu fringilla nulla accumsan.

Aliquam erat volutpat. Vivamus euismod consectetur ultricies. Maecenas vel sem sed lectus consequat vulputate. Etiam in orci massa. Sed eros nisl, aliquam vitae pulvinar nec, lobortis sit amet nisl. Donec metus leo, accumsan et ultricies vel, elementum id leo. Donec tempus nibh sed est interdum cursus.

Paragraph jumps can also be triggered through the “`\par`” directive.

L^AT_EX handles rather well line breaks, page breaks, hyphenation, etc., thus there is usually no need to use the commands “`\`”, “`\newline`”, or “`\linebreak`” for line breaks, “`\clearpage`” or “`\pagebreak`” for page breaks, nor “`\-`” for hyphenations.

Text styles, to be used sparingly in the main text, are set through the commands “`\textbf{...}`” for **bold face**, “`\textit{...}`” for *italics*, “`\textsl{...}`” for *slanted*, “`\textsf{...}`”

for sans-serif, “`\texttt{...}`” for typewriter, and “`\textsc{...}`” for SMALL CAPS. Much more useful: the *emphasis* “`\emph{...}`”, which emphasizes depending on the surrounding font.

Finally, a number of symbols are reserved and should be escaped or replaced: “`\%`” because “`%`” is used to start a comment line, “`\$`” because “`$`” delimits inline maths, “`\~{}`” because “`~`” denotes an unbreakable space, “`\#`”, “`\-`”, “`\&`”, “`\{`”, “`\}`”, and “`\textbackslash`” (or in math mode) for “`\`”, and “`\textasciicircum{}`” (or “`\hat{}`” in math mode) for “`^`”.

2.1.2 Sectioning

The text can be sectioned into parts, chapters etc. using “`\part{Title of the Part}`”, “`\chapter{Title of the Chapter}`” (parts and chapters are not available in the “`article`” class of documents; one needs to use e.g. “`book`” or “`report`”), “`\section{Title of the Section}`”, “`\subsection{...}`”, “`\subsubsection{...}`”, “`\paragraph{...}`”, and “`\subparagraph{...}`”. Appendices start after the “`\appendix`” command.

A table of contents is automatically inserted by the “`\tableofcontents`” command; this requires *two* compilations by the `pdflatex` program: a first pass generates an auxiliary file which is read during the second pass to construct the table.

Here is for instance the table of contents for this document:

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2.1.3 Lists

Example 2 (Lists). L^AT_EX provides three predefined list environments: “itemize”, “enumerate”, and “description”:

```

1 \begin{description}
2 \item[itemize] lists are used for generic, “bulleted lists”:
3   \begin{itemize}
4     \item something
5     \begin{itemize}
6       \item that we can refine into something else
7       \item or yet another thing
8     \end{itemize}
9     \item something different.
10  \end{itemize}
11 \item[enumerate] lists are for numbered lists:
12   \begin{enumerate}
13     \item a first point
14     \begin{enumerate}
15       \item a first subpoint
16       \item a second subpoint
17     \end{enumerate}
18     \item a second point.
19   \end{enumerate}
20 \item[description] lists are for lists of entries along with their
21   descriptions.
22 \end{description}

```

results in

<p>itemize lists are used for generic, “bulleted lists”:</p> <ul style="list-style-type: none"> – something – that we can refine into something else – or yet another thing – something different. <p>enumerate lists are for numbered lists:</p> <ol style="list-style-type: none"> 1. a first point <ol style="list-style-type: none"> (a) a first subpoint (b) a second subpoint 2. a second point. <p>description lists are for lists of entries along with their descriptions.</p>

2.1.4 Mathematics

Math Mode L^AT_EX has two main modes of interpretation: *text mode* for plain text, and *math mode* for mathematics. The latter can be used *inline* by delimiting with “\$...\$”, for instance to write $(x + y)^n = \sum_{k=0}^n \binom{n}{k} x^{n-k} y^k$, or as a *block* using “\$\$...\$\$” or “[...]”,

as in

$$(x + y)^n = \sum_{k=0}^n \binom{n}{k} x^{n-k} y^k ,$$

which was typeset by

```
$$ (x+y)^n = \sum_{k=0}^n \binom{n}{k} x^{n-k} y^k ; $$
```

(the “`\binom`” command requires “`amsmath`”; see Section 3.2).

Equations When writing maths in blocks, the environments proposed by $\mathcal{A}\mathcal{M}\mathcal{S}$ -L^AT_EX are recommended instead of the plain “`$$...$$`”; for instance,

```
1 \usepackage{amsmath}
2 ...
3 \begin{equation}
4 \quad (x+y)^n = \sum_{k=0}^n \binom{n}{k} x^{n-k} y^k ;
5 \end{equation}
6 \end{document}
```

results in

$$(x + y)^n = \sum_{k=0}^n \binom{n}{k} x^{n-k} y^k . \quad (1)$$

See Section 3.2 for more on $\mathcal{A}\mathcal{M}\mathcal{S}$ -L^AT_EX.

Symbols L^AT_EX comes with a lot of commands for mathematical symbols: see <http://www.ctan.org/tex-archive/info/symbols/comprehensive/symbols-a4.pdf> for a *big* list. Beware that latin characters in math mode are interpreted as *variables* and typeset accordingly; contrast

```
1 \begin{align}
2 \quad \operatorname{argmax}_{i \in I} & \quad \mathit{argmax}_{i \in I} & \quad \mathop{\mathrm{argmax}}_{i \in I} \\
3 \end{align}
```

$$\operatorname{argmax}_{i \in I} \qquad \mathit{argmax}_{i \in I} \qquad \mathop{\mathrm{argmax}}_{i \in I} \quad (2)$$

2.1.5 Tables

Tables tend to be annoying in L^AT_EX. The basic environment “tabular” is rather poor, and one often has to resort to the more advanced environments provided by the packages “array” (for fine-grained column specifications), “multirow” (for cells spanning multiple rows), “tabularx” (for extensible columns), and “longtable” (for tables spanning over several pages).

Example 3. The table layouts found in L^AT_EX documents tend to overuse vertical lines, and to have improper spacing. Here is an example of the nice results one obtains with the “booktabs” package (see Section 3 on the use of packages):

```

1 \usepackage{booktabs}
2 ...
3 \begin{tabular}{lccc} % 4 columns: 1 left-aligned and 3 centered
4 \toprule
5 \multicolumn{3}{c}{Problems} \\
6 \cmidrule(r){1-3}
7 Name & Input & Question & Complexity \\
8 \midrule
9 Membership &  $\langle \mathcal{A}, w \rangle$  &  $w \in L(\mathcal{A})?$  & NLOGSPACE-complete \\
10  $\$w \in L(\mathcal{A})?\$ & \textsc{NLogSpace}-complete \\
11 Emptiness &  $\langle \mathcal{A} \rangle$  &  $L(\mathcal{A}) = \emptyset?$  & NLOGSPACE-complete \\
12  $\$L(\mathcal{A}) = \emptyset?\$ & \textsc{NLogSpace}-complete \\
13 Universality &  $\langle \mathcal{A} \rangle$  &  $L(\mathcal{A}) = \Sigma^*?$  & PSPACE-complete \\
14  $\$L(\mathcal{A}) = \Sigma^*?\$ & \textsc{PSPACE}-complete \\
15 \bottomrule
16 \end{tabular}$$$ 
```

results in

Problems			
Name	Input	Question	Complexity
Membership	$\langle \mathcal{A}, w \rangle$	$w \in L(\mathcal{A})?$	NLOGSPACE-complete
Emptiness	$\langle \mathcal{A} \rangle$	$L(\mathcal{A}) = \emptyset?$	NLOGSPACE-complete
Universality	$\langle \mathcal{A} \rangle$	$L(\mathcal{A}) = \Sigma^*?$	PSPACE-complete

2.2 Further Tools

More T_EX Dialects L^AT_EX is by no means the only text processor built on top of T_EX. One alternative is CONTEX_T <http://wiki.contextgarden.net/>, which emphasizes the ease of modifying the layout and typography, or X_EL_AT_EX <http://scripts.sil.org/xetex>, which provides an improved support of fonts and typography. Both are distributed along with your T_EX environment.

2.2.1 BibT_EX

L^AT_EX manages bibliographies as provided by a “thebibliography” environment. It is however much easier to rely on BibT_EX to generate the contents of this environment, based on the citations found in the main text.

Example 4 (Bibliography). A citation in the main text is triggered by the “\cite{key}” command, where “key” is the key of the bibliographic entry of interest. When running `pdflatex`, information about citations is saved to an `.aux` auxiliary file, which BibT_EX reads to generate a `.bbl` file containing the desired “thebibliography” environment. This file is read on a next pass of `pdflatex`, and one more pass is necessary before the links between the citations and the bibliography are made:

Contents of `example2.tex`

```

1 \documentclass{article}
2 \begin{document}
3 See \cite{TeX,LaTeX}, but really look at \cite{latexcomp}.
4
5 \bibliographystyle{plain}
6 \bibliography{mybib}
7 \end{document}

```

Contents of `mybib.bib`

```

1 @book{TeX,
2   author   = {Donald E. Knuth},
3   title    = {The \TeX{} book},
4   publisher = {Addison–Wesley},
5   year     = 1984,
6 }
7 @book{LaTeX,
8   author   = {Leslie Lamport},
9   title    = {\LaTeX\string: {A} Document Preparation System},
10  publisher = {Addison–Wesley},
11  edition   = 2,
12  year      = 1994,
13 }
14 @book{latexcomp,
15   author   = {Frank Mittelbach and Michel Goossens},
16   title    = {The \LaTeX\ Companion\string: Tools and Techniques
17             for Computer Typesetting},
18   publisher = {Addison–Wesley},
19   edition   = 2,
20   year      = 2004,
21 }

```

Then running

```

1 # pdflatex example2
2 # bibtex example2
3 # pdflatex example2
4 # pdflatex example2

```

will result in:

See [1; 2], but really look at [3].

References

- [1] Donald E. Knuth. *The T_EXbook*. Addison-Wesley, 1984.
- [2] Leslie Lamport. *L^AT_EX: A Document Preparation System*. Addison-Wesley, second edition, 1994.
- [3] Frank Mittelbach and Michel Goossens. *The L^AT_EX Companion: Tools and Techniques for Computer Typesetting*. Addison-Wesley, second edition, 2004.

2.2.2 Indexing

An index for the document can be generated automatically using the “makeidx” package. The command “\makeindex” must also be used in the preamble of the document, and a command “\index{key}” each time an index entry should be created for the provided *key*.

L^AT_EX then generates a .idx file, which is processed by the makeindex program to generate a .ind file, which is included in the document thanks to the “\printindex” command.

Example 5 (Indexing).

Contents of `example3.tex`

```

1 \documentclass{article}
2 \usepackage{makeidx}
3 \makeindex
4 \begin{document}
5 Here is an \emph{entry}\index{entry}.
6
7 \printindex
8 \end{document}

```

can be processed by

```

# pdflatex example3
# makeindex example3
# pdflatex example3

```

It will not result in anything fancy; here is rather the index of this document:

Index

- commands
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 `\dots` (\dots), 10, 12
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 `\geq` (\geq), 12
 `\hat` ($\hat{}$), 3
 `\in` (\in), 5, 10
 `\langle` (\langle), 6, 10, 12
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3 Packages

There are many, *many* packages available for L^AT_EX, BibT_EX and other T_EX-related software (the current file index of CTAN weights more than 10MiB). L^AT_EX packages gather sets of macro definitions and redefine some of the L^AT_EX internals.

Example 6 (Loading Packages). A package is loaded through a command of the form “`\usepackage[options]{package}`”. The command has to appear in the *preamble*, i.e. after the “`\documentclass`” directive and before the beginning of the “document” environment. Here is an example that loads “babel” and “inputenc”:

```

1 \documentclass{article}
2 \usepackage[français]{babel} % French typography and hyphenation
3 \usepackage[latin1]{inputenc} % Allow accented chars from iso-8859-1
4 \begin{document}
5   Une machine de \bsc{Turing} est un tuple  $\mathcal{M} = \langle Q, \Sigma, \Gamma, \delta, q_0, F \rangle$  :  $Q$  est un ensemble fini
6   d'états,  $\Sigma$  et  $\Gamma$  sont des alphabets d'entrée et de travail respectivement,  $\delta \subseteq Q \times \Gamma \times Q \times \Gamma \times \{\leftarrow, \rightarrow\}$  est une
7   relation de transition associant à un état courant et un symbole de l'espace de travail un nouvel état, un symbole de remplacement, et une
8   direction de la tête de lecture,  $q_0 \in Q$  est un état initial,
9   et  $F \subseteq Q$  est un ensemble d'états finaux.
10
11   Une configuration \dots
12
13 \end{document}

```

results in a document

Une machine de TURING est un tuple $\mathcal{M} = \langle Q, \Sigma, \Gamma, \delta, q_0, F \rangle$: Q est un ensemble fini d'états, Σ et Γ sont des alphabets d'entrée et de travail respectivement, $\delta \subseteq Q \times \Gamma \times Q \times \Gamma \times \{\leftarrow, \rightarrow\}$ est une relation de transition associant à un état courant et un symbole de l'espace de travail un nouvel état, un symbole de remplacement, et une direction de la tête de lecture, $q_0 \in Q$ est un état initial, et $F \subseteq Q$ est un ensemble d'états finaux.

Une configuration ...

Note for instance the inserted unbreakable space before the colon “:”. The “`\bsc`” command enforces the French usage of small-caps with no line breaks for last names.

Let us finish this document with a short overview of a few useful L^AT_EX packages. The purpose of the section is not to explain in details how each package can be used (read the documentation for that!), but to show a few handy ones along with examples of use.

3.1 Bibliographies

The “natbib” package is very useful for author-year references and more flexible citation commands.

Example 7. Contrast Example 4 with the following:

```

1 \usepackage{natbib}
2 ...
3 \Citeauthor{TeX} is the inventor of \TeX, but the text processing
4 tool most people use in mathematics and computer science is the
5 higher-level \LaTeX~\citep{LaTeX}, built on top of \TeX.
6
7 An excellent reference for the management of bibliographies in
8 \LaTeX\ is given by \citet[Chapters~12 and~13]{latexcomp}.
9
10 \bibliographystyle{plainnat}
11 \bibliography{mybib}

```

which results in:

Knuth is the inventor of T_EX, but the text processing tool most people use in mathematics and computer science is the higher-level L^AT_EX (Lampport, 1994), built on top of T_EX.

An excellent reference for the management of bibliographies in L^AT_EX is given by Mittelbach and Goossens (2004, Chapters 12 and 13).

References

Donald E. Knuth. *The T_EXbook*. Addison-Wesley, 1984.

Leslie Lampport. *L^AT_EX: A Document Preparation System*. Addison-Wesley, second edition, 1994.

Frank Mittelbach and Michel Goossens. *The L^AT_EX Companion: Tools and Techniques for Computer Typesetting*. Addison-Wesley, second edition, 2004.

Note that we used a different, “natbib”-compliant style for the bibliography, namely “plainnat” instead of “plain”.

3.2 Mathematics

The main package for mathematics is $\mathcal{A}\mathcal{M}\mathcal{S}$ -L^AT_EX, loaded through the package “amsmath”. More packages should be loaded along with it, notably “amssymb” for additional symbols, and possibly “mathtools” for some interesting additions to $\mathcal{A}\mathcal{M}\mathcal{S}$ -L^AT_EX.

Among the many features of $\mathcal{A}\mathcal{M}\mathcal{S}$ -L^AT_EX, let us mention the environments for equations: “equation”, “align”, “gather”, “multline”, and their starred versions (which do not display equation numbers). Also handy are the commands “\tag” (to add text between parenthesis instead of the equation number) and “\text” (to go back to text mode inside math mode).

Theorems and other similar environments are usually defined using the “amsthm” package (a more recent but also less stable alternative is “thmtools”).

Example 8. A typical declaration for theorem-like environments would be

```

1 \theoremstyle{break}
2 \newtheorem{theorem}{Theorem}

```

```

3 \newtheorem{lemma}{Lemma}
4 \newtheorem{proposition}{Proposition}
5 \newtheorem{corollary}{Corollary}
6 \theoremstyle{definition}
7 \newtheorem{definition}{Definition}
8 \newtheorem{example}{Example}
9 \theoremstyle{remark}
10 \newtheorem{remark}{Remark}

```

These newly-created environments can then be used:

```

1 \begin{lemma}[Context–Freeness]
2   Fix a context–free grammar
3    $\mathcal{G} = \langle \Sigma, N, P, S \rangle$ ,  $V = N \cup \Sigma$ , and
4   let  $m \geq 1$ . If  $\alpha_1, \dots, \alpha_m, \beta$  are sequences
5   in  $V^*$ 
6   s.t.  $\alpha_1 \cdots \alpha_m \xrightarrow{\mathcal{G}} \beta$ 
7   for some  $n \geq 0$ , then there exist  $n_1, \dots, n_m$  in
8    $\mathbb{N}$  and  $\beta_1, \dots, \beta_m$  in  $V^*$  s.t.
9    $n = n_1 + \dots + n_m$ ,  $\beta = \beta_1 \cdots \beta_m$ , and for all
10   $1 \leq i \leq m$ ,  $\alpha_i \xrightarrow{\mathcal{G}} \beta_i$ .
11 \end{lemma}
12 \begin{proof}
13   By induction on  $n$ .
14
15   For the base case  $n=0$ , the lemma holds when defining  $n_i=0$ 
16   and  $\beta_i = \alpha_i$  for each  $1 \leq i \leq m$ .
17
18   For the induction step, given a derivation in  $n+1$  steps, we can
19   isolate a first step:
20   \begin{align*}
21     & \alpha_1 \cdots \alpha_m \\
22     & \&= \alpha_1 \cdots \alpha'_j \alpha''_j \cdots \alpha_m \\
23     & \quad \tag{by setting  $\alpha_j = \alpha'_j \alpha''_j$ } \\
24     & \& \xrightarrow{\mathcal{G}} \alpha_1 \cdots \alpha'_j \gamma \alpha''_j \\
25     & \quad \cdots \alpha_m \\
26     & \quad \tag{by some rule  $A \rightarrow \gamma$  in  $P$ } \\
27     & \& \xrightarrow{\mathcal{G}} \alpha_1 \cdots \alpha'_j \beta_j \cdots \alpha_m
28   \end{align*}
29   By induction hypothesis, these last  $n$  steps imply the
30   existence of  $n'_1, \dots, n'_m$  in
31    $\mathbb{N}$  and  $\beta_1, \dots, \beta_m$  in  $V^*$  s.t.
32    $n = n'_1 + \dots + n'_m$ ,  $\beta = \beta_1 \cdots \beta_m$ , and for all
33    $1 \leq i \leq m$ ,
34    $\alpha_i \xrightarrow{\mathcal{G}} \beta_i$ ; in particular,
35   \begin{equation*}
36     \alpha_j = \alpha'_j \alpha''_j \\
37     \xrightarrow{\mathcal{G}} \alpha'_j \gamma \alpha''_j \\
38     \xrightarrow{\mathcal{G}} \alpha'_j \beta_j \cdots \alpha''_j
39   \end{equation*}
40   Then, setting  $n_j = n'_j + 1$  and  $n_i = n'_i$  for all  $i \neq j$ 
41   proves the lemma.
42 \end{proof}

```

As you can see, “amsthm” also provides a “proof” environment:

Lemma 1 (Context-Freeness). *Fix a context-free grammar $\mathcal{G} = \langle \Sigma, N, P, S \rangle$, $V = N \uplus \Sigma$, and let $m \geq 1$. If $\alpha_1, \dots, \alpha_m, \beta$ are sequences in V^* s.t. $\alpha_1 \cdots \alpha_m \Rightarrow_{\mathcal{G}}^n \beta$ for some $n \geq 0$, then there exist n_1, \dots, n_m in \mathbb{N} and β_1, \dots, β_m in V^* s.t. $n = n_1 + \cdots + n_m$, $\beta = \beta_1 \cdots \beta_m$, and for all $1 \leq i \leq m$, $\alpha_i \Rightarrow_{\mathcal{G}}^{n_i} \beta_i$.*

Proof. By induction on n .

For the base case $n = 0$, the lemma holds when defining $n_i = 0$ and $\beta_i = \alpha_i$ for each $1 \leq i \leq m$.

For the induction step, given a derivation in $n + 1$ steps, we can isolate a first step that exercises some production $A \rightarrow \gamma$ in P :

$$\begin{aligned} \alpha_1 \cdots \alpha_m &= \alpha_1 \cdots \alpha'_j A \alpha''_j \cdots \alpha_m && \text{(by setting } \alpha_j = \alpha'_j A \alpha''_j \text{)} \\ &\Rightarrow_{\mathcal{G}} \alpha_1 \cdots \alpha'_j \gamma \alpha''_j \cdots \alpha_m && \text{(by some rule } A \rightarrow \gamma \text{ in } P \text{)} \\ &\Rightarrow_{\mathcal{G}}^n \beta. \end{aligned}$$

By induction hypothesis, these last n steps imply the existence of n'_1, \dots, n'_m in \mathbb{N} and β_1, \dots, β_m in V^* s.t. $n = n'_1 + \cdots + n'_m$, $\beta = \beta_1 \cdots \beta_m$, and for all $1 \leq i \leq m$, $\alpha_i \Rightarrow_{\mathcal{G}}^{n'_i} \beta_i$; in particular,

$$\alpha_j = \alpha'_j A \alpha''_j \Rightarrow_{\mathcal{G}} \alpha'_j \gamma \alpha''_j \Rightarrow_{\mathcal{G}}^{n'_j} \beta_j.$$

Then, setting $n_j = n'_j + 1$ and $n_i = n'_i$ for all $i \neq j$ proves the lemma. □

3.3 Layout

The “geometry” package features a very comprehensive set of commands for fine-tuning the layout of your pages.

3.4 Drawing

TikZ (standing for “TikZ ist *kein* Zeichenprogramm”, with package name “tikz”) is a highly versatile package for drawing.

Example 9 (Drawing with TikZ). Let us draw an automaton with “tikz”:

```

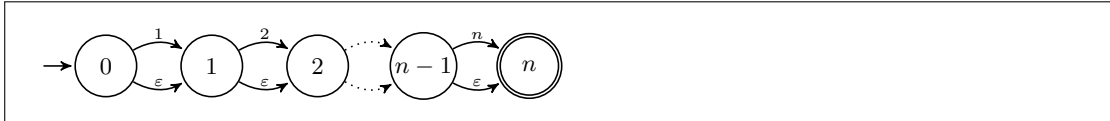
1 \usepackage{tikz}
2 \usetikzlibrary{positioning}
3 \usetikzlibrary{arrows}
4 \usetikzlibrary{automata}
5 ...
6 \begin{tikzpicture}
7   [->, >=>stealth', shorten >=1pt, initial text=, %
8   node distance=2cm, on grid, semithick, auto,
9   inner sep=2pt]
10  \node[state, initial](0) {0};
11  \node[state] (1) [right=of 0] {1};
12  \node[state] (2) [right=of 1] {2};
13  \node[state] (m) [right=of 2] {$n-1$};
14  \node[state, accepting] (n) [right=of m] {$n$};
15  \path[every node/.style={font=\footnotesize}]
16  (0) edge[bend left] node{1} (1)

```

```

17 (0) edge[bend right] node{\varepsilon} (1)
18 (1) edge[bend left] node{2} (2)
19 (1) edge[bend right] node{\varepsilon} (2)
20 (2) edge[bend left,dotted] (m)
21 (2) edge[bend right,dotted] (m)
22 (m) edge[bend left] node{$n$} (n)
23 (m) edge[bend right] node{\varepsilon} (n);
24 \end{tikzpicture}

```



3.5 Graphics

Use the “graphics” package for loading external images into your document. Whenever possible, use *vector graphics*: except at very high resolutions (and then the size of your document blows up), bitmaps have a very poor rendering when printed.

Example 10.

```

1 \includegraphics[height=3cm]{t1c2e.jpg}

```



(As you can see from the “.jpg” extension, this is an instance of the “do as I say, not as I do” principle.)

3.6 Source Code

The “listings” package provides an extensive support for pretty-printing source code in a number of languages (this is what I used throughout this document).

3.7 References and Hyperlinks

The “url” package provides an “`\url{address}`” command for printing URLs. The “hyperref” package redefines much of L^AT_EX internals in order to benefit from some of the capabilities of the PDF format: hyperlinks within the document, a navigation table, meta-information, etc.